ABSTRACT
In fuel gauge solutions, current integration and voltage correlation algorithms suffer from a decrease in accuracy with battery aging and also require extensive data collection. This application report outlines the theory of Impedance Track™ (IT) technology that overcomes these problems. Implementing the IT algorithm in the Texas Instruments bq20z8x family is reviewed and setting the data flash constants associated with the fuel-gauging algorithm is described in detail.

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1 Summary of the Algorithm Operation
The Impedance Track™ gas gauge algorithm(1) uses three types of information to calculate remaining capacity (SBS.RemainingCapacity( )) and full charge capacity (SBS.FullChargeCapacity( )).
1. Chemical: depth of discharge (DOD), and total chemical capacity Qmax
2. Electrical: internal battery resistance dependence on DOD
3. External: load, temperature

SBS.FullChargeCapacity( ) is defined as the amount of charge passed from a fully charged state until the voltage defined in DF:Terminate Voltage flash constant is reached at a given rate of discharge, after subtracting the reserve capacity (DF:Reserve Capacity).

Note that it depends on the rate of discharge and is lower at higher rates and low temperatures because the cell I x R drop causes the Terminate Voltage threshold to be reached earlier.

2 Detailed Description of Parameters Updated by the Gas Gauge Algorithm

2.1 Modes of Algorithm Operation

The algorithm differentiates between charge, discharge, and relaxation modes of operation. During charge mode, the SBS.OperationStatus() [DSG] bit is cleared, and during discharge and relaxation mode, it is set. Entry and exit of each mode is controlled by Data Flash (DF) parameters in the subclass Gas Gauging: Current Thresholds section as illustrated in Figure 1. Charge mode is exited, relaxation mode is entered when SBS.Current() goes below DF:Quit Current and after a DF:Chg Relax Time period. Discharge mode is entered when SBS.Current() goes below DF:Dsg Current Threshold. Discharge mode is exited, relaxation mode is entered when SBS.Current() goes above —DF:Quit Current threshold and after a DF:Dsg Relax Time period. Charge mode is entered when SBS.Current() goes above DF:Chg Current Threshold.

![Figure 1. Example of the Algorithm Operation Mode Changes With Varying SBS.Current()](image)

2.2 Update of Chemical Depth of Discharge (DOD)

The gas gauge updates information on the chemical depth of discharge (DOD) based on open-circuit voltage (OCV) readings when in a relaxed state. This is done for each cell separately. DOD is found by correlating DOD with OCV using a predefined table DOD(OCV,T) stored as reserved data flash parameters. The table is specific for a particular chemistry such as LiCoO2/carbon (default settings), LiMn2O4/carbon, etc., and can be identified by reading the chemistry ID through sending SBS.ManufacturerAccess() command 0008, then reading SBS.ManufacturerAccess(). The gas gauge can be set up for a particular chemistry by using the relevant firmware file (*.senc) that can be downloaded from the bq20zXX production folder on [power.ti.com](http://power.ti.com). See Support of Multiple Chemistries ([SLUA384](http://www.ti.com)) for more details.

Figure 2 shows the timing of parameter updates during the relaxation mode. First, OCV readings and DOD0 calculations are taken after a 30-minute relaxation period has passed. Then, OCV readings continue to be taken every 100 seconds. DOD is calculated based on each measured OCV reading using the linear interpolation DOD = f(OCV,T). Integrated PassedCharge is set to zero at each DOD0 update.
If the current during the OCV reading is non-zero, then an IR correction is done. The first iteration of DOD is found from the uncorrected OCV reading; then the resistance value is found from the R(DOD) table and used to correct the OCV value as $OCV\prime = OCV - I \times R$. Then, the corrected DOD is found from $OCV\prime$. This method achieves the best accuracy if the current during relaxation mode is below the C/20 rate. This is why it is recommended that the DF.Quit Current not exceed C/20.

![Figure 2. Timing of DOD and Qmax Updates During Relaxation Mode](image)

If no DOD has been measured until the relaxation state is exited, the previous DOD is used along with the PassedCharge integrated since the last DOD reading.

During charge and discharge modes, the present DOD is recalculated every second as $DOD = DOD_0 + PassedCharge/Qmax$. DOD is used for determining when a resistance update needs to occur, as well as the starting point for a Remaining Capacity (and FCC) calculation. Remaining capacity calculations occur immediately after discharge onset, at every resistance update, and after entering relaxation mode.

### 2.3 Update of Qmax

Maximal chemical capacity $Q_{\text{max}}$ for each serial cell is stored in Data Flash as $DF:Q_{\text{max}}X$, where $X=0, 1, 2, 3$, the cell serial number.

The GG updates $Q_{\text{max}}$ based on two DOD readings made before and after charge or discharge, for each serial cell separately. For example, DOD is taken during relaxation, then discharge mode starts, and PassedCharge is integrated. Following this, another relaxation mode is entered, and DOD is taken.

DOD1 and DOD2 are calculated from OCV readings in a well-relaxed state, as exemplified in Figure 2. A well-relaxed state is detected if $dV/dt < 4 \, \mu V/s$ or maximal waiting time of 5 hours is exceeded. The first condition is satisfied in typical batteries after about 1 hour if DOD is between 0% and 80%, and 3–4 hours if DOD is above 80%. At a low temperature, relaxation takes a longer time.

In order to ensure high accuracy of DOD measurement, Qmax calculation do not occur if the temperature is above 40°C or below 10°C. It also does not occur if at least one of voltage measurements for DOD1 or DOD2 was taken in the cell voltage range between 3737 mV and 3800 mV because of flat OCV(DOD) dependence in this range. These limits are chemistry dependent and will be specified separately for different chemistries.

Qmax is calculated as $Q_{\text{max}} = \text{PassedCharge} / (DOD_2 - DOD_1)$. 
The data flash constant $DF\text{.} Update\ Status$ increments by 1 when the first Qmax update takes place (e.g., from 4 to 5 if no resistance updates were made, or from 5 to 6 if a resistance update was made). $SBS\text{.} Max\ Error(\ )$ becomes 5% in the first case and 1% in the second case.

PassedCharge has to be more than 37% of $DF:\text{Design Capacity}$ for an update to occur. For the first cycle (with $DF\text{.} Update\ Status = 4$), 90% of $DF:\text{Design Capacity}$ is required because this cycle takes place in the factory settings and Qmax is learned for the first time.

In order to prevent Qmax fluctuations, a first-order smoothing filter is applied to all Qmax readings except in the first cycle. Readings with lower PassedCharge are assigned lower weights in the smoothing.

### 2.4 Update of Resistance

Resistance is updated during discharge, as summarized in Figure 3. The first resistance update happens after 500 seconds, to prevent distortion from transients after load onset.

**Figure 3. Impedance Updates**

Calculation is performed by comparing the measured voltage with the OCV value at the same DOD, that is taken from the OCV(DOD,T) table:

\[
dV = V - OCV(\text{DOD,T}) \\
R(\text{DOD}) = \frac{dV}{I}
\]

Resistance measurements are taken continuously and stored in RAM.

Resistance is updated in the Data Flash (in $DF\text{.} Ra\ Table$) after each 11.1% of DOD charge (1/9th increment) is exceeded (DOD charge is PassedCharge/Qmax). When DOD reaches 77.7%, resistance is updated after each 3.2%. The final resistance update is made after discharge is terminated.

The constant $DF\text{.} Update\ Status$ increments by 1 when the first grid-point resistance update takes place (e.g., from 4 to 5 if no Qmax updates were made before, or from 5 to 6 if Qmax updates were made before).
Before storage to Data Flash, resistance values are normalized to 0°C as \(Ra_{dod} = R_{dod}/\exp(Rb_{dod} \times T)\) where \(R\) is the measured resistance value at a given DOD, \(Rb_{DOD}\) is the value of temperature coefficient of impedance change at a given DOD stored as a reserved data-flash table, and \(T\) is temperature in °C. Note that values of resistance normalized to 0°C are somewhat larger than values at room temperature and so cannot be directly compared with \(R=dV/I\) values.

Resistance values for the grid points with a higher DOD than presently updated are scaled by the same factor as the present grid-point change, e.g., by factor \(Ra_{\text{new}}/Ra_{\text{old}}\). In this way, faster convergence of the resistance profile is achieved.

Values in \(DF.Ra\) Table are stored in \(\Omega\) units, in the format CellX Ra N where X is a cell serial number from 0 to 3, and N is grid-point number from 0 to 14 that corresponds to 11.1% increments of DOD until 77.7%, and then 3.2% increments of DOD. The CellX flag and xCellX flag are used for interchanging the data-flash column usage for reducing the number of DF writes. A flag value of 55 indicates the presently used data column; 00 indicates the presently unused data column.

If during resistance update, the DOD exceeds 100%, or resistance appears negative, which are both indications of a too-small \(DF.QmaxX\) initial guess, \(DF.QmaxX\) increments by 10% and all resistances are recalculated. This is normal behavior during the first learning cycle. However, if the initial guess of \(DF.QmaxX\) was too far from the correct value, the second cycle might be needed to achieve full resistance accuracy. To avoid this, set \(DF.QmaxX\) to a value specified by the cell manufacturer, multiplied by the number of parallel cells.

### 2.5 Update of Temperature Model

Because temperature changes significantly during the course of a discharge, the algorithm needs to be able to predict the future temperature. This is needed for temperature correction of battery impedance \(R = Ra \times \exp(Rb \times T)\) during voltage simulation near the end of a discharge. To achieve this, the algorithm collects \(T(t)\)-dependence data during discharge. It is used to update parameters of a simple thermal model including a heat exchange coefficient and a thermal time constant. These parameters are updated at the same time as resistances. The algorithm also records the outside temperature \(T_{\text{out}}\) during relaxation periods. These parameters are used to define a function \(T(t, T_{\text{start}})\) that calculates a temperature profile starting from present temperature, \(T_{\text{start}}\), and continuing until the end of discharge.

### 2.6 Update of Remaining Capacity (RM) and Full Charge Capacity (FCC)

Update of RM and FCC takes place after each resistance grid-point update, at the end of discharge, and at the exit of relaxation mode.

FCC consists of 3 parts:

\[
SBS.\text{FullChargeCapacity}(\cdot) = Q_{\text{start}} + \text{PassedCharge} + \text{RM}
\]

Components of FCC are indicated in an example in Figure 4.
1. $Q_{\text{start}}$ is the charge that would have passed to make $\text{DOD} = \text{DOD}_0$ from a fully charged state ($\text{DODcharge}$). For a fully charged battery, $Q_{\text{start}} = 0$. $Q_{\text{start}}$ is recalculated at the exit of the relaxation mode. In the case of constant current, it is simply $Q_{\text{start}} = Q_{\text{max}} \times (\text{DOD}_0 - \text{DODcharge})$, but for the constant power case a voltage simulation is run. $\text{DODcharge}$ is assigned equal to $\text{DOD}_0$ at first $\text{DOD}_0$ update, after charge termination by taper current. Note that $\text{DODcharge}$ is somewhat higher than 0 because chargers typically do not charge a battery to full.

2. PassedCharge is the coulomb count integrated during the present discharge or charge, and set to zero at every $\text{DOD}_0$ update.

3. Remaining capacity is calculated after each resistance grid-point update and at the end of discharge.

$SBS.\text{RemainingCapacity}(\ )$ (RM) is calculated using a voltage simulation. The GG starts a simulation at the present $\text{DODstart} = \text{DOD}_0 + \text{PassedCharge}/Q_{\text{max}}$ and continue calculating voltage $V(\text{DODx},T) = \text{OCV}(\text{DODx},T) + I \times R(\text{DODx},T)$ by incrementing DOD with $d\text{DOD}$ increment of 4%. $\text{DOD}[i] = \text{DODstart} + d\text{DOD} \times i$. This incrementing is continued until the simulated voltage $V(\text{DOD}[i])$ becomes less than $DF.\text{Terminate Voltage}$. Once that happens, the final DOD $SBS.\text{RemainingCapacity}(\ ) = (\text{DODfin} - \text{DODstart}) \times Q_{\text{max}}$ is detected. Note that $Q_{\text{max}}$ for the lowest capacity cell is used.

Current that is used in the simulation is the average current during the present discharge (several types of averaging can be selected using $DF:\text{Load Select}$ data flash constant). A simulation can run in constant current mode ($DF:\text{Load Mode} = 0$) or constant power mode ($DF:\text{Load Mode} = 1$).
2.7 Update of SBS.Remaining Capacity( ) and SBS.RemainingStateOfCharge( ) Values

Although SBS.FullChargeCapacity( ) is only updated at a few points during a discharge as previously described, the SBS.RemainingCapacity( ) is updated continuously (every 1 second) based on the integrated charge. SBS.RemainingCapacity( ) = RM − Q_integrated where Q_integrated is charge passed since the last RM calculation. The value of SBS.RemainingCapacity( ) is also used to update SBS.RelativeStateOfCharge( ) every second as SBS.RelativeStateOfCharge( ) = SBS.RemainingCapacity( ) x 100/SBS.FullChargeCapacity( ).

The same value is used to calculate the run-time to empty as SBS.RunTimeToEmpty( ) = SBS.RemainingCapacity( ) / SBS.AverageCurrent( ).

Note that even if a simulation of RM is run in constant power mode (DF:Load Mode = 1), the reporting of SBS.RemainingCapacity( ) and SBS.RemainingRunTime( ) can be done either based on mAh or in 10mWh values. The mAh or mWh reporting depends on the setting of SBS.BatteryMode( ) [CAPACITY_MODE] bit (0=mAh, 1=10mWh). In case of a second setting, the run-time-to-empty is calculated as SBS.RunTimeToEmpty( ) = SBS.RemainingEnergy( ) / SBS.AveragePower( ) and is generally more accurate for most devices because of increased power consumption at low voltages.

2.8 Update of SBS.Max Error()

SBS.Max Error() is an estimate of maximal error of SBS.RSOC. Initially, it is set to 100% because the fuel gauge has no information about the battery. After Qmax is learned, or resistance is learned (as indicated by DF.Update Status = 5), SBS.Max Error changes to 5%. After the second part of the database (resistance or Qmax) is learned (Update Status = 6), SBS.Max Error changes to 1%. SBS.Max Error( ) is increased to reflect the number of cycles since the last Qmax. This is achieved by storing the cycle number when Qmax was last updated in an internal variable Qmax_cycle. SBS.Max Error is then calculated as Max Error + (SBS.Cycle Count() − Qmax_cycle) x 0.05. This means that SBS.Max Error increases by 1% in 20 cycles, e.g., only occasionally is a Qmax update needed to maintain high accuracy.
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