Preface

Read This First

About This Manual

The Texas Instruments TMS320C55x™ DSPLIB is an optimized DSP Function Library for C programmers on TMS320C55x devices. It includes over 50 C-callable assembly-optimized general-purpose signal processing routines. These routines are typically used in computationally intensive real-time applications where optimal execution speed is critical. By using these routines you can achieve execution speeds considerable faster than equivalent code written in standard ANSI C language. In addition, by providing ready-to-use DSP functions, TI DSPLIB can shorten significantly your DSP application development time.

Related Documentation

- Digital Signal Processing with the TMS320 Family (SPR012)
- TMS320C55x DSP CPU Reference Guide (SPRU371)
- TMS320C55x Optimizing C Compiler User’s Guide (SPRU281)

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1.1 DSP Routines

The TI DSPLIB includes commonly used DSP routines. Source code is provided to allow you to modify the functions to match your specific needs.

The routines included within the library are organized into eight different functional categories:

- Fast-Fourier Transforms (FFT)
- Filtering and convolution
- Adaptive filtering
- Correlation
- Math
- Trigonometric
- Miscellaneous
- Matrix

1.2 Features and Benefits

- Hand-coded assembly optimized routines
- C-callable routines fully compatible with the TI C55x compiler
- Fractional Q15-format operand supported
- Complete set of examples on usage provided
- Benchmarks (time and code) provided
- Tested against Matlab™ scripts

1.3 DSPLIB: Quality Freeware That You Can Build On and Contribute To

DSPLIB is a free-of-charge product. You can use, modify, and distribute TI C55x DSPLIB for usage on TI C55x DSPs with no royalty payments. See section 3.7, Where DSPLIB Goes From Here, for details.
Installing DSPLIB

This chapter describes how to install the DSPLIB.

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2.1 DSPLIB Content

The TI DSPLIB software consists of 4 parts:

1) a header file for C programmers under the "include" sub-directory:
   \textit{dsplib.h}

2) One object library under the "lib" sub-directory:
   \textit{55xdsp.lib}

3) One source library to allow function customization by the end user under the "55x_src" sub-directory
   \textit{55xdsp.src}

4) Example programs and linker command files used under the “55x_test” Examples sub-directory.
How to Install DSPLIB

2.2 How to Install DSPLIB

Note:
Read the README.TXT file for specific details of release.

2.2.1 De-Archive DSPLIB

DSPLIB is distributed in the form of an executable self-extracting ZIP file (c55_dsplib.exe). The zip file automatically restores the DSPLIB individual components in the same directory you execute the self extracting file. Following is an example on how to install DSPLIB, just type:

c55_dsplib.exe –d

The DSPLIB directory structure and content you will find is:

c55_dsplib(dir)
55xdsp.lib : use for standards short-call mode
blt55x.bat : re-generate 55xdsp.lib based on 55xdsp.src
examples(dir) : contains one subdirectory for each routine included in the library where you can find complete test cases
include(dir)
dsplib.h : include file with data types and function prototypes
tms320.h : include file with type definitions to increase TMS320 portability
misc.h : include file with useful miscellaneous definitions
doc(dir)
55x_src (dir) : contains assembly source files for functions

2.2.2 Relocate Library File

Copy the C55x DSPLIB object library file, 55xdsp.lib, to your C5500 runtime support library folder.

For example, if your TI C5500 tools are located in c:\ti\c55x\cgtools\bin and c runtime support libraries (rts55.lib etc.) in c:\ti\c55x\cgtools\lib, copy 55xdspilib.lib to this folder. This allows the C55x compiler/linker to find 55xdsp.lib.
2.3 How to Rebuild DSPLIB

2.3.1 For Full Rebuild of 55xdsp.lib
To rebuild 55xdsp.lib, execute the blt55x.bat. This will overwrite any existing 55xdsp.lib.

2.3.2 For Partial Rebuild of 55xdsp.lib
(modification of a specific DSPLIB function, for example fir.asm)

1) Extract the source for the selected function from the source archive:
   `ar55 x 55xdsp.src fir.asm`

2) Re-assemble your new fir.asm assembly source file:
   `asm55 –g fir.asm`

3) Replace the object, fir.obj, in the dsplib.lib object library with the newly formed object:
   `ar55 r 55xdsp.lib fir.obj`
Using DSPLIB

This chapter describes how to use the DSPLIB.

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3.1 DSPLIB Arguments and Data Types

3.1.1 DSPLIB Arguments

DSPLIB functions typically operate over vector operands for greater efficiency. Though these routines can be used to process short arrays or scalars (unless a minimum size requirement is noted), the execution times will be longer in those cases.

- **Vector stride is always equal 1**: vector operands are composed of vector elements held in consecutive memory locations (vector stride equal to 1).

- **Complex elements** are assumed to be stored in a Re-Im format.

- **In-place computation is allowed (unless specifically noted)**: Source operand can be equal to destination operand to conserve memory.

3.1.2 DSPLIB Data Types

DSPLIB handles the following fractional data types:

- **Q.15 (DATA)**: A Q.15 operand is represented by a *short* data type (16 bit) that is predefined as *DATA*, in the *dsplib.h* header file.

- **Q.31 (LDATA)**: A Q.31 operand is represented by a *long* data type (32 bit) that is predefined as *LDATA*, in the *dsplib.h* header file.

- **Q.3.12**: Contains 3 integer bits and 12 fractional bits.

Unless specifically noted, DSPLIB operates on Q15-fractional data type elements. Appendix A presents an overview of Fractional Q formats.
3.2 Calling a DSPLIB Function from C

In addition to installing the DSPLIB software, to include a DSPLIB function in your code you have to:

- Include the `dsplib.h` include file
- Link your code with the DSPLIB object code library, 55xdsp.lib or 55xdspx.lib.
- Use a correct linker command file describing the memory configuration available in your C55x board.

A project file has been included for each function in the examples folder. You can reference function_t.c files for calling a DSPLIB function from C.

The examples presented in this document have been tested using the Texas Instruments C55x Simulator. Customization may be required to use it with a different simulator or development board.

Refer to the TMS320C55x Optimizing C Compiler User’s Guide (SPRU281).

3.3 Calling a DSPLIB Function from Assembly Language Source Code

The TMS320C55x DSPLIB functions were written to be used from C. Calling the functions from assembly language source code is possible as long as the calling-function conforms with the Texas Instruments C55x C compiler calling conventions. Refer to the TMS320C55x Optimizing C Compiler User’s Guide, if a more in-depth explanation is required.

Realize that the TI DSPLIB is not an optimal solution for assembly-only programmers. Even though DSPLIB functions can be invoked from an assembly program, the result may not be optimal due to unnecessary C-calling overhead.

3.4 Where to Find Sample Code

You can find examples on how to use every single function in DSPLIB, in the examples subdirectory. This subdirectory contains one subdirectory for each function. For example, the examples/araw subdirectory contains the following files:

- araw_t.c: main driver for testing the DSPLIB acorr (raw) function.
- test.h: contains input data(a) and expected output data(yraw) for the acorr (raw) function as. This test.h file is generated by using Matlab scripts.
How DSPLIB is Tested – Allowable Error

- test.c: contains function used to compare the output of a raw function with the expected output data.
- ftest.c: contains function used to compare two arrays of float data types.
- ltest.c: contains function used to compare two arrays of long data types.
- ld3.cmd: an example of a linker command you can use for this function.

3.5 How DSPLIB is Tested – Allowable Error

Version 1.0 of DSPLIB is tested against Matlab scripts. Expected data output has been generated from Matlab that uses double-precision (64-bit) floating-point operations (default precision in Matlab). Test utilities have been added to our test main drivers to automate this checking process. Note that a maximum absolute error value (MAXERROR) is passed to the test function, to set the trigger point to flag a functional error.

We consider this testing methodology a good first pass approximation. Further characterization of the quantization error ranges for each function (under random input) as well as testing against a set of fixed-point C models is planned for future releases. We welcome any suggestions you may have on this respect.

3.6 How DSPLIB Deals with Overflow and Scaling Issues

One of the inherent difficulties of programming for fixed-point processors is determining how to deal with overflow issues. Overflow occurs as a result of addition and subtraction operations when the dynamic range of the resulting data is larger than what the intermediate and final data types can contain.

The methodology used to deal with overflow should depend on the specifics of your signal, the type of operation in your functions, and the DSP architecture used. In general, overflow handling methodologies can be classified in five categories: saturation, input scaling, fixed scaling, dynamic scaling, and system design considerations.

It's important to note that a TMS320C55x architectural feature that makes overflow easier to deal with is the presence of guard bits in all four accumulators. The 40-bit accumulators provide eight guard bits that allow up to 256 consecutive multiply-and-accumulate (MAC) operations before an accumulator overrun – a very useful feature when implementing, for example, FIR filters.
There are 4 specific ways DSPLIB deals with overflow, as reflected in each function description:

- **Scaling implemented for overflow prevention**: In this type of function, DSPLIB scales the intermediate results to prevent overflow. Overflow should not occur as a result. Precision is affected but not significantly. This is the case of the FFT functions, in which scaling is used after each FFT stage.

- **No scaling implemented for overflow prevention**: In this type of function, DSPLIB does not scale to prevent overflow due to the potentially strong effect in data output precision or in the number of cycles required. This is the case, for example, of the MAC-based operations like filtering, correlation, or convolutions. The best solution on those cases is to design your system, for example your filter coefficients with a gain less than 1 to prevent overflow. In this case, overflow could happen unless you input scale or you design for no overflow.

- **Saturation implemented for overflow handling**: In this type of function, DSPLIB has enabled the TMS320C55x 32-bit saturation mode (SATD bit = 1). This is the case of certain basic math functions that require the saturation mode to be enabled.

- **Not applicable**: In this type of function, due to the nature of the function operations, there is no overflow.

- **DSPLIB reporting of overflow conditions (overflow flag)**: Due to the sometimes unpredictable overflow risk, most DSPLIB functions have been written to return an overflow flag (`oflag`) as an indication of a potentially dangerous 32-bit overflow. However, because of the guard-bits, the C55x is capable of handling intermediate 32-bit overflows and still produce the correct final result. Therefore, the `oflag` parameter should be taken in the context of a warning but not a definitive error.

As a final note, DSPLIB is provided also in source format to allow customization of DSPLIB functions to your specific system needs.
3.7 Where DSPLIB Goes From Here

We anticipate DSPLIB to improve in future releases in the following areas:

- **Increased number of functions**: We anticipate the number of functions in DSPLIB will increase. We welcome user-contributed code. If during the process of developing your application you develop a DSP routine that seems like a good fit to DSPLIB, let us know. We will review and test your routine and possibly include it in the next DSPLIB software release. Your contribution will be acknowledged and recognized by TI in the Acknowledgments section. Use this opportunity to make your name known by your DSP industry peers. Simply email your contribution To Whom It May Concern: dsph@ti.com and we will contact you.

- **Increased Code portability**: DSPLIB looks to enhance code portability across different TMS320-based platforms. It is our goal to provide similar DSP libraries for other TMS320™ devices, working in conjunction with C55x compiler intrinsics to make C-developing easier for fixed-point devices. However, it’s anticipated that a 100% portable library across TMS320 devices may not be possible due to normal device architectural differences. TI will continue monitoring DSP industry standardization activities in terms of DSP function libraries.
Function Descriptions

This chapter provides descriptions for the TMS330C55x DSPLIB functions.

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4.1 Arguments and Conventions Used

The following convention has been followed when describing the arguments for each individual function:

Table 4-1. Function Descriptions

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<tr>
<th>Argument</th>
<th>Description</th>
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<tr>
<td>$x,y$</td>
<td>argument reflecting input data vector</td>
</tr>
<tr>
<td>$r$</td>
<td>argument reflecting output data vector</td>
</tr>
<tr>
<td>$nx,ny,nn$</td>
<td>arguments reflecting the size of vectors $x,y$, and $r$ respectively. In functions where $nx = nr = nn$, only $nx$ has been used.</td>
</tr>
<tr>
<td>$h$</td>
<td>Argument reflecting filter coefficient vector (filter routines only)</td>
</tr>
<tr>
<td>$nh$</td>
<td>Argument reflecting the size of vector $h$</td>
</tr>
<tr>
<td>DATA</td>
<td>data type definition equating a short, a 16-bit value representing a Q15 number. Usage of DATA instead of short is recommended to increase future portability across devices.</td>
</tr>
<tr>
<td>LDATA</td>
<td>data type definition equating a long, a 32-bit value representing a Q31 number. Usage of LDATA instead of long is recommended to increase future portability across devices.</td>
</tr>
<tr>
<td>ushort</td>
<td>Unsigned short (16 bit). You can use this data type directly, because it has been defined in dsplib.h</td>
</tr>
</tbody>
</table>
4.2 DSPLIB Functions

The routines included within the library are organized into 8 different functional categories:

- FFT
- Filtering and convolution
- Adaptive filtering
- Correlation
- Math
- Trigonometric
- Miscellaneous
- Matrix

Table 4–2 lists the functions by these 8 functional categories.

Table 4–2. Summary Table

(a) FFT

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<th>Functions</th>
<th>Description</th>
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<tr>
<td>void cfft (DATA *x, ushort nx, type)</td>
<td>Radix-2 complex forward FFT – MACRO</td>
</tr>
<tr>
<td>void cfft32 (LDATA *x, ushort nx, type);</td>
<td>32-bit forward complex FFT</td>
</tr>
<tr>
<td>void ciff (DATA *x, ushort nx, type)</td>
<td>Radix-2 complex inverse FFT – MACRO</td>
</tr>
<tr>
<td>void ciff32 (LDATA *x, ushort nx, type);</td>
<td>32-bit inverse complex FFT</td>
</tr>
<tr>
<td>void cbrev (DATA *x, DATA *r, ushort n)</td>
<td>Complex bit-reverse function</td>
</tr>
<tr>
<td>void cbrev32 (LDATA *a, LDATA *r, ushort)</td>
<td>32-bit complex bit reverse</td>
</tr>
<tr>
<td>void rfft (DATA *x, ushort nx, type)</td>
<td>Radix-2 real forward FFT – MACRO</td>
</tr>
<tr>
<td>void rifft (DATA *x, ushort nx, type)</td>
<td>Radix-2 real inverse FFT – MACRO</td>
</tr>
<tr>
<td>void rfft32 (LDATA *x, ushort nx, type)</td>
<td>Forward 32-bit Real FFT (in-place)</td>
</tr>
<tr>
<td>void rifft32 (LDATA *x, ushort nx, type)</td>
<td>Inverse 32-bit Real FFT (in-place)</td>
</tr>
</tbody>
</table>

(b) Filtering and Convolution

<table>
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<th>Functions</th>
<th>Description</th>
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<tr>
<td>ushort fir (DATA *x, DATA *h, DATA *r, DATA *dbuffer, ushort nx, ushort nh)</td>
<td>FIR direct form</td>
</tr>
<tr>
<td>ushort fir2 (DATA *x, DATA *h, DATA *r, DATA *dbuffer, ushort nx, ushort nh)</td>
<td>FIR direct form (Optimized to use DUAL–MAC)</td>
</tr>
<tr>
<td>ushort firs (DATA *x, DATA *h, DATA *r, DATA *dbuffer, ushort nx, ushort nh2)</td>
<td>Symmetric FIR direct form (generic routine)</td>
</tr>
<tr>
<td>Functions</td>
<td>Description</td>
</tr>
<tr>
<td>----------------------------------------------</td>
<td>--------------------------------------------------</td>
</tr>
<tr>
<td>ushort cfir (DATA *x, DATA *h, DATA *r, DATA *dbuf, ushort nx, ushort nh)</td>
<td>Complex FIR direct form</td>
</tr>
<tr>
<td>ushort convol (DATA *x, DATA *h, DATA *r, ushort nr, ushort nh)</td>
<td>Convolution</td>
</tr>
<tr>
<td>ushort convol1 (DATA *x, DATA *h, DATA *r, ushort nr, ushort nh)</td>
<td>Convolution (Optimized to use DUAL–MAC)</td>
</tr>
<tr>
<td>ushort convol2 (DATA *x, DATA *h, DATA *r, ushort nr, ushort nh)</td>
<td>Convolution (Optimized to use DUAL–MAC)</td>
</tr>
<tr>
<td>ushort iircas4 (DATA *x, DATA *h, DATA *r, DATA *dbuf, ushort nbiq, ushort nx)</td>
<td>IIR cascade direct form II. 4 coefficients per biquad.</td>
</tr>
<tr>
<td>ushort iircas5 (DATA *x, DATA *h, DATA *r, DATA *dbuf, ushort nbiq, ushort nx)</td>
<td>IIR cascade direct form II. 5 coefficients per biquad</td>
</tr>
<tr>
<td>ushort iircas51 (DATA *x, DATA *h, DATA *r, DATA *dbuf, ushort nbiq, ushort nx)</td>
<td>IIR cascade direct form I. 5 coefficients per biquad</td>
</tr>
<tr>
<td>ushort iirlat (DATA *x, DATA *h, DATA *r, DATA *pbuf, int nx, int nh)</td>
<td>Lattice inverse IIR filter</td>
</tr>
<tr>
<td>ushort firlat (DATA *x, DATA *h, DATA *r, DATA *pbuf, int nx, int nh)</td>
<td>Lattice forward FIR filter</td>
</tr>
<tr>
<td>ushort firdec (DATA *x, DATA *h, DATA *r, DATA *dbuf, ushort nh, ushort nx, ushort D)</td>
<td>Decimating FIR filter</td>
</tr>
<tr>
<td>ushort firinterp (DATA *x, DATA *h, DATA *r, DATA *dbuf, ushort nh, ushort nx, ushort l)</td>
<td>Interpolating FIR filter</td>
</tr>
<tr>
<td>ushort hilb16 (DATA *x, DATA *h, DATA *r, DATA *dbuf, ushort nx, ushort nh)</td>
<td>FIR Hilbert Transformer</td>
</tr>
<tr>
<td>ushort iir32 (DATA *x, LDATA *h, DATA *r, LDATA *dbuf, ushort nbiq, ushort nr)</td>
<td>Double-precision IIR filter</td>
</tr>
<tr>
<td>ushort dlms (DATA *x, DATA *h, DATA *r, DATA *des, DATA *dbuf, DATA step, ushort nh, ushort nx)</td>
<td>LMS FIR (delayed version)</td>
</tr>
<tr>
<td>ushort oflag = dlmsfast (DATA *x, DATA *h, DATA *r, DATA *des, DATA *dbuf, DATA step, ushort nh, ushort nx)</td>
<td>Adaptive delayed LMS filter (fast implemented)</td>
</tr>
</tbody>
</table>

(c) Adaptive filtering
Table 4–2 Summary Table (Continued)

(d) Correlation

<table>
<thead>
<tr>
<th>Functions</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>ushort acorr (DATA *x, DATA *r, ushort nx, ushort nr, type)</td>
<td>Autocorrelation (positive side only) – MACRO</td>
</tr>
<tr>
<td>ushort corr (DATA *x, DATA *y, DATA *r, ushort nx, ushort ny, type)</td>
<td>Correlation (full-length)</td>
</tr>
</tbody>
</table>

(e) Trigonometric

<table>
<thead>
<tr>
<th>Functions</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>ushort sine (DATA *x, DATA *r, ushort nx)</td>
<td>sine of a vector</td>
</tr>
<tr>
<td>ushort atan2_16 (DATA *q, DATA *i, DATA *r, ushort nx)</td>
<td>Four quadrant inverse tangent of a vector</td>
</tr>
<tr>
<td>ushort atan16 (DATA *x, DATA *r, ushort nx)</td>
<td>Arctan of a vector</td>
</tr>
</tbody>
</table>

(f) Math

<table>
<thead>
<tr>
<th>Functions</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>ushort add (DATA *x, DATA *y, DATA *r, ushort nx, ushort scale)</td>
<td>Optimized vector addition</td>
</tr>
<tr>
<td>ushort expn (DATA *x, DATA *r, ushort nx)</td>
<td>Exponent of a vector</td>
</tr>
<tr>
<td>short bexp (DATA *x, ushort nx)</td>
<td>Exponent of all values in a vector</td>
</tr>
<tr>
<td>ushort logn (DATA *x, LDATA *r, ushort nx)</td>
<td>Natural log of a vector</td>
</tr>
<tr>
<td>ushort log_2 (DATA *x, LDATA *r, ushort nx)</td>
<td>Log base 2 of a vector</td>
</tr>
<tr>
<td>ushort log_10 (DATA *x, LDATA *r, ushort nx)</td>
<td>Log base 10 of a vector</td>
</tr>
<tr>
<td>short maxidx (DATA *x, ushort ng, ushort ng_size)</td>
<td>Index for maximum magnitude in a vector</td>
</tr>
<tr>
<td>short maxidx34 (DATA *x, ushort nx)</td>
<td>Index of the maximum element of a vector ≤ 34</td>
</tr>
<tr>
<td>short maxval (DATA *x, ushort nx)</td>
<td>Maximum magnitude in a vector</td>
</tr>
<tr>
<td>void maxvec (DATA *x, ushort nx, DATA *r_val, DATA *r_idx)</td>
<td>Index and value of the maximum element of a vector</td>
</tr>
<tr>
<td>short minidx (DATA *x, ushort nx)</td>
<td>Index for minimum magnitude in a vector</td>
</tr>
<tr>
<td>short minval (DATA *x, ushort nx)</td>
<td>Minimum element in a vector</td>
</tr>
<tr>
<td>void minvec (DATA *x, ushort nx, DATA *r_val, DATA *r_idx)</td>
<td>Index and value of the minimum element of a vector</td>
</tr>
<tr>
<td>ushort mul32 (LDATA *x, LDATA *y, LDATA *r, ushort nx)</td>
<td>32-bit vector multiply</td>
</tr>
<tr>
<td>short neg (DATA *x, DATA *r, ushort nx)</td>
<td>16-bit vector negate</td>
</tr>
<tr>
<td>short neg32 (LDATA *x, LDATA *r, ushort nx)</td>
<td>32-bit vector negate</td>
</tr>
</tbody>
</table>
Table 4-2  Summary Table (Continued)

<table>
<thead>
<tr>
<th>Description</th>
<th>Functions</th>
</tr>
</thead>
<tbody>
<tr>
<td>sum of squares of a vector (power)</td>
<td>short power (DATA *x, LDATA *r, ushort nx)</td>
</tr>
<tr>
<td>Vector reciprocal</td>
<td>void recip16 (DATA *x, DATA *r, DATA *rexp, ushort nx)</td>
</tr>
<tr>
<td>32-bit by 16-bit long division</td>
<td>void ldiv16 (LDATA *x, DATA *y, DATA *r, DATA *rexp, ushort nx)</td>
</tr>
</tbody>
</table>

(f) Math (Continued)

<table>
<thead>
<tr>
<th>Description</th>
<th>Functions</th>
</tr>
</thead>
<tbody>
<tr>
<td>Square root of a vector</td>
<td>ushort sqrt_16 (DATA *x, DATA *r, short nx)</td>
</tr>
<tr>
<td>Vector subtraction</td>
<td>short sub (DATA *x, DATA *y, DATA *r, ushort nx, ushort scale)</td>
</tr>
</tbody>
</table>

(g) Matrix

<table>
<thead>
<tr>
<th>Description</th>
<th>Functions</th>
</tr>
</thead>
<tbody>
<tr>
<td>matrix multiply</td>
<td>ushort mmul (DATA *x1, short row1, short col1, DATA *x2, short row2, short col2, DATA *r)</td>
</tr>
<tr>
<td>matrix transpose</td>
<td>ushort mtrans (DATA *x, short row, short col, DATA *r)</td>
</tr>
</tbody>
</table>

(h) Miscellaneous

<table>
<thead>
<tr>
<th>Description</th>
<th>Functions</th>
</tr>
</thead>
<tbody>
<tr>
<td>Floating-point to Q15 conversion</td>
<td>ushort fltoq15 (float *x, DATA *r, ushort nx)</td>
</tr>
<tr>
<td>Q15 to floating-point conversion</td>
<td>ushort q15tofl (DATA *x, float *r, ushort nx)</td>
</tr>
<tr>
<td>Random number generation</td>
<td>ushort rand16 (DATA *r, ushort nr)</td>
</tr>
<tr>
<td>Random number generation initialization</td>
<td>void rand16init(void)</td>
</tr>
</tbody>
</table>
Function

ushort oflag = acorr (DATA *x, DATA *r, ushort nx, ushort nr, type)
(defined in araw.asm, abias.asm, aubias.asm)

Arguments

x [nx] Pointer to real input vector of nx real elements. nx ≥ nr
r [nr] Pointer to real output vector containing the first nr elements of the positive side of the autocorrelation function of vector x. r must be different than x (in-place computation is not allowed).

nx Number of real elements in vector x
nr Number of real elements in vector r
type Autocorrelation type selector. Types supported:
- If type = raw, r contains the raw autocorrelation of x
- If type = bias, r contains the biased autocorrelation of x
- If type = unbias, r contains the unbiased autocorrelation of x

oflag Overflow flag.
- If oflag = 1, a 32-bit overflow has occurred
- If oflag = 0, a 32-bit overflow has not occurred

Description

Computes the first nr points of the positive side of the autocorrelation of the real vector x and stores the results in real output vector r. The full-length autocorrelation of vector x will have 2\*nx−1 points with even symmetry around the lag 0 point (r[0]). This routine provides only the positive half of this for memory and computational savings.

Algorithm

Raw Autocorrelation

\[ r[j] = \sum_{k=0}^{nx-j-1} x[j + k] \times [k] \quad 0 \leq j \leq nr \]

Biased Autocorrelation

\[ r[j] = \frac{1}{nx} \sum_{k=0}^{nx-j-1} x[j + k] \times [k] \quad 0 \leq j \leq nr \]

Unbiased Autocorrelation

\[ r[j] = \frac{1}{(nx - \text{abs}(j))} \sum_{k=0}^{nx-j-1} x[j + k] \times [k] \quad 0 \leq j \leq nr \]
Overflow Handling Methodology  No scaling implemented for overflow prevention

Special Requirements  x array in internal memory (coefficient pointer CDP used to address it)

Implementation Notes

☐ Special debugging consideration: This function is implemented as a macro that invokes different autocorrelation routines according to the type selected. As a consequence the acorr symbol is not defined. Instead the acorr_raw, acorr_bias, acorr_unbias symbols are defined.

☐ Autocorrelation is implemented using time-domain techniques

Example  See examples/abias, examples/aubias, examples/araw subdirectories

Benchmarks  (preliminary)

Cycles†

<table>
<thead>
<tr>
<th></th>
<th>Abias:</th>
<th>Araw:</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Core:</td>
<td>Core:</td>
</tr>
<tr>
<td>nr even</td>
<td>[(4 * nx - nr * (nr + 2) + 20) / 8] * nr</td>
<td>[(4 * nx - nr * (nr + 2) + 28) / 8] * nr</td>
</tr>
<tr>
<td>nr odd</td>
<td>[(4 * nx - (nr - 1) * (nr + 1) + 20) / 8] * (nr - 1) + 10</td>
<td>[(4 * nx - (nr - 1) * (nr + 1) + 28) / 8] * (nr - 1) + 13</td>
</tr>
<tr>
<td>nr = 1:</td>
<td>(nx + 2)</td>
<td>(nx + 1)</td>
</tr>
<tr>
<td>Overhead:</td>
<td></td>
<td></td>
</tr>
<tr>
<td>nr even</td>
<td>90</td>
<td>34</td>
</tr>
<tr>
<td>nr odd:</td>
<td>83</td>
<td>35</td>
</tr>
<tr>
<td>nr = 1:</td>
<td>59</td>
<td>30</td>
</tr>
</tbody>
</table>

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).
Vector Add

**Function**

```c
ushort oflag = add (DATA *x, DATA *y, DATA *r, ushort nx, ushort scale)
```
(defined in add.asm)

**Arguments**

- **x[nx]** Pointer to input data vector 1 of size nx. In-place processing allowed (r can be = x = y)
- **y[nx]** Pointer to input data vector 2 of size nx
- **r[nx]** Pointer to output data vector of size nx containing
  - (x+y) if scale = 0
  - (x+y)/2 if scale = 1
- **nx** Number of elements of input and output vectors.
  - nx \(\geq 4\)
- **scale** Scale selection
  - If scale = 1, divide the result by 2 to prevent overflow
  - If scale = 0, do not divide by 2
- **oflag** Overflow flag.
  - If oflag = 1, a 32-bit overflow has occurred
  - If oflag = 0, a 32-bit overflow has not occurred

**Cycles**†

<table>
<thead>
<tr>
<th></th>
<th>Aubias:</th>
</tr>
</thead>
<tbody>
<tr>
<td>Core:</td>
<td></td>
</tr>
<tr>
<td>n even:</td>
<td></td>
</tr>
<tr>
<td>n odd:</td>
<td></td>
</tr>
<tr>
<td>n = 1:</td>
<td></td>
</tr>
<tr>
<td>Overhead:</td>
<td></td>
</tr>
<tr>
<td>Code size (in bytes)</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Abias: 226</td>
</tr>
<tr>
<td></td>
<td>Araw: 178</td>
</tr>
<tr>
<td></td>
<td>Aubias: 308</td>
</tr>
</tbody>
</table>

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).

---

*Function Descriptions*
atan2_16

**Description**  This function adds two vectors, element by element.

**Algorithm**  
```
for (i = 0; i < nx; i++)  z(i) = x(i) + y(i)
```

**Overflow Handling Methodology**  Scaling implemented for overflow prevention (user selectable)

**Special Requirements**  none

**Implementation Notes**  none

**Example**  See examples/add subdirectory

**Benchmarks**  
(preliminary)

<table>
<thead>
<tr>
<th>Cycles†</th>
<th>Core: 3 * nx</th>
</tr>
</thead>
<tbody>
<tr>
<td>Overhead: 23</td>
<td></td>
</tr>
</tbody>
</table>

| Code size | 60 |
| (in bytes) |

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).

### Arctangent 2 Implementation

**Function**  
```
ushort oflag = atan2_16 (DATA *q, DATA *i, DATA *r, ushort nx)
```
(defined in arct2.asm)

**Arguments**

<table>
<thead>
<tr>
<th>Argument</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>q[nx]</td>
<td>Pointer to quadrature input vector of size nx.</td>
</tr>
<tr>
<td>i[nx]</td>
<td>Pointer to in-phase input vector of size nx</td>
</tr>
<tr>
<td>r[nx]</td>
<td>Pointer to output data vector (in Q15 format) number representation of size nx containing. In-place processing allowed (r can be equal to x) on output, r contains the arctangent of (i/q) /π</td>
</tr>
<tr>
<td>nx</td>
<td>Number of elements of input and output vectors.</td>
</tr>
<tr>
<td>oflag</td>
<td>Overflow flag.</td>
</tr>
</tbody>
</table>

- If oflag = 1, a 32-bit overflow has occurred
- If oflag = 0, a 32-bit overflow has not occurred
**Description**  
This function calculates the arctangent of the ratio i/q, where \(-1 \leq \text{atan2}_{16}(i/q) \leq 1\) representing an actual range of \(-\pi < \text{atan2}_{16}(i/q) < \pi\). The result is placed in the resultant vector r. Output scale factor correction = \(\pi\). For example, if:

\[ \begin{align*}  
y &= [0x1999, 0x1999, 0x0, 0xe667, 0x1999] \text{ (equivalent to } [0.2, 0.2, 0, -0.2, 0.2] \text{ float)} 
x &= [0x1999, 0x3dcc, 0x7fff, 0x3dcc c234] \text{ (equivalent to } [0.2, 0.4828, 1, 0.4828, -0.4828] \text{ float)} 
\end{align*} \]

\[ \text{atan2}_{16}(y, x, r, 4) \text{ should give:} \]
\[ r = [0x2000, 0x1000, 0x0, 0xf000, 0x7000] \text{ equivalent to } [0.25, 0.125, 0, -0.125, 0.875] \times \pi \]

**Algorithm**  
\[ \text{for } (j = 0; j < nx; j + +) \quad r(j) = \text{atan2}(y[j], q[j]) \]

**Overflow Handling Methodology**  
Not applicable

**Special Requirements**  
Linker command file: you must allocate .data section (for polynomial coefficients)

**Implementation Notes**  
none

**Example**  
See examples/arct2 subdirectory

**Benchmarks**  
(preliminary)

Cycles†  
18 + 62 \times nx

Code size  
170 program; 10 data; 4 stack  
(in bytes)

† Assumptions: all data is on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).

---

**atan16**

**Arctangent Implementation**

**Function**  
ushort oflag = atan16 (DATA *x, DATA *r, ushort nx)  
(defined in atant.asm)

**Arguments**

\[ \begin{align*}  
x[nx] & \quad \text{Pointer to input data vector of size } nx. \ x \text{ contains the tangent of } r, \text{ where } |x| < 1. 
x[nx] & \quad \text{Pointer to output data vector of size } nx \text{ containing the arctangent of } x \text{ in the range } [-\pi/4, \pi/4] \text{ radians. In-place processing allowed (} r \text{ can be equal to } x) 
\end{align*} \]

\[ \text{atan}(1.0) = 0.7854 \text{ or } 6478h \]
atan16

nx Number of elements of input and output vectors.
oflag Overflow flag.
  □ If oflag = 1, a 32-bit overflow has occurred
  □ If oflag = 0, a 32-bit overflow has not occurred

Description
This function calculates the arc tangent of each of the elements of vector x. The result is placed in the resultant vector r and is in the range \([-\pi/2 to \pi/2]\) radians. For example, if \( x = [0x7fff, 0x3505, 0x1976, 0x0] \) (equivalent to \( \tan(\pi/4), \tan(\pi/8), \tan(\pi/16), 0 \) in float):
atan16(x,r,4) should give
\( r = [0x6478, 0x3243, 0x1921, 0x0] \) equivalent to \( \pi/4, \pi/8, \pi/16, 0 \)

Algorithm
for (i = 0; i < nx; i++) \( r(i) = \text{atan}(x(i)) \)

Overflow Handling Methodology Not applicable

Special Requirements Linker command file: you must allocate .data section (for polynomial coefficients)

Implementation Notes
\[ \text{atan}(x), \text{ with } 0 \leq x \leq 1, \text{ output scaling factor } = \pi. \]
\[ \text{Uses a polynomial to compute the arctan } (x) \text{ for } |x| < 1. \text{ For } |x| > 1, \text{ you can express the number } x \text{ as a ratio of } 2 \text{ fractional numbers and use the atan2_16 function.} \]

Example See examples/atant subdirectory

Benchmarks (preliminary)

<table>
<thead>
<tr>
<th>Cycles†</th>
<th>14 + 8 * nx</th>
</tr>
</thead>
<tbody>
<tr>
<td>Code size</td>
<td>43 program; 6 data</td>
</tr>
</tbody>
</table>

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).
### bexp

**Block Exponent Implementation**

**Function**

\[ \text{short } r = \text{bexp}(\text{DATA } \ast x, \text{ushort } nx) \]

(defined in bexp.asm)

**Arguments**

- **x [nx]** Pointer to input vector of size nx
- **r** Return value. Maximum exponent that may be used in scaling.
- **nx** Length of input data vector

**Description**

Computes the exponents (number of extra sign bits) of all values in the input vector and returns the minimum exponent. This will be useful in determining the maximum shift value that may be used in scaling a block of data.

**Algorithm**

Not applicable

**Overflow Handling Methodology**

Not applicable

**Special Requirements**

none

**Implementation Notes**

none

**Example**

See examples/bexp subdirectory

**Benchmarks**

(preliminary)

- **Cycles**
  - Core: 3 * nx
  - Overhead: 4

- **Code size**
  - 19 (in bytes)
cbrev

**Complex Bit Reverse**

**Function**

```c
void cbrev (DATA *, DATA *, ushort)
(defined in cbrev.asm)
```

**Arguments**

<table>
<thead>
<tr>
<th>Argument</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>x[2*nx]</td>
<td>Pointer to complex input vector x.</td>
</tr>
<tr>
<td>r[2*nx]</td>
<td>Pointer to complex output vector r.</td>
</tr>
<tr>
<td>nx</td>
<td>Number of complex elements of vectors x and r.</td>
</tr>
</tbody>
</table>

- To bit-reverse the input of a complex FFT, nx should be the complex FFT size.
- To bit-reverse the input of a real FFT, nx should be half the real FFT size.

**Description**

This function bit-reverses the position of elements in complex vector x into output vector r. In-place bit-reversing is allowed. Use this function in conjunction with FFT routines to provide the correct format for the FFT input or output data. If you bit-reverse a linear-order array, you obtain a bit-reversed order array. If you bit-reverse a bit-reversed order array, you obtain a linear-order array.

**Algorithm**

Not applicable

**Overflow Handling Methodology**

Not applicable

**Special Requirements**

- Input vector x[ ] and output vector r[ ] must be aligned on 32-bit boundary.
  (2 LSBs of byte address must be zero)

- Ensure that the entire array fits within a 64K boundary (the largest possible array addressable by the 16-bit auxiliary register).

**Implementation Notes**

- In place bit-reversal has better performance.

**Example**

See examples/cfft and examples/rfft subdirectories
cbrev32

32-Bit Complex Bit Reverse

Function
void cbrev32(LDATA *, LDATA *r, ushort)
(defined in cbrev32.asm)

Arguments
x[2*nx] Pointer to complex input vector x.
r[2*x] Pointer to complex output vector r.
(nx Number of complex elements in vector x.

- To bit-reverse the output of a complex (i)FFT, nx should be the complex (i)FFT size.
- To bit-reverse the output of a real (i)FFT, nx should be half the real (i)FFT size.

Description
This function bit-reverses the position of elements in complex vector x into output vector r. In-place bit-reversing is allowed. Use this function in conjunction with (i)FFT routines to provide the correct format for the (i)FFT input or output data. If you bit-reverse a linear-order array, you obtain a bit-reversed order array. If you bit-reverse a bit-reversed order array, you obtain a linear-order array.

Algorithm
Not applicable

Benchmarks
(preliminary)

<table>
<thead>
<tr>
<th>FFT Size</th>
<th>Cycles†</th>
</tr>
</thead>
<tbody>
<tr>
<td>8</td>
<td>107</td>
</tr>
<tr>
<td>16</td>
<td>128</td>
</tr>
<tr>
<td>32</td>
<td>150</td>
</tr>
<tr>
<td>64</td>
<td>222</td>
</tr>
<tr>
<td>128</td>
<td>310</td>
</tr>
<tr>
<td>256</td>
<td>554</td>
</tr>
<tr>
<td>512</td>
<td>918</td>
</tr>
<tr>
<td>1024</td>
<td>1794</td>
</tr>
</tbody>
</table>

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).
Overflow Handling Methodology

Not applicable

Special Requirements

- In-place bit-reversal has better performance.
- Ensure that the entire array fits within a 64K boundary (the largest possible array addressable by the 16-bit auxiliary register).

Implementation Notes

\( x \) is read in normal linear addressing and \( r \) is written with bit-reversed addressing.

Example

See example/c(i)fft subdirectory

Benchmarks

Cycles

\begin{align*}
\text{Core:} & \\
5^*nx & \text{ (off-place)} \\
11^*nx & \text{ (in-place)} \\
\end{align*}

\[ \text{Code size} \quad 75 \text{ (includes support for both in-place and off-place} \]

\[ \text{(in bytes)} \quad \text{bit-reverse)} \]

\[ \dagger \text{ Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).} \]

\section*{cfft}

\textbf{Forward Complex FFT}

Function

void cfft (DATA *x, ushort nx, type);

(defined in cfft.asm)

Arguments

\begin{itemize}
\item \( x \) [2*nx] \quad \text{Pointer to input vector containing nx complex elements (2*nx real elements) in normal order. On output, vector contains the nx complex elements of the FFT(x) in bit-reversed order. Complex numbers are stored in interleaved Re-Im format.}
\item \( nx \) \quad \text{Number of complex elements in vector x. Must be between 8 and 1024.}
\item \( \text{type} \) \quad \text{FFT type selector. Types supported:}
\begin{itemize}
\item If type = SCALE, scaled version selected
\item If type = NOSCALE, non-scaled version selected
\end{itemize}
\end{itemize}

Description

Computes a complex nx-point FFT on vector \( x \), which is in normal order. The original content of vector \( x \) is destroyed in the process. The nx complex elements of the result are stored in vector \( x \) in bit-reversed order. The twiddle table is in bit-reversed order.
Algorithm  

\[ y[k] = \frac{1}{(\text{scale factor})} \sum_{i=0}^{n-1} x[i] \left( \cos\left(\frac{-2\pi ik}{nx}\right) + j \sin\left(\frac{-2\pi ik}{nx}\right) \right) \]

Overflow Handling Methodology  
If type = SCALE is selected, scaling before each stage is implemented for overflow prevention.

Special Requirements

- The twiddle table must be located in internal memory since it is accessed by the C55x coefficient bus.
- Input data section is aligned on 32-bit boundary.
- For the best performance:
  - Input data in DARAM block
  - Twiddle table in SARAM block or DARAM block different than the DARAM clock that contains the input data.
- Ensure that the entire input array fits within a 64K boundary (the largest possible array addressable by the 16-bit auxiliary register).
- If the twiddle table and the data buffer are in the same block then the radix-2 kernel is 7 cycles and the radix-4 kernel is not affected.

Implementation Notes

- The implementations are optimized for MIPS, not for code size. They implement the decimation-in-time (DIT) FFT algorithm.
- The NOSCALE version is implemented using radix-2 butterflies. The first two stages are replaced by a single radix-4 stage.
- The SCALE version is implemented using only radix-2 stages. This routine prevents overflow by scaling by 2 before each FFT stage.

Example

See examples/cfft subdirectory

Benchmarks

- 5 cycles (radix-2 butterfly – used in both SCALE and NOSCALE versions)
- 10 cycles (radix-4 butterfly – used in the first 2 stages of a non-scaled version)
Comparing the results to MATLAB:

- **NOSCALE version**

![Diagram showing comparison between C55 DSPLIB and MATLAB cfft with NOSCALE](image)

The MATLAB cfft results need to be multiplied by the cfft size, N, in order to be compared to the C55 DSPLIB cfft results.

- **SCALE version**

![Diagram showing comparison between C55 DSPLIB and MATLAB cfft with SCALE](image)

The C55 DSPLIB cfft results can be compared to the unmodified MATLAB cfft results.

**CFFT – SCALE**

<table>
<thead>
<tr>
<th>FFT Size</th>
<th>Cycles†</th>
<th>Code Size (in bytes)</th>
</tr>
</thead>
<tbody>
<tr>
<td>8</td>
<td>208</td>
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<td>493</td>
</tr>
<tr>
<td>1024</td>
<td>25954</td>
<td>493</td>
</tr>
</tbody>
</table>

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).
Function Descriptions

### 32-Bit Forward Complex FFT

**Function**

```c
void cfft32 (LDATA *x, ushort nx, type);
```

**Arguments**

- `x[2*nx]` Pointer to input vector containing `nx` complex elements (2×`nx` real elements) in normal-order. On output, vector x contains the `nx` complex elements of the FFT(x) in bit-reversed order. Complex numbers are stored in the interleaved Re-Im format.

- `nx` Number of complex elements in vector x. Must be between 8 and 1024.

- `type` FFT type selector. Types supported:
  - If `type` = SCALE, scaled version selected
  - If `type` = NOSCALE, non-scaled version selected

**Description**

Computes a complex `nx`-point FFT on vector `x`, which is in normal order. The original content of vector `x` is destroyed in the process. The `nx` complex elements of the result are stored in vector `x` in bit-reversed order.

**Algorithm**

(DFT)

\[
y[k] = \frac{1}{(\text{scale factor})} \sum_{i=0}^{nx-1} x[i] \cdot \left( \cos\left(\frac{2\pi i k}{nx}\right) - j \sin\left(\frac{2\pi i k}{nx}\right) \right)
\]
Overflow Handling Methodology  If scale==1, scaling before each stage is implemented for overflow prevention.

Special Requirements
- The twiddle table must be located in the internal memory since it is accessed by the C55x coefficient bus.
- Ensure that the entire array fits within a 64K boundary (the largest possible array addressable by the 16-bit auxiliary register).
- For best performance, the data buffer has to be in a DARAM block.
- For best performance, the coefficient buffer can be in SARAM block or a DARAM different from the DARAM block that contains the data buffer.

Implementation Notes
- Radix-2 DIT version of the FFT algorithm is implemented. The implementation is optimized for MIPS, not for code size.

Example
See example/cfft32 subdirectory

Benchmarks
- 12 cycles for radix-2 butterfly in non-scaled version; 15 cycles for radix-2 butterfly in scaled version
- 21 cycles for radix-4 butterfly in non-scaled version
- 10 cycles for stage 1 loop in scaled version; 10 cycles for group 1 of stage 2 loop in scaled version; 13 cycles for group 2 of stage 2 in scaled version

CFFT32 – SCALE

<table>
<thead>
<tr>
<th>FFT Size</th>
<th>Cycles†</th>
<th>Code Size (in bytes)</th>
</tr>
</thead>
<tbody>
<tr>
<td>16</td>
<td>715</td>
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<td>504</td>
</tr>
<tr>
<td>512</td>
<td>48960</td>
<td>504</td>
</tr>
</tbody>
</table>

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).
Complex FIR Filter

Function

`ushort oflag = cfir (DATA *x, DATA *h, DATA *r, DATA *dbuffer, ushort nx, ushort nh)`

Arguments

- `x[2*nx]` Pointer to input vector of nx complex elements.
- `h[2*nh]` Pointer to complex coefficient vector of size nh in normal order. For example, if nh=6, then `h[nh] = {h0r, h0i, h1r, h1i, h2r, h2i, h3r, h3i, h4r, h4i, h5r, h5i}` where h0 resides at the lowest memory address in the array.
  - This array must be located in internal memory since it is accessed by the C55x coefficient bus.
- `r[2*nx]` Pointer to output vector of nx complex elements. In-place computation (r = x) is allowed.

---

**CFFT – NOSCALE**

<table>
<thead>
<tr>
<th>FFT Size</th>
<th>Cycles†</th>
<th>Code Size (in bytes)</th>
</tr>
</thead>
<tbody>
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<td>16</td>
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<td>337</td>
</tr>
<tr>
<td>512</td>
<td>42161</td>
<td>337</td>
</tr>
</tbody>
</table>

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).
dbuffer[2*nh + 2] Pointer to delay buffer of length 2 * nh + 2

- In the case of multiple-buffering schemes, this array should be initialized to 0 for the first filter block only. Between consecutive blocks, the delay buffer preserves the previous r output elements needed.
- The first element in this array is present for alignment purposes, the second element is special in that it contains the array index−1 of the oldest input entry in the delay buffer. This is needed for multiple-buffering schemes, and should be initialized to 0 (like all the other array entries) for the first block only.

nx Number of complex input samples

nh The number of complex coefficients of the filter. For example, if the filter coefficients are {h0, h1, h2, h3, h4, h5}, then nh = 6. Must be a minimum value of 3. For smaller filters, zero pad the coefficients to meet the minimum value.

oflag Overflow error flag (returned value)

- If oflag = 1, a 32-bit data overflow has occurred in an intermediate or final result.
- If oflag = 0, a 32-bit overflow has not occurred.

**Description**

Computes a complex FIR filter (direct-form) using the coefficients stored in vector h. The complex input data is stored in vector x. The filter output result is stored in vector r. This function maintains the array dbuffer containing the previous delayed input values to allow consecutive processing of input data blocks. This function can be used for both block-by-block (nx ≥ 2) and sample-by-sample filtering (nx = 1). In-place computation (r = x) is allowed.

**Algorithm**

\[ r[j] = \sum_{k=0}^{nh-1} h[k] x[j-k] \quad 0 \leq j \leq nx \]

**Overflow Handling Methodology**

No scaling implemented for overflow prevention.

**Special Requirements**

- nh must be a minimum value of 3. For smaller filters, zero pad the h[ ] array.
- Coefficient array h[ ] is located in the internal memory.
- Input array x[ ] must be aligned on a 32-bit boundary (2 LSBs of byte address must be zero).
Delay buffer dbuffer[ ] must be aligned on a 32-bit boundary (2 LSBs of byte address must be zero).

**Implementation Notes** The first element in the dbuffer array is present only for alignment purposes. The second element in this array (index=0) is the entry index for the input history. It is treated as an unsigned 16-bit value by the function even though it has been declared as signed in C. The value of the entry index is equal to the index – 1 of the oldest input entry in the array. The remaining elements make up the input history. Figure 4–1 shows the array in memory with an entry index of 2. The newest entry in the dbuffer is denoted by x(j−0), which in this case would occupy index = 3 in the array. The next newest entry is x(j−1), and so on. It is assumed that all x() entries were placed into the array by the previous invocation of the function in a multiple-buffering scheme.

Figure 4–1, Figure 4–2, and Figure 4–3 show the dbuffer, x, and r arrays as they appear in memory.
Figure 4–1. *dbuf* Array in Memory at Time $j$

- dnbuffer Array in Memory at Time $j$

- oldest x( ) entry

- newest x( ) entry

- dummy value
  - entry index = 2
  - $x(r(j-nh-2))$
  - $x(i(j-nh-2))$
  - $x(r(j-nh-1))$
  - $x(i(j-nh-1))$
  - $x(r(j-nh))$
  - $x(i(j-nh))$
  - $x(r(j-0))$
  - $x(i(j-0))$
  - $x(r(j-1))$
  - $x(i(j-1))$
  - $x(r(j-2))$
  - $x(i(j-2))$

- ...

- ...

- $x(r(j-nh-3))$
  - $x(i(j-nh-3))$
  - $x(r(j-nh-4))$
  - $x(i(j-nh-4))$
  - $x(r(j-nh-3))$
  - $x(i(j-nh-3))$

- highest memory address

- lowest memory address
Figure 4–2. $x$ Array in Memory

- Oldest $x()$ entry: $xr(0)$, $xi(0)$, $xr(1)$, $xi(1)$
- Newest $x()$ entry: $xr(nx-1)$, $xi(nx-1)$

Figure 4–3. $r$ Array in Memory

- Oldest $x()$ entry: $rr(0)$, $ri(0)$, $rr(1)$, $ri(1)$
- Newest $x()$ entry: $rr(nx-2)$, $ri(nx-2)$, $rr(nx-1)$, $ri(nx-1)$

Example

See examples/cfir subdirectory

Benchmarks (preliminary)

**Cycles**: Core: $nx \times [8 + 2(nh-2)]$
Overhead: 51

**Code size** (in bytes): 136

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).
cifft

Inverse Complex FFT

Function

void cifft (DATA *x, ushort nx, type);
(defined in cifft.asm)

Arguments

x [2*nx] Pointer to input vector containing nx complex elements (2*nx real elements) in normal order. On output, vector contains the nx complex elements of the IFFT(x) in bit-reversed order. Complex numbers are stored in interleaved Re-Im format.

nx Number of complex elements in vector x. Must be between 8 and 1024.

type FFT type selector. Types supported:
- If type = SCALE, scaled version selected
- If type = NOSCALE, non-scaled version selected

Description

Computes a complex nx-point IFFT on vector x, which is in normal order. The original content of vector x is destroyed in the process. The nx complex elements of the result are stored in vector x in bit-reversed order.

Algorithm

(IDFT)

\[ y[k] = \frac{1}{(scale \ factor)} \sum_{i=0}^{nx-1} x[i] \left( \cos\left(\frac{2^*\pi^*i^*k}{nx}\right) + j \sin\left(\frac{2^*\pi^*i^*k}{nx}\right) \right) \]

Overflow Handling Methodology

If type = SCALE is selected, scaling before each stage is implemented for overflow prevention

Special Requirements

- The twiddle table must be located in internal memory since it is accessed by the C55x coefficient bus.
- Input data section is aligned on 32-bit boundary.
- For the best performance:
  - Input data in DARAM block.
  - Twiddle table in SARAM block or DARAM block different than the DARAM clock that contains the input data.
- Ensure that the entire array fits within a 64K boundary (the largest possible array addressable by the 16-bit auxiliary register).
- If the twiddle table and the data buffer are in the same block then the radix-2 kernel is 7 cycles and the radix-4 kernel is not affected.
Implementation Notes

- The implementations are optimized for MIPS, not for code size. They implement the decimation-in-time (DIT) FFT algorithm.
- The NOSCALE version is implemented using radix-2 butterflies. The first two stages are replaced by a single radix-4 stage.
- The SCALE version is implemented using only radix-2 stages. This routine prevents overflow by scaling by 2 before each FFT stage.

Example

See examples/cifft subdirectory

Benchmarks

(preliminary)

- 5 cycles (radix-2 butterfly – used in both SCALE and NOSCALE versions)
- 10 cycles (radix-4 butterfly – used in NOSCALE version)

CIFFT – SCALE

<table>
<thead>
<tr>
<th>FFT Size</th>
<th>Cycles(^\d)</th>
<th>Code Size (in bytes)</th>
</tr>
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<tbody>
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<td>8</td>
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<tr>
<td>16</td>
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<td>494</td>
</tr>
<tr>
<td>1024</td>
<td>25954</td>
<td>494</td>
</tr>
</tbody>
</table>

\(^\d\) Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).
**cifft32**

### 32-Bit Inverse Complex FFT

#### Function

```c
void cifft32 (LDATA *x, ushort nx, type);
```

#### Arguments

- **x[2*nx]**: Pointer to input vector containing nx complex elements (2*nx real elements) in normal-order. On output, vector `x` contains the nx complex elements of the iFFT(x) in bit-reversed order. Complex numbers are stored in the interleaved Re-Im format.

- **nx**: Number of complex elements in vector `x`. Must be between 8 and 1024.

- **type**: FFT type selector. Types supported:
  - If `type = SCALE`, scaled version selected
  - If `type = NOSCALE`, non-scaled version selected

#### Description

Computes a complex nx-point iFFT on vector `x`, which is in normal-order. The original content of vector `x` is destroyed in the process. The nx complex elements of the result are stored in vector `x` in bit-reversed order.

#### Algorithm

(iDFT)

\[
y[k] = \frac{1}{(\text{scale factor})} \sum_{i=0}^{n-1} x[i] \left( \cos\left(\frac{2 \pi i k}{nx}\right) + j \sin\left(\frac{2 \pi i k}{nx}\right) \right)
\]
Overflow Handling Methodology  If scale == 1, scaling before each stage is implemented for overflow prevention.

Special Requirements

☒ The twiddle table must be located in the internal memory since it is accessed by the C55x coefficient bus.

☒ Ensure that the entire array fits within a 64K boundary (the largest possible array addressable by the 16-bit auxiliary register).

☒ For best performance, the data buffer has to be in a DARAM block.

☒ For best performance, the coefficient buffer can be in an SARAM block or a DARAM different from the DARAM block that contains the data buffer.

Implementation Notes

☒ Radix-2 DIT version of the iFFT algorithm is implemented. The implementation is optimized for MIPS, not for code size.

Example

See example/cifft32 subdirectory

Benchmarks

☒ 12 cycles for radix-2 butterfly in non-scaled version; 15 cycles for radix-2 butterfly in scaled version

☒ 21 cycles for radix-4 butterfly in non-scaled version

☒ 10 cycles for stage 1 loop in scaled version; 10 cycles for group 1 of stage 2 loop in scaled version; 13 cycles for group 2 of stage 2 in scaled version

CIFFT32 – SCALE

<table>
<thead>
<tr>
<th>iFFT Size</th>
<th>Cycles†</th>
<th>Code Size (in bytes)</th>
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<td>504</td>
</tr>
<tr>
<td>512</td>
<td>48960</td>
<td>504</td>
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</tbody>
</table>

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).
<table>
<thead>
<tr>
<th>iFFT Size</th>
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</table>

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).
convol  

Convolution

Function

```c
ushort oflag = convol (DATA *x, DATA *h, DATA *r, ushort nr, ushort nh)
```

Arguments

- `x[nr+nh−1]` Pointer to input vector of `nr + nh − 1` real elements.
- `h[nh]` Pointer to input vector of `nh` real elements.
- `r[nr]` Pointer to output vector of `nr` real elements.
- `nr` Number of elements in vector `r`. In-place computation (`r = x`) is allowed (see Description section for comment).
- `nh` Number of elements in vector `h`.
- `oflag` Overflow error flag (returned value)
  - If `oflag = 1`, a 32-bit data overflow occurred in an intermediate or final result.
  - If `oflag = 0`, a 32-bit overflow has not occurred.

Description

Computes the real convolution of two real vectors `x` and `h`, and places the results in vector `r`. Typically used for block FIR filter computation when there is no need to retain an input delay buffer. This function can also be used to implement single-sample FIR filters (`nr = 1`) provided the input delay history for the filter is maintained external to this function. In-place computation (`r = x`) is allowed, but be aware that the `r` output vector is shorter in length than the `x` input vector; therefore, `r` will only overwrite the first `nr` elements of the `x`.

Algorithm

\[
   r[j] = \sum_{k=0}^{nh-1} h[k] x[j - k] \quad 0 \leq j \leq nr
\]

Overflow Handling Methodology

No scaling implemented for overflow prevention.

Special Requirements

none

Implementation Notes

Figure 4–4, Figure 4–5, and Figure 4–6 show the `x`, `r`, and `h` arrays as they appear in memory.
**Example**
See examples/convol subdirectory

**Benchmarks** (preliminary)

<table>
<thead>
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<th>Metric</th>
<th>Value</th>
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<td>Cycles†</td>
<td>nr * (1 + nh)</td>
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<tr>
<td>Overhead</td>
<td>44</td>
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<td>Code size (in bytes)</td>
<td>88</td>
</tr>
</tbody>
</table>

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).
Function

`ushort oflag = convol1 (DATA *x, DATA *h, DATA *r, ushort nr, ushort nh)`

Arguments

- `x[nr+nh−1]` Pointer to input vector of `nr+nh−1` real elements.
- `h[nh]` Pointer to input vector of `nh` real elements.
- `r[nr]` Pointer to output vector of `nr` real elements. In-place computation (`r = x`) is allowed (see Description section for comment).
- `nr` Number of elements in vector `r`. Must be an even number.
- `nh` Number of elements in vector `h`.
- `oflag` Overflow error flag (returned value)
  - If `oflag = 1`, a 32-bit data overflow occurred in an intermediate or final result.
  - If `oflag = 0`, a 32-bit overflow has not occurred.

Description

Computes the real convolution of two real vectors `x` and `h`, and places the results in vector `r`. This function utilizes the dual-MAC capability of the C55x to process in parallel two output samples for each iteration of the inner function loop. It is, therefore, roughly twice as fast as `CONVOL`, which implements only a single-MAC approach. However, the number of output samples (`nr`) must be even. Typically used for block FIR filter computation when there is no need to retain an input delay buffer. This function can also be used to implement single-sample FIR filters (`nr = 1`) provided the input delay history for the filter is maintained external to this function. In-place computation (`r = x`) is allowed, but be aware that the `r` output vector is shorter in length than the `x` input vector; therefore, `r` will only overwrite the first `nr` elements of the `x`.

Algorithm

\[ r[j] = \sum_{k=0}^{nh-1} h[k] \times[j - k] \quad 0 \leq j \leq nr \]

Overflow Handling Methodology

No scaling implemented for overflow prevention.

Special Requirements

- `nr` must be an even value.
- The vector `h[nh]` must be located in internal memory since it is accessed using the C55x coefficient bus, and that bus does not have access to external memory.

Implementation Notes

Figure 4–7, Figure 4–8, and Figure 4–9 show the `x`, `r`, and `h` arrays as they appear in memory.
**Example**  
See examples/convol1 subdirectory

**Benchmarks**  
(preliminary)

- **Cycles**: $\frac{nr}{2} \times [3+(nh-2)]$
  - Core: $58$
  - Overhead: $58$
- **Code size**: 101

$^\dagger$ Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).
Convol2

Convolution (fastest)

Function

```c
ushort oflag = convol2 (DATA *x, DATA *h, DATA *r, ushort nr, ushort nh)
```

Arguments

- `x[nr+nh−1]` Pointer to input vector of `nr + nh − 1` real elements.
- `h[nh]` Pointer to input vector of `nh` real elements.
- `r[nr]` Pointer to output vector of `nr` real elements. In-place computation (`r = x`) is allowed (see Description section for comment). This array must be aligned on a 32-bit boundary in memory.
- `nr` Number of elements in vector `r`. Must be an even number.
- `nh` Number of elements in vector `h`.
- `oflag` Overflow error flag (returned value)
  - If `oflag = 1`, a 32-bit data overflow has occurred in an intermediate or final result.
  - If `oflag = 0`, a 32-bit overflow has not occurred.

Description

Computes the real convolution of two real vectors `x` and `h`, and places the results in vector `r`. This function utilizes the dual-MAC capability of the C55x to process in parallel two output samples for each iteration of the inner function loop. It is, therefore, roughly twice as fast as CONVOL, which implements only a single-MAC approach. However, the number of output samples (`nr`) must be even. In addition, this function offers a small performance improvement over CONVOL1 at the expense of requiring the `r` array to be 32-bit aligned in memory. Typically used for block FIR filter computation when there is no need to retain an input delay buffer. This function can also be used to implement single-sample FIR filters (`nr = 1`) provided the input delay history for the filter is maintained external to this function. In-place computation (`r = x`) is allowed, but be aware that the `r` output vector is shorter in length than the `x` input vector; therefore, `r` will only overwrite the first `nr` elements of the `x`.

Algorithm

\[ r[j] = \sum_{k=0}^{nh-1} h[k] x[j - k] \quad 0 \leq j \leq nr \]

Overflow Handling Methodology

No scaling implemented for overflow prevention.
Special Requirements

- nr must be an even value.
- The vector h[nh] must be located in internal memory since it is accessed using the C55x coefficient bus, and that bus does not have access to external memory.
- The vector r[nr] must be 32-bit aligned in memory.

Implementation Notes Figure 4–10, Figure 4–11, and Figure 4–12 show the x, r, and h arrays as they appear in memory.

**Figure 4–10. x Array in Memory**

<table>
<thead>
<tr>
<th>x(0)</th>
<th>lowest memory address</th>
</tr>
</thead>
<tbody>
<tr>
<td>x(1)</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
</tr>
<tr>
<td>x(nr+nh–2)</td>
<td></td>
</tr>
<tr>
<td>x(nr+nh–1)</td>
<td>highest memory address</td>
</tr>
</tbody>
</table>

**Figure 4–11. r Array in Memory**

<table>
<thead>
<tr>
<th>r(0)</th>
<th>lowest memory address</th>
</tr>
</thead>
<tbody>
<tr>
<td>r(1)</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
</tr>
<tr>
<td>r(nr–2)</td>
<td></td>
</tr>
<tr>
<td>r(nr–1)</td>
<td>highest memory address</td>
</tr>
</tbody>
</table>

**Figure 4–12. h Array in Memory**

<table>
<thead>
<tr>
<th>h(0)</th>
<th>lowest memory address</th>
</tr>
</thead>
<tbody>
<tr>
<td>h(1)</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
</tr>
<tr>
<td>h(nh–2)</td>
<td></td>
</tr>
<tr>
<td>h(nh–1)</td>
<td>highest memory address</td>
</tr>
</tbody>
</table>
**corr**

**Function**

```c
ushort oflag = corr (DATA *x, DATA *y, DATA *r, ushort nx, ushort ny, type)
```

**Arguments**

- `x [nx]` Pointer to real input vector of `nx` real elements.
- `y [ny]` Pointer to real input vector of `ny` real elements.
- `r[nx+ny-1]` Pointer to real output vector containing the full-length correlation (`nx + ny - 1` elements) of vector `x` with `y`. `r` must be different than both `x` and `y` (in-place computation is not allowed).
- `nx` Number of real elements in vector `x`
- `ny` Number of real elements in vector `y`
- `type` Correlation type selector. Types supported:
  - `raw` if `type = raw`, `r` contains the raw correlation
  - `bias` if `type = bias`, `r` contains the biased-correlation
  - `unbias` if `type = unbias`, `r` contains the unbiased-correlation
- `oflag` Overflow flag
  - `1` if `oflag = 1`, a 32-bit overflow has occurred
  - `0` if `oflag = 0`, a 32-bit overflow has not occurred

**Description**

Computes the full-length correlation of vectors `x` and `y` and stores the result in vector `r` using time-domain techniques.

---

**Example**

See examples/convol2 subdirectory

**Benchmarks**

(preliminary)

$\text{Cycles}^\dagger \quad \text{Core: } nr/2 \ast (1 + nh) \\
\quad \text{Overhead: } 24$

<table>
<thead>
<tr>
<th>Code size</th>
<th>100</th>
</tr>
</thead>
</table>

$^\dagger$ Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).
### Algorithm

**Raw correlation**

\[
r[j] = \sum_{k=0}^{nr-1} x[j + k] \cdot y[k] \quad 0 \leq j \leq nr = nx + ny - 1
\]

**Biased correlation**

\[
r[j] = \frac{1}{nr} \sum_{k=0}^{nr-1} x[j + k] \cdot y[k] \quad 0 \leq j \leq nr = nx + ny - 1
\]

**Unbiased correlation**

\[
r[j] = \frac{1}{(nx - \text{abs}(j))} \sum_{k=0}^{nr-1} x[j + k] \cdot y[k] \quad 0 \leq j \leq nr = nx + ny - 1
\]

### Overflow Handling Methodology

No scaling implemented for overflow prevention

### Special Requirements

- x array located in the internal memory because it is accessed by the C55 coefficient bus.
- Requirements for nx, ny
  - \( nx \geq y \)
  - \( ny \geq nx \)

### Implementation Notes

- Special debugging consideration: This function is implemented as a macro that invokes different correlation routines according to the type selected. As a consequence the `corr` symbol is not defined. Instead the `corr_raw`, `corr_bias`, `corr_unbias` symbols are defined.
- Correlation is implemented using time-domain techniques

### Benchmarks

(Preliminary)

<table>
<thead>
<tr>
<th>Cycles</th>
<th>Raw: 2 times faster than C54x</th>
<th>Unbias: 2.14 times faster than C54x</th>
<th>Bias: 2.1 times faster than C54x</th>
</tr>
</thead>
</table>
Adaptive Delayed LMS Filter

**Function**

```c
ushort oflag = dlms (DATA *x, DATA *h, DATA *r, DATA *des, DATA *dbuffer, DATA step, ushort nh, ushort nx)
```
(defined in dlms.asm)

**Arguments**

- `x[nx]` Pointer to input vector of size `nx`
- `h[nh]` Pointer to filter coefficient vector of size `nh`.  
  - `h` is stored in reversed order: `h(n-1), ... h(0)` where `h[n]` is at the lowest memory address.
  - Memory alignment: `h` is a circular buffer and must start in a `k`-bit boundary (that is, the `k` LSBs of the starting address must be zeros) where `k = log2(nh)`
- `r[nx]` Pointer to output data vector of size `nx`. `r` can be equal to `x`.
- `des[nx]` Pointer to expected output array
- `dbuf[r+nh+2]` Pointer to the delay buffer structure.  
  The delay buffer is a structure comprised of an index register and a circular buffer of length `nh + 1`. The index register is the index into the circular buffer of the oldest data sample.
- `nh` Number of filter coefficients. Filter order = `nh - 1`.
  - `nh` ≥ 3
- `nx` Length of input and output data vectors
- `oflag` Overflow flag. 
  - If `oflag = 1`, a 32-bit overflow has occurred
  - If `oflag = 0`, a 32-bit overflow has not occurred

**Description**

Adaptive delayed least-mean-square (LMS) FIR filter using coefficients stored in vector `h`. Coefficients are updated after each sample based on the LMS algorithm and using a constant step = 2*μ. The real data input is stored in vector `dbuf`. The filter output result is stored in vector `r`.

LMS algorithm uses the previous error and the previous sample (delayed) to take advantage of the C55x LMS instruction.
The delay buffer used is the same delay buffer used for other functions in the C55x DSP Library. There is one more data location in the circular delay buffer than there are coefficients. Other C55x DSP Library functions use this delay buffer to accommodate use of the dual-MAC architecture. In the DLMS function, we make use of the additional delay slot to allow coefficient updating as well as FIR calculation without a need to update the circular buffer in the interim operations.

The FIR output calculation is based on \( x(i) \) through \( x(i-\text{nh}+1) \). The coefficient update for a delayed LMS is based on \( x(i-1) \) through \( x(i-\text{nh}) \). Therefore, by having a delay buffer of \( \text{nh}+1 \), we can perform all calculations with the given delay buffer containing delay values of \( x(i) \) through \( x(i-\text{nh}) \). If the delay buffer was of length \( \text{nh} \), the oldest data sample, \( x(i-\text{nh}) \), would need to be updated with the newest data sample, \( x(i) \), sometime after the calculation of the first coefficient update term, but before the calculation of the last FIR term.

**Algorithm**

FIR portion

\[
    r[j] = \sum_{k=0}^{\text{nh}-1} h[k] \ast x[i - k] \quad 0 \leq i \leq \text{nx} - 1
\]

Adaptation using the previous error and the previous sample:

\[
    e(i) = \text{des}(i - 1) - r(i - 1)
    h_x(i + 1) = h_x(i) + 2 \ast \mu \ast e(i - 1) \ast x(i - k - 1)
\]

**Overflow Handling Methodology**  No scaling implemented for overflow prevention.

**Special Requirements**  Minimum of 2 input and desired data samples. Minimum of 2 coefficients

**Implementation Notes**

- Delayed version implemented to take advantage of the C55x LMS instruction.

- Effect of using delayed error signal on convergence minimum:
  
  For reference, the following is the algorithm for the regular LMS (non-delayed):

  FIR portion

  \[
  r[j] = \sum_{k=0}^{\text{nh}-1} h[k] \ast x[i - k] \quad 0 \leq i \leq \text{nx} - 1
  \]

  Adaptation using the current error and the current sample:

  \[
  e(i) = \text{des}(i) - r(i)
  h_x(i + 1) = h_x(i) + 2 \ast \mu \ast e(i) \ast x(i - k)
  \]
dlmsfast

**Example**

See examples/dlms subdirectory

**Benchmarks**

(preliminary)

<table>
<thead>
<tr>
<th>Cycles†</th>
<th>Core: nx * (7 + 2*(nh − 1)) = nx * (5 + 2 * nh)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Overhead:</td>
<td>26</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Code size</th>
<th>122</th>
</tr>
</thead>
<tbody>
<tr>
<td>(in bytes)</td>
<td></td>
</tr>
</tbody>
</table>

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).

**dlmsfast**

**Adaptive Delayed LMS Filter (fast implemented)**

**Function**

`ushort oflag = dlmsfast (DATA *x, DATA *h, DATA *r, DATA *des, DATA *dbuffer, DATA step, ushort nh, ushort nx)`

This function is implemented for better performance on large number of filter orders.

(defined in dlmsfast.asm)

**Arguments**

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>x[nx]</td>
<td>Pointer to input vector of size nx.</td>
</tr>
<tr>
<td>h[2*nh]</td>
<td>Pointer to filter coefficient array of size 2*nh. This array contains two coefficient buffers h_coef and h_scratch. The updated coefficients in different time slot are stored into these two buffers alternatively. The final updated coefficients are stored in h_coef.</td>
</tr>
<tr>
<td></td>
<td></td>
</tr>
<tr>
<td>h_coef is stored in reversed order: h_coef(n−1), ..., h_coef(0) where h_coef(n−1) is at the lowest memory address of the first half of array h.</td>
<td></td>
</tr>
<tr>
<td>h_scratch is stored in reversed order: h_scratch(n−1), ..., h_scratch(0) where h_scratch(n−1) is at the lowest memory address of the second half of array h.</td>
<td></td>
</tr>
<tr>
<td>Memory alignment: h must be aligned in 32 bytes boundary.</td>
<td></td>
</tr>
<tr>
<td>r[nx]</td>
<td>Pointer to output data vector of size nx. r can be equal to x.</td>
</tr>
<tr>
<td>des[nx]</td>
<td>Pointer to expected output array.</td>
</tr>
</tbody>
</table>
dlmsfast

dbuffer[nh+3]  Pointer to the delay buffer structure.

- The delay buffer is a structure comprised of an index register and a circular buffer of length nh+2. The index register is the index into the circular buffer of the oldest data sample.
- Memory alignment: dbuffer must be aligned in 32 bytes boundary.

nh  Number of filter coefficients. Filter order = nh−1. nh has to be a even number. nh ≥ 10.

nx  Length of input and output data vectors. nx has to be a even number.

oflag  Overflow flag.

- If oflag = 1, a 32-bit overflow has occurred
- If oflag = 0, a 32-bit overflow has not occurred

Description

Adaptive delayed least-mean-square (LMS) FIR filter using coefficients stored in vector h. Coefficients are updated after each sample based on the LMS algorithm and using a constant step = 2*μ. The real data input is stored in vector dbuffer. The filter output result is stored in vector r.

Unlike the DLMS function in DSPLIB, which uses C55x LMS instruction to do partial filtering and addition of delta h to the coefficient, this fast LMS algorithm is implemented by doing coefficient updating and filtering separately to get better cycle count.

In this implementation, two input data are processed as a pair. The filtering operation uses dual-MAC to process two time slots of data and two set of coefficients are updated corresponding to these two time slots.

The delay buffer used is the same delay buffer used for other functions in the C55x DSP Library. There is two more data location in the circular delay buffer than there are coefficients. Other C55x DSP Library functions use this delay buffer to accommodate use of the dual-MAC architecture. In the DLMS function, we make use of the additional delay slots to allow coefficient updating as well as FIR calculation without a need to update the circular buffer in the interim operations.
The first time slot of FIR output calculation is based on $x(i)$ through $x(i-nh+1)$. While the coefficient update for a delayed LMS is based on $x(i-1)$ through $x(i-nh)$. The second time slot of FIR output is based on $x(i+1)$ through $x(i-nh+2)$. While the coefficient update for the delayed LMS is based on $x(i)$ through $x(i-nh+1)$. Therefore, by having a delay buffer of $nh+2$, we can perform all calculations with the given delay buffer containing delay values of $x(i)$ through $x(i-nh+1)$.

**Algorithm**

FIR portion:

$$r[i] = \sum_{k=0}^{nh-1} h[k] \cdot x[i - k] \quad 0 \leq i \leq nx - 1$$

Adaptation using the previous error and the previous sample:

$$e(i) = des(i - 1) - r(i - 1)$$

$$h_k(i + 1) = h_k(i) + 2 \cdot \mu \cdot e(i - 1) \cdot x(i - k - 1)$$

**Overflow Handling Methodology**

No scaling implemented for overflow prevention.

**Special Requirements**

- Delay buffer array dbugger[ ] must be located in the internal memory.
- Minimum of 10 coefficients. Coefficient buffer need to be aligned on 32-bit boundary (2 LSBs of byte address must be zero).
- dbuffer need to be aligned on 32 bytes memory boundary.
- Coefficient buffer and dbuffer need to be put into different block of memory for the best performance.

**Implementation Notes**

Filtering and coefficient updating are implemented separately. Figure 4–13, Figure 4–14, and Figure 4–15 show the x buffer, dbuffer, and h buffers.

**Figure 4–13. x Buffer**

- **oldest x() entry** → $x(0)$
- **x(1)**
- **...**
- **x(nx-2)**
- **highest memory address**
- **newest x() entry** → $x(nx-1)$
Figure 4-14. dbuffer

<table>
<thead>
<tr>
<th>entry index = 0</th>
<th>lowest memory address</th>
</tr>
</thead>
<tbody>
<tr>
<td>x(0)</td>
<td></td>
</tr>
<tr>
<td>x(1)</td>
<td></td>
</tr>
<tr>
<td>x(-(nh+1))</td>
<td></td>
</tr>
<tr>
<td>x(-nh)</td>
<td></td>
</tr>
</tbody>
</table>

newest x( ) entry
oldest x( ) entry

Figure 4-15. h Buffers

<table>
<thead>
<tr>
<th>h_coefs</th>
<th>lowest memory address</th>
</tr>
</thead>
<tbody>
<tr>
<td>h_coef(nh-1)</td>
<td></td>
</tr>
<tr>
<td>h_coef(nh-2)</td>
<td></td>
</tr>
</tbody>
</table>

h_scratch

<table>
<thead>
<tr>
<th>h_scratch</th>
<th>highest memory address</th>
</tr>
</thead>
<tbody>
<tr>
<td>h_scratch(nh-1)</td>
<td></td>
</tr>
<tr>
<td>h_scratch(nh-2)</td>
<td></td>
</tr>
</tbody>
</table>

Example
See examples/dlmsfast subdirectory

Effect of using delayed error signal on convergence minimum. For reference, the following is the algorithm for the regular LMS (non-delayed):

FIR portion

\[
r[i] = \sum_{k=0}^{nh-1} h[k] * x[i - k] \quad 0 \leq i \leq nx - 1
\]

Adaptation using the current error and the current sample

\[
e(i) = des(i) - r(i)
\]

\[
h_s(i + 1) = h_s(i) + 2 * \mu * e(i) * x(i - k)
\]
Benchmarks

<table>
<thead>
<tr>
<th>Cycles†</th>
<th>Core: nx/2 * (26 + 3*nh)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Overhead:</td>
<td>71</td>
</tr>
</tbody>
</table>

| Code size | 322 (in bytes) |

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).

---

**expn**

**Exponential Base e**

**Function**

ushort oflag = expn (DATA *x, DATA *r, ushort nx)

(defined in expn.asm)

**Arguments**

- **x[nx]** Pointer to input vector of size nx. x contains the numbers normalized between (-1,1) in q15 format
- **r[nx]** Pointer to output data vector (Q3.12 format) of size nx. r can be equal to x.
- **nx** Length of input and output data vectors
- **oflag** Overflow flag.
  - □ If oflag = 1, a 32-bit overflow has occurred
  - □ If oflag = 0, a 32-bit overflow has not occurred

**Description**

Computes the exponent of elements of vector x using Taylor series.

**Algorithm**

for \( i = 0; i < nx; i + + \) \( y(i) = e^{x(i)} \) where \(-1 < x(i) < 1\)

**Overflow Handling Methodology**

Not applicable

**Special Requirements**

Linker command file: you must allocate .data section (for polynomial coefficients) on a 32-bit boundary (2 LSBs of byte address must be zero).
**Implementation Notes** Computes the exponent of elements of vector x. It uses the following Taylor series:

\[ \exp(x) = c_0 + (c_1 \times x) + (c_2 \times x^2) + (c_3 \times x^3) + (c_4 \times x^4) + (c_5 \times x^5) \]

where

- \( c_0 = 1.0000 \)
- \( c_1 = 1.0001 \)
- \( c_2 = 0.4990 \)
- \( c_3 = 0.1705 \)
- \( c_4 = 0.0348 \)
- \( c_5 = 0.0139 \)

**Example** See examples/expn subdirectory

**Benchmarks** (preliminary)

<table>
<thead>
<tr>
<th>Cycles†</th>
<th>Core: 11 * nx</th>
</tr>
</thead>
<tbody>
<tr>
<td>Overhead:</td>
<td>18</td>
</tr>
</tbody>
</table>

| Code size | 57 |
| (in bytes) | |

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).

---

**FIR Filter**

**Function**

\[ \text{ushort oflag} = \text{fir}(\text{DATA} \times x, \text{DATA} \times h, \text{DATA} \times r, \text{DATA} \times dbuffer, \text{ushort} \ nx, \text{ushort} \ nh) \]

**Arguments**

- \( x[\text{nx}] \) Pointer to input vector of \( nx \) real elements.
- \( h[\text{nh}] \) Pointer to coefficient vector of size \( nh \) in normal order. For example, if \( nh=6 \), then \( h[\text{nh}] = \{h_0, h_1, h_2, h_3, h_4, h_5\} \) where \( h_0 \) resides at the lowest memory address in the array.
- \( r[\text{nx}] \) Pointer to output vector of \( nx \) real elements. In-place computation \( (r = x) \) is allowed.
dbuffer[nh+2]  Pointer to delay buffer of length nh = nh + 2

- In the case of multiple-buffering schemes, this array should be initialized to 0 for the first filter block only. Between consecutive blocks, the delay buffer preserves the previous elements needed.
- The first element in this array is special in that it contains the array index−1 of the oldest input entry in the delay buffer. This is needed for multiple-buffering schemes, and should be initialized to 0 (like all the other array entries) for the first block only.

nx  Number of input samples

nh  The number of coefficients of the filter. For example, if the filter coefficients are \{h0, h1, h2, h3, h4, h5\}, then nh = 6. Must be a minimum value of 3. For smaller filters, zero pad the coefficients to meet the minimum value.

oflag  Overflow error flag (returned value)

- If oflag = 1, a 32-bit data overflow occurred in an intermediate or final result.
- If oflag = 0, a 32-bit overflow has not occurred.

Description  Computes a real FIR filter (direct-form) using the coefficients stored in vector h. The real input data is stored in vector x. The filter output result is stored in vector r. This function maintains the array dbuffer containing the previous delayed input values to allow consecutive processing of input data blocks. This function can be used for both block-by-block (nx ≥ 2) and sample-by-sample filtering (nx = 1). In place computation (r = x) is allowed.

Algorithm  
\[
r[j] = \sum_{k=0}^{nh-1} h[k] x[j - k] \quad 0 \leq j \leq nx
\]

Overflow Handling Methodology  No scaling implemented for overflow prevention.

Special Requirements  nh must be a minimum value of 3. For smaller filters, zero pad the h[] array.
Implementation Notes  The first element in the dbuffer array (index = 0) is the entry index for the input history. It is treated as an unsigned 16-bit value by the function even though it has been declared as signed in C. The value of the entry index is equal to the index − 1 of the oldest input entry in the array. The remaining elements make up the input history. Figure 4–16 shows the array in memory with an entry index of 2. The newest entry in the dbuffer is denoted by x(j−0), which in this case would occupy index = 3 in the array. The next newest entry is x(j−1), and so on. It is assumed that all x() entries were placed into the array by the previous invocation of the function in a multiple-buffering scheme.

The dbuffer array actually contains one more history value than is needed to implement this filter. The value x(j–nh) does not enter into the calculations for for the output r(j). However, this value is required in other DSPLIB filter functions that utilize the dual-MAC units on the C55x, such as FIR2. Including this extra location ensures compatibility across all filter functions in the C55x DSPLIB.

Figure 4–16, Figure 4–17, and Figure 4–18 show the dbuffer, x, and r arrays as they appear in memory.

Figure 4–16. dbuffer Array in Memory at Time j

<table>
<thead>
<tr>
<th>entry index = 2</th>
</tr>
</thead>
<tbody>
<tr>
<td>x(j–nh–2)</td>
</tr>
<tr>
<td>x(j–nh–1)</td>
</tr>
<tr>
<td>x(j–nh–1)</td>
</tr>
<tr>
<td>x(j–nh)</td>
</tr>
<tr>
<td>x(j–0)</td>
</tr>
<tr>
<td>x(j–1)</td>
</tr>
<tr>
<td>x(j–2)</td>
</tr>
<tr>
<td>x(j–nh–4)</td>
</tr>
<tr>
<td>x(j–nh–3)</td>
</tr>
</tbody>
</table>

oldest x( ) entry

newest x( ) entry

lowest memory address

highest memory address
Function Descriptions

Figure 4–17. x Array in Memory

- Oldest x(0) entry
- Middle entries
- Newest x(nx-2) entry

- Lowest memory address

Figure 4–18. r Array in Memory

- Oldest r(0) entry
- Middle entries
- Newest r(nx-2) entry

- Lowest memory address

Example
See examples/fir subdirectory

Benchmarks
(preliminary)

- Cycles†
  - Core: nx * (2 + nh)
  - Overhead: 25

- Code size 107
  - (in bytes)

† Assumes all data is in on-chip dual-access RAM (provided linker command file reflects those conditions).

FIR2 Filter

Function
ushort oflag = fir (DATA *x, DATA *h, DATA *r, DATA *dbuf, ushort nx, ushort nh)

Arguments
- x[nx] Pointer to input vector of nx real elements.
- h[nh] Pointer to coefficient vector of size nh in normal order. For example, if nh=6, then h[nh] = {h0, h1, h2, h3, h4, h5} where h0 resides at the lowest memory address in the array.
r[nx]  Pointer to output vector of nx real elements. In-place computation (r = x) is allowed.

dbuffer[nh+2]  Pointer to delay buffer of length nh = nh + 2

- In the case of multiple-buffering schemes, this array should be initialized to 0 for the first filter block only. Between consecutive blocks, the delay buffer preserves the previous elements needed.
- The first element in this array is special in that it contains the array index−1 of the oldest input entry in the delay buffer. This is needed for multiple-buffering schemes, and should be initialized to 0 (like all the other array entries) for the first block only.

nx  Number of input samples

nh  The number of coefficients of the filter. For example, if the filter coefficients are \{h0, h1, h2, h3, h4, h5\}, then nh = 6. Must be a minimum value of 3. For smaller filters, zero pad the coefficients to meet the minimum value.

oflag  Overflow error flag (returned value)

- If oflag = 1, a 32-bit data overflow occurred in an intermediate or final result.
- If oflag = 0, a 32-bit overflow has not occurred.

Description
Computes a real FIR filter (direct-form) using the coefficients stored in vector h. The real input data is stored in vector x. The filter output result is stored in vector r. This function maintains the array dbuffer containing the previous delayed input values to allow consecutive processing of input data blocks. This function can be used for both block-by-block (nx ≥ 2) and sample-by-sample filtering (nx = 1). In place computation (r = x) is allowed.

Algorithm
\[
r[j] = \sum_{k=0}^{nh-1} h[k] x[j-k] \quad 0 \leq j \leq nx
\]

Overflow Handling Methodology  No scaling implemented for overflow prevention.

Special Requirements
- nh must be a minimum value of 3. For smaller filters, zero pad the h[ ] array.
- array r[ ] must be aligned on 32-bit boundary.
- array h[ ] must be located in internal memory because it is accessed with the coefficient data pointer, CDP.
**Implementation Notes** The first element in the dbuffer array (index = 0) is the entry index for the input history. It is treated as an unsigned 16-bit value by the function even though it has been declared as signed in C. The value of the entry index is equal to the index − 1 of the oldest input entry in the array. The remaining elements make up the input history. Figure 4–16 shows the array in memory with an entry index of 2. The newest entry in the dbuffer is denoted by $x(j-0)$, which in this case would occupy index = 3 in the array. The next newest entry is $x(j-1)$, and so on. Every iteration two entries are updated in the dbuffer array. It is assumed that all $x()$ entries were placed into the array by the previous invocation of the function in a multiple-buffering scheme.

Figure 4–16, Figure 4–17, and Figure 4–18 show the dbuffer, x, and r arrays as they appear in memory.

**Figure 4–19. dbuffer Array in Memory at Time j**

```
entry index = 2
x(j-nh-2)
x(j-nh-1)
x(j-nh-1)
x(j-nh)
x(j-0)
x(j-1)
x(j-2)
```

oldest $x()$ entry

newest $x()$ entry

```
x(j-nh-5)
x(j-nh-4)
x(j-nh-3)
```

highest memory address

**Figure 4–20. x Array in Memory**

```
x(0)
x(1)
```

oldest $x()$ entry

```
x(nx-2)
x(nx-1)
```

newest $x()$ entry

lowest memory address

highest memory address
**Figure 4–21. r Array in Memory**

<p>| | | | | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
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<tbody>
<tr>
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</tbody>
</table>

<p>| | | | | | |</p>
<table>
<thead>
<tr>
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<td></td>
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<td></td>
<td></td>
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<td></td>
</tr>
</tbody>
</table>

**Exmaple**
See examples/fir2 subdirectory

**Benchmarks**
(preliminary)

<table>
<thead>
<tr>
<th>Cycles†</th>
<th>Core:</th>
<th>Overhead:</th>
</tr>
</thead>
<tbody>
<tr>
<td>nx * (3 + nh/2)</td>
<td>25</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Code size (in bytes)</th>
</tr>
</thead>
<tbody>
<tr>
<td>107</td>
</tr>
</tbody>
</table>

† Assumes all data is in on-chip dual-access RAM (provided linker command file reflects those conditions).

---

**firdec**

*Decimating FIR Filter*

**Function**

```c
ushort oflag = firdec (DATA *x, DATA *h, DATA *r, DATA *dbuffer , ushort nh, ushort nx, ushort D)
```

(defined in decimate.asm)

**Arguments**

- `x [nx]` Pointer to real input vector of nx real elements.
- `h[nh]` Pointer to coefficient vector of size nh in normal order: $H = b0 \ b1 \ b2 \ b3 \ ...$
- `r[nx/D]` Pointer to real input vector of nx/D real elements. In-place computation ($r = x$) is allowed.
- `dbuffer[nh+1]` Delay buffer

- In the case of multiple-buffering schemes, this array should be initialized to 0 for the first block only. Between consecutive blocks, the delay buffer preserves previous delayed input samples. It also preserves a ptr to the next new entry into the dbuffer. This ptr is preserved across function calls in dbuffer[0].
nx Number of real elements in vector x
nh Number of coefficients
D Decimation factor. For example a D = 2 means you drop every other sample. Ideally, nx should be a multiple of D. If not, the trailing samples will be lost in the process.
oflag Overflow error flag
- If oflag = 1, a 32-bit data overflow occurred in an intermediate or final result.
- If oflag = 0, a 32-bit overflow has not occurred.

Description Computes a decimating real FIR filter (direct-form) using coefficient stored in vector h. The real data input is stored in vector x. The filter output result is stored in vector r. This function retains the address of the delay filter memory d containing the previous delayed values to allow consecutive processing of blocks. This function can be used for both block-by-block and sample-by-sample filtering (nx = 1).

Algorithm \[ r[j] = \sum_{k=0}^{nh} h[k] x[j*D - k] \quad 0 \leq j \leq nx \]

Overflow Handling Methodology No scaling implemented for overflow prevention.

Special Requirements none

Implementation Notes none

Example See examples/decim subdirectory

Benchmarks (preliminary)

<table>
<thead>
<tr>
<th>Category</th>
<th>Formula</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cycles Core</td>
<td>((nx/D)\times(10+nh+(D-1)))</td>
<td></td>
</tr>
<tr>
<td>Overhead</td>
<td>67</td>
<td></td>
</tr>
<tr>
<td>Code size (in bytes)</td>
<td>144</td>
<td></td>
</tr>
</tbody>
</table>
**firinterp**

*Interpolating FIR Filter*

**Function**

```c
ushort oflag = firinterp (DATA *x, DATA *h, DATA *r, DATA *dbuffer , ushort nh,
ushort nx, ushort I)
```

(defined in interp.asm)

**Arguments**

- **x [nx]** Pointer to real input vector of nx real elements.
- **h[nh]** Pointer to coefficient vector of size nh in normal order:
  \[ H = b_0 \ b_1 \ b_2 \ b_3 \ldots \]
- **r[nx*I]** Pointer to real output vector of nx real elements.
  In-place computation \((r = x)\) is allowed
- **dbuffer[(nh/I)+1]** Delay buffer of \((nh/I)+1\) elements
  - In the case of multiple-buffering schemes, this array should be initialized to 0 for the first block only. Between consecutive blocks, the delay buffer preserves delayed input samples in `dbuffer[1\ldots(nh/I)+1]`. It also preserves a ptr to the next new entry into the `dbuffer`. This ptr is preserved across function calls in `dbuffer[0]`.
  - The delay buffer is only `nh/I` elements and holds only delayed `x` inputs. No zero-samples are inserted into `dbuffer` (since only non-zero products contribute to the filter output)
- **nx** Number of real elements in vector `x` and `r`
- **nh** Number of coefficients, with \((nh/I) \geq 3\)
- **I** Interpolation factor. `I` is effectively the number of output samples for every input sample. This routine can be used with `I=1`.
- **oflag** Overflow error flag
  - If `oflag = 1`, a 32-bit data overflow occurred in an intermediate or final result.
  - If `oflag = 0`, a 32-bit overflow has not occurred.
Description
Computes an interpolating real FIR filter (direct-form) using coefficient stored in vector h. The real data input is stored in vector x. The filter output result is stored in vector r. This function retains the address of the delay filter memory d containing the previous delayed values to allow consecutive processing of blocks. This function can be used for both block-by-block and sample-by-sample filtering (nx = 1).

Algorithm
\[ r[t] = \sum_{k=0}^{nh} h[k]x\left[\frac{t}{i - k}\right], \quad 0 \leq j \leq nr \]

Overflow Handling Methodology
No scaling implemented for overflow prevention.

Special Requirements
nh has to be a multiple of I, such nh/I ≥ 3.

Implementation Notes
none

Example
See examples/decimate subdirectory

Benchmarks
(preliminary)

<table>
<thead>
<tr>
<th>Cycles</th>
<th>Core:</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>If I &gt; 1</td>
</tr>
<tr>
<td></td>
<td>nx*(2+I*(1+(nh/I)))</td>
</tr>
<tr>
<td></td>
<td>If I=1:</td>
</tr>
<tr>
<td></td>
<td>nx*(2+nh)</td>
</tr>
</tbody>
</table>

Overhead 72

<table>
<thead>
<tr>
<th>Code size</th>
<th>164</th>
</tr>
</thead>
<tbody>
<tr>
<td>(in bytes)</td>
<td></td>
</tr>
</tbody>
</table>
**firlat**

**Lattice Forward (FIR) Filter**

**Function**

```c
ushort oflag = firlat (DATA *x, DATA *h, DATA *r, DATA *pbuffer, int nx, int nh)
```

**Arguments**

- **x [nx]** Pointer to real input vector of nx real elements in normal order:
  - `x[0]`
  - `x[1]`
  - ...
  - `x[nx-2]`
  - `x[nx-1]`

- **h[nh]** Pointer to lattice coefficient vector of size nh in normal order:
  - `h[0]`
  - `h[1]`
  - ...
  - `h[nh-2]`
  - `h[nh-1]`

- **r[nx]** Pointer to output vector of nx real elements. In-place computation (r = x) is allowed.
  - `r[0]`
  - `r[1]`
  - ...
  - `r[nx-2]`
  - `r[nx-1]`
pbuffer [nh]  Delay buffer

- In the case of multiple-buffering schemes, this array should be initialized to 0 for the first block only. Between consecutive blocks, the delay buffer preserves the previous r output elements needed.
- pbuffer: procession buffer of nh length in order:
  \[ e'[0][n-1] \]
  \[ e'[1][n-1] \]
  \[ \ldots \]
  \[ e'[nh-2][n-1] \]
  \[ e'[nh-1][n-1] \]

nx  Number of real elements in vector x (input samples)

nh  Number of coefficients

oflag  Overflow error flag

- If oflag = 1, a 32-bit data overflow has occurred in an intermediate or final result
- If oflag = 0, a 32-bit overflow has not occurred.

**Description**
Computes a real lattice FIR filter implementation using coefficient stored in vector h. The real data input is stored in vector x. The filter output result is stored in vector r. This function retains the address of the delay filter memory containing the previous delayed values to allow consecutive processing of blocks. This function can be used for both block-by-block and sample-by-sample filtering (nx=1)

**Algorithm**
\[
e_0[n] = e'[0][n] = x[n],
\]
\[
e_i[n] = e_{i-1}[n] - h e'_{i-1}[n - 1], \quad i = 1, 2, \ldots, N
\]
\[
e'[n] = h e_{i-1}[n] + e'_{i-1}[n - 1], \quad i = 1, 2, \ldots, N
\]
\[
y[n] = e_0[n]
\]

**Overflow Handling Methodology**  No scaling implemented for overflow prevention.

**Special Requirements**  none

**Implementation Notes**  none

**Example**
See examples/firlat subdirectory
Benchmarks

(preliminary)

Cycles†
Core: \(nx[4 + 4(nh - 1)]\)
Overhead: 23

Code size 53
(in bytes)

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).

**firs**

*Symmetric FIR Filter*

**Function**

`ushort oflag = firs (DATA *x, DATA *h, DATA *r, DATA *dbuffer, ushort nx, ushort nh2)`

**Arguments**

- `x[nx]` Pointer to input vector of \(nx\) real elements.
- `r[nx]` Pointer to output vector of \(nx\) real elements. In-place computation \((r = x)\) is allowed.
- `h[nh2]` Pointer to coefficient vector containing the first half of the symmetric filter coefficients. For example, if the filter coefficients are \(\{h_0, h_1, h_2, h_2, h_1, h_0\}\), then \(h[nh2] = \{h_0, h_1, h_2\}\) where \(h_0\) resides at the lowest memory address in the array.
  - This array must be located in internal memory since it is accessed by the C55x coefficient bus.
- `dbuffer[2*nh2 + 2]` Pointer to delay buffer of length \(nh = 2*nh2 + 2\)
  - In the case of multiple-buffering schemes, this array should be initialized to 0 for the first filter block only. Between consecutive blocks, the delay buffer preserves the previous \(r\) output elements needed.
  - The first element in this array is special in that it contains the array index of the oldest input entry in the delay buffer. This is needed for multiple-buffering schemes, and should be initialized to 0 (like all the other array entries) for the first block only.
- `nx` Number of input samples
nh2 Half the number of coefficients of the filter (due to symmetry there is no need to provide the other half). For example, if the filter coefficients are \{h0, h1, h2, h2, h1, h0\}, then nh2 = 3. Must be a minimum value of 3. For smaller filters, zero pad the coefficients to meet the minimum value.

oflag Overflow error flag (returned value)
- If oflag = 1, a 32-bit data overflow occurred in an intermediate or final result.
- If oflag = 0, a 32-bit overflow has not occurred.

Description Computes a real FIR filter (direct-form) with nh2 symmetric coefficients using the FIRS instruction approach. The filter is assumed to have a symmetric impulse response, with the first half of the filter coefficients stored in the array h. The real input data is stored in vector x. The filter output result is stored in vector r. This function maintains the array dbuffer containing the previous delayed input values to allow consecutive processing of input data blocks. This function can be used for both block-by-block (nx \geq 2) and sample-by-sample filtering (nx = 1). In-place computation (r = x) is allowed.

Algorithm  
\[ r[j] = \sum_{k=0}^{nh2-1} h[k] \times (x[j - k] + x[j + k - 2 * nh2 + 1]) \quad 0 \leq j \leq nx \]

Overflow Handling Methodology No scaling implemented for overflow prevention.

Special Requirements
- nh must be a minimum value of 3. For smaller filters, zero pad the h[] array.
- Coefficient array h[nh2] must be located in internal memory since it is accessed using the C55x coefficient bus, and that bus does not have access to external memory.

Implementation Notes The first element in the dbuffer array (index = 0) is the entry index for the input history. It is treated as an unsigned 16-bit value by the function even though it has been declared as signed in C. The value of the entry index is equal to the index – 1 of the oldest input entry in the array. The remaining elements make up the input history. Figure 4–22 shows the array in memory with an entry index of 2. The newest entry in the dbuffer is denoted by x(j−0), which in this case would occupy index = 3 in the array. The next newest entry is x(j−1), and so on. It is assumed that all x() entries were placed into the array by the previous invocation of the function in a multiple-buffering scheme.
The dbuffer array actually contains one more history value than is needed to implement this filter. The value $x(j-2\times nh2)$ does not enter into the calculations for the output $r(j)$. However, this value is required in other DSPLIB filter functions that utilize the dual-MAC units on the C55x, such as FIR2. Including this extra location ensures compatibility across all filter functions in the C55x DSPLIB.

Figure 4–22, Figure 4–23, and Figure 4–24 show the dbuffer, x, and r arrays as they appear in memory.

**Figure 4–22. dbuffer Array in Memory at Time $j$**

```
<table>
<thead>
<tr>
<th>entry index = 2</th>
<th>lowest memory address</th>
</tr>
</thead>
<tbody>
<tr>
<td>$x(j-2\times nh2-2)$</td>
<td></td>
</tr>
<tr>
<td>$x(j-2\times nh2-1)$</td>
<td></td>
</tr>
<tr>
<td>$x(j-2\times nh2)$</td>
<td></td>
</tr>
<tr>
<td>$x(j-0)$</td>
<td></td>
</tr>
<tr>
<td>$x(j-1)$</td>
<td></td>
</tr>
<tr>
<td>$x(j-2)$</td>
<td></td>
</tr>
</tbody>
</table>
```

oldest x( ) entry →
newest x( ) entry →

```
<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>$x(j-2\times nh2-5)$</td>
<td>highest memory address</td>
</tr>
<tr>
<td>$x(j-2\times nh2-4)$</td>
<td></td>
</tr>
<tr>
<td>$x(j-2\times nh2-3)$</td>
<td></td>
</tr>
</tbody>
</table>
```

**Figure 4–23. x Array in Memory**

```
<table>
<thead>
<tr>
<th></th>
<th>lowest memory address</th>
</tr>
</thead>
<tbody>
<tr>
<td>$x(0)$</td>
<td></td>
</tr>
<tr>
<td>$x(1)$</td>
<td></td>
</tr>
</tbody>
</table>
```

oldest x( ) entry →
newest x( ) entry →

```
<table>
<thead>
<tr>
<th></th>
<th>highest memory address</th>
</tr>
</thead>
<tbody>
<tr>
<td>$x(nx-2)$</td>
<td></td>
</tr>
<tr>
<td>$x(nx-1)$</td>
<td></td>
</tr>
</tbody>
</table>
```

Function Descriptions

**fltoq15**

**Floating-point to Q15 Conversion**

**Function**

`ushort errorcode = fltoq15(float *x, DATA *r, ushort nx)`  
(defined in fltoq15.asm)

**Arguments**

- `x[nx]` Pointer to floating-point input vector of size `nx`. `x` should contain the numbers normalized between `(-1,1)`. The `errorcode` returned value will reflect if that condition is not met.
- `r[nx]` Pointer to output data vector of size `nx` containing the q15 equivalent of vector `x`.
- `nx` Length of input and output data vectors
- `errorcode` The function returns the following error codes:
  - 1 – if any element is too large to represent in Q15 format
  - 2 – if any element is too small to represent in Q15 format
  - 3 – both conditions 1 and 2 were encountered

**Example**

See examples/firs subdirectory

**Benchmarks**

(preliminary)

- Cycles†: `nx[5 + (nh–2)]`
- Overhead: 72
- Code size: 133 bytes

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).

---

**Figure 4–24. r Array in Memory**

![Array in Memory Diagram]

- **oldest x() entry**  
  - `r(0)`  
  - `r(1)`

- **newest x() entry**  
  - `r(nx–2)`  
  - `r(nx–1)`

- **lowest memory address**

- **highest memory address**
**hilb16**

**Description**
Convert the IEEE floating-point numbers stored in vector x into Q15 numbers stored in vector r. The function returns the error codes if any element x[i] is not representable in Q15 format.

All values that exceed the size limit will be saturated to a Q15 1 or -1 depending on sign (0x7fff if value is positive, 0x8000 if value is negative). All values too small to be correctly represented will be truncated to 0.

**Algorithm**
Not applicable

**Overflow Handling Methodology**
Saturation implemented for overflow handling

**Special Requirements**
none

**Implementation Notes**
none

**Example**
See examples/expn subdirectory

**Benchmarks**
(accurate)

<table>
<thead>
<tr>
<th>Cycles†</th>
<th>Core:</th>
</tr>
</thead>
<tbody>
<tr>
<td>17 * nx (if x[n] ==0)</td>
<td>17 * nx (if x[n] is too small for Q15 representation)</td>
</tr>
<tr>
<td>23 * nx (if x[n] is too large for Q15 representation)</td>
<td>32 * nx (if x[n] is too large for Q15 representation)</td>
</tr>
<tr>
<td>38 * nx (otherwise)</td>
<td></td>
</tr>
</tbody>
</table>

**Overhead:** 23

**Code size** (in bytes)
157

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).

**FIR Hilbert Transformer**

**Function**
ushort oflag = hilb16 (DATA *x, DATA *h, DATA *r, DATA *dbuffer, ushort nx, ushort nh)

**Arguments**

<table>
<thead>
<tr>
<th>x[nx]</th>
<th>Pointer to input vector of nx real elements.</th>
</tr>
</thead>
<tbody>
<tr>
<td>h[nh]</td>
<td>Pointer to coefficient vector of size nh in normal order. H={h0, h1, h2, h3, h4, …} Every odd valued filter coefficient has to 0, i.e. h1 = h3 = … = 0. And H = {h0, 0, h2, 0, h4, 0, …} where h0 resides at the lowest memory address in the array.</td>
</tr>
</tbody>
</table>
hilb16

**Description**
Computes a real FIR filter (direct-form) using the coefficients stored in vector h. The real input data is stored in vector x. The filter output result is stored in vector r. This function maintains the array dbuffer containing the previous delayed input values to allow consecutive processing of input data blocks. This function can be used for both block-by-block (nx >= 2) and sample-by-sample filtering (nx = 1). In place computation (r = x) is allowed.

**Algorithm**
\[ r[j] = \sum_{k=0}^{nh-1} h[k]x[j-k] \quad 0 \leq j \leq nx \]

**Overflow Handling Methodology**
No scaling implemented for overflow prevention.
Special Requirements

- Every odd valued filter coefficient has to be 0. This is a requirement for the Hilbert transformer. For example, a 6 tap filter may look like this: \( H = [0.867 \ 0 \ -0.324 \ 0 \ -0.002 \ 0] \)

- Always pad 0 to make \( nh \) as a even number. For example, a 5 tap filter with a zero pad may look like this: \( H = [0.867 \ 0 \ -0.324 \ 0 \ -0.002 \ 0] \)

- \( nh \) must be a minimum value of 6. For smaller filters, zero pad the \( H[] \) array.

Implementation Notes

The first element in the dbuffer array (index = 0) is the entry index for the input history. It is treated as an unsigned 16-bit value by the function even though it has been declared as signed in C. The value of the entry index is equal to the index – 1 of the oldest input entry in the array. The remaining elements make up the input history. Figure 4–25 shows the array in memory with an entry index of 2. The newest entry in the dbuffer is denoted by \( x(j-0) \), which in this case would occupy index = 3 in the array. The next newest entry is \( x(j-1) \), and so on. It is assumed that all \( x() \) entries were placed into the array by the previous invocation of the function in a multiple-buffering scheme.

The dbuffer array actually contains one more history value than is needed to implement this filter. The value \( x(j-nh) \) does not enter into the calculations for the output \( r(j) \). However, this value is required in other DSPLIB filter functions that utilize the dual-MAC units on the C55x, such as FIR2. Including this extra location ensures compatibility across all filter functions in the C55x DSPLIB.

Figure 4–25, Figure 4–26, and Figure 4–27 show the dbuffer, \( x \), and \( r \) arrays as they appear in memory.

*Figure 4–25. dbuffer Array in Memory at Time \( j \)*

<table>
<thead>
<tr>
<th>entry index = 2</th>
<th>lowest memory address</th>
</tr>
</thead>
<tbody>
<tr>
<td>( x(j-nh-2) )</td>
<td></td>
</tr>
<tr>
<td>( x(j-nh-1) )</td>
<td></td>
</tr>
<tr>
<td>( x(j-nh) )</td>
<td></td>
</tr>
<tr>
<td>( x(j-0) )</td>
<td></td>
</tr>
<tr>
<td>( x(j-1) )</td>
<td></td>
</tr>
<tr>
<td>( x(j-2) )</td>
<td></td>
</tr>
</tbody>
</table>

oldest \( x() \) entry

newest \( x() \) entry

\( x(j-nh-5) \)

\( x(j-nh-4) \)

\( x(j-nh-3) \)

highest memory address
**Figure 4–26. x Array in Memory**

oldest x( ) entry →  

<table>
<thead>
<tr>
<th></th>
<th>x(0)</th>
<th></th>
<th></th>
<th>x(1)</th>
<th></th>
<th></th>
<th></th>
<th>lowest memory address</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
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</table>

newest x( ) entry →  

<table>
<thead>
<tr>
<th></th>
<th>x(nx−2)</th>
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**Figure 4–27. r Array in Memory**

oldest x( ) entry →  

<table>
<thead>
<tr>
<th></th>
<th>r(0)</th>
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<th>r(1)</th>
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<th>lowest memory address</th>
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</tbody>
</table>

newest x( ) entry →  

<table>
<thead>
<tr>
<th></th>
<th>r(nx−2)</th>
<th></th>
<th></th>
<th>r(nx−1)</th>
<th></th>
<th></th>
<th></th>
<th>highest memory address</th>
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</table>

**Example**  
See examples/hilb16 subdirectory

**Benchmarks**  
(preliminary)

<table>
<thead>
<tr>
<th>Cycles</th>
<th>Core: nx*(2+nh/2)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Overhead:</td>
<td>28</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Code size</th>
<th>108</th>
</tr>
</thead>
</table>
**Function**

```c
ushort oflag = iir32 (DATA *x, LDATA *h, DATA *r, LDATA *dbuffer, ushort nbiq, ushort nr)
(defined in iir32.asm)
```

**Arguments**

<table>
<thead>
<tr>
<th>Argument</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>x [nr]</td>
<td>Pointer to input data vector of size nr</td>
</tr>
<tr>
<td>h[5*nbiq]</td>
<td>Pointer to the 32-bit filter coefficient vector with the following format. For example for nbiq = 2, h is equal to:</td>
</tr>
<tr>
<td></td>
<td>beginning of biquad 1</td>
</tr>
<tr>
<td></td>
<td>b21 – high</td>
</tr>
<tr>
<td></td>
<td>b21 – low</td>
</tr>
<tr>
<td></td>
<td>b11 – high</td>
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<td></td>
<td>b11 – low</td>
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<tr>
<td></td>
<td>b01 – high</td>
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<tr>
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<td>b01 – low</td>
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<tr>
<td></td>
<td>a21 – high</td>
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<td>a21 – low</td>
</tr>
<tr>
<td></td>
<td>a11 – high</td>
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<tr>
<td></td>
<td>a11 – low</td>
</tr>
<tr>
<td></td>
<td>beginning of biquad 2 coefs</td>
</tr>
<tr>
<td></td>
<td>b22 – high</td>
</tr>
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<td>b22 – low</td>
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<td>b12 – high</td>
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<td>b12 – low</td>
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<td></td>
<td>b02 – high</td>
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<td></td>
<td>b02 – low</td>
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<td></td>
<td>a22 – high</td>
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<td>a22 – low</td>
</tr>
<tr>
<td></td>
<td>a12 – high</td>
</tr>
<tr>
<td></td>
<td>a12 – low</td>
</tr>
<tr>
<td>r[nr]</td>
<td>Pointer to output data vector of size nr. r can be equal or less than x.</td>
</tr>
</tbody>
</table>
dbuffer[2*nbiq+2]  Pointer to address of 32-bit delay line dbuffer. Each biquad has 3 consecutive delay line elements. For example for nbiq = 2:

\[
\begin{align*}
&\text{d1(n−2)} – \text{low} & \text{beginning of biquad 1} \\
&\text{d1(n−2)} – \text{high} \\
&\text{d1(n−1)} – \text{low} \\
&\text{d1(n−1)} – \text{high} \\
&\text{d2(n−2)} – \text{low} & \text{beginning of biquad 2} \\
&\text{d2(n−2)} – \text{high} \\
&\text{d2(n−1)} – \text{low} \\
&\text{d2(n−1)} – \text{high}
\end{align*}
\]

- In the case of multiple-buffering schemes, this array should be initialized to 0 for the first block only. Between consecutive blocks, the delay buffer preserves the previous elements needed.

- Memory alignment: none required for C5510. This is a group of circular buffers. Each biquad’s delay buffer is treated separately. The Buffer Start Address (BSAxx) updated to a new location for each biquad.

\[
lbiq \quad \text{Number of biquads} \\
r \quad \text{Number of elements of input and output vectors} \\
oflag \quad \text{Overflow flag.}
\]

- If oflag = 1, a 32-bit overflow has occurred
- If oflag = 0, a 32-bit overflow has not occurred

**Description**

Computes a cascaded IIR filter of nbiquad biquad sections using 32-bit coefficients and 32-bit delay buffers. The input data is assumed to be single-precision (16 bits).

Each biquad section is implemented using Direct-form II. All biquad coefficients (5 per biquad) are stored in vector h. The real data input is stored in vector x. The filter output result is stored in vector r .

This function retains the address of the delay filter memory d containing the previous delayed values to allow consecutive processing of blocks. This function is more efficient for block-by-block filter implementation due to the C-calling overhead. However, it can be used for sample-by-sample filtering (nx = 1).
iircas4

Algorithm  (for biquad)
\[ d(n) = x(n) - a1 \times d(n - 1) - a2 \times d(n - 2) \]
\[ y(n) = b0 \times d(n) + b1 \times d(n - 1) + b2 \times d(n - 2) \]

Overflow Handling Methodology  No scaling implemented for overflow prevention.

Special Requirements  none

Implementation Notes  See program iircas32.asm

Example  See examples/iir32 subdirectory

Benchmarks  (preliminary)
\[ \text{Cycles} \quad \text{Core: } n_x(7 + 31 \times \text{nbiq}) \]
\[ \text{Overhead: } 77 \]
\[ \text{Code size} \quad 203 \]
\[ \text{in bytes} \]

iircas4  Cascaded IIR Direct Form II Using 4 Coefficients per Biquad

Function  ushort oflag = iircas4 (DATA *x, DATA *h, DATA *r, DATA *dbuffer, ushort nbiq, ushort nx)
(defined in iir4cas4.asm)

Arguments
\[ x [n_x] \quad \text{Pointer to input data vector of size } n_x \]
\[ h[4 \times \text{nbiq}] \quad \text{Pointer to filter coefficient vector with the following format:} \]
\[ h = a11 \ b11 \ a21 \ b21 \ ....a1i \ b1i \ a2i \ b2i \]
\[ \text{where } i \text{ is the biquad index (a21 is the a2 coefficient of biquad 1). Pole (recursive) coefficients = a. Zero (non-recursive) coefficients = b} \]
\[ r[n_x] \quad \text{Pointer to output data vector of size } n_x. r \text{ can be equal than } x. \]
dbuffer[2*nbiq+1]  First location of dbuffer is reserved for the index.  Each biquad has 2 delay line elements separated by nbiq locations in the following format:  
\[ d_1(n-1), d_2(n-2), \ldots, d_{i}(n-1), d_1(n-2), d_2(n-2), \ldots, d_{i}(n-2) \]
where \( i \) is the biquad index \((d_2(n-1)\) is the \((n-1)\)th delay element for biquad 2).

- In the case of multiple-buffering schemes, this array should be initialized to 0 for the first block only. Between consecutive blocks, the delay buffer preserves the previous \( r \) output elements needed.

nbiq    Number of biquads

nx    Number of elements of input and output vectors

oflag    Overflow flag.

- If oflag = 1, a 32-bit overflow has occurred
- If oflag = 0, a 32-bit overflow has not occurred

Description
Computes a cascade IIR filter of nbiq biquad sections. Each biquad section is implemented using Direct-form II. All biquad coefficients (4 per biquad) are stored in vector \( h \). The real data input is stored in vector \( x \). The filter output result is stored in vector \( r \).

This function retains the address of the delay filter memory \( d \) containing the previous delayed values to allow consecutive processing of blocks. This function is more efficient for block-by-block filter implementation due to the C-calling overhead. However, it can be used for sample-by-sample filtering (\( nx = 1 \)).

Algorithm
(for biquad)
\[
\begin{align*}
    d(n) &= x(n) - a_1 * d(n - 1) - a_2 * d(n - 2) \\
    y(n) &= d(n) + b_1 * d(n - 1) + b_2 * d(n - 2)
\end{align*}
\]

Overflow Handling Methodology
No scaling implemented for overflow prevention.

Special Requirements
Number of biquads, nbiq, must be even.

Implementation Notes
none

Example
See examples/iircas4 subdirectory
## iircas5

### Benchmarks
(preliminary)

- **Cycles†**: $nx \times (2 + 3 \times nbiq)$
- **Overhead**: 44
- **Code size (in bytes)**: 122

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).

### iircas5

**Cascaded IIR Direct Form II (5 Coefficients per Biquad)**

**Function**

```c
ushort oflag = iircas5 (DATA *x, DATA *h, DATA *r, DATA *dbuffer, ushort nbiq, ushort nx)
```

(defined in iircas5.asm)

**Arguments**

- **x [nx]**: Pointer to input data vector of size nx
- **h[5*nbiq]**: Pointer to filter coefficient vector with the following format:
  
  $h = a11 b11 a21 b21 b01 ... a1i b1i a2i b2i b0i$
  
  where $i$ is the biquad index, $a21$ is the $a2$ coefficient of biquad 1, pole (recursive) coefficients = $a$. Zero (non-recursive) coefficients = $b$
- **r[nx]**: Pointer to output data vector of size nx. $r$ can be equal than $x$.
- **dbuffer[2*nbiq+1]**: Pointer to address of delay line $d$. Each biquad has 2 delay line elements separated by $nbiq$ locations in the following format:
  
  $d1(n–1), d2(n–1),...d1(n–2), d2(n–2),...d1(n–2)$
  
  where $i$ is the biquad index, $d2(n–1)$ is the $(n–1)$th delay element for biquad 2.

- **nbiq**: Number of biquads

In the case of multiple-buffering schemes, this array should be initialized to 0 for the first block only. Between consecutive blocks, the delay buffer preserves the previous elements needed.
nx Number of elements of input and output vectors
oflag Overflow flag.
  □ If oflag = 1, a 32-bit overflow has occurred
  □ If oflag = 0, a 32-bit overflow has not occurred

Description Computes a cascade IIR filter of nbiq biquad sections. Each biquad section is implemented using Direct-form II. All biquad coefficients (5 per biquad) are stored in vector h. The real data input is stored in vector x. The filter output result is stored in vector r.

This function retains the address of the delay filter memory d containing the previous delayed values to allow consecutive processing of blocks. This function is more efficient for block-by-block filter implementation due to the C-calling overhead. However, it can be used for sample-by-sample filtering (nx = 1).

The usage of 5 coefficients instead of 4 facilitates the design of filters with a unit gain of less than 1 (for overflow avoidance), typically achieved by filter coefficient scaling.

Algorithm (for biquad)
\[
d(n) = x(n) - a1 \cdot d(n - 1) - a2 \cdot d(n - 2) \\
y(n) = b0 \cdot d(n) + b1 \cdot d(n - 1) + b2 \cdot d(n - 2)
\]

Overflow Handling Methodology No scaling implemented for overflow prevention.

Special Requirements none

Implementation Notes none

Example See examples/iircas5 subdirectory

Benchmarks (preliminary)

<table>
<thead>
<tr>
<th>Description</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cycles† Core</td>
<td>nx ( \cdot (5 + 5 \cdot \text{nbiq}) )</td>
</tr>
<tr>
<td>Cycles† Overhead</td>
<td>60</td>
</tr>
<tr>
<td>Code size (in bytes)</td>
<td>126</td>
</tr>
</tbody>
</table>

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).
Cascaded IIR Direct Form I (5 Coefficients per Biquad)

Function

```c
ushort oflag = iircas51 (DATA *x, DATA *h, DATA *r, DATA *dbuffer, ushort nbiq, ushort nx)
(defined in iircas51.asm)
```

Arguments

- **x [nx]** Pointer to input data vector of size nx
- **h[5*nbiq]** Pointer to filter coefficient vector with the following format:
  
  \[
  h = b01 \ b11 \ a11 \ a21 \ldots \ b0i \ b1i \ a1i \ a2i
  \]
  
  where \(i\) is the biquad index (\(a21\) is the \(a2\) coefficient of biquad 1). Pole (recursive) coefficients = \(a\). Zero (non-recursive) coefficients = \(b\)
- **r[nx]** Pointer to output data vector of size nx. \(r\) can be equal to \(x\).
- **dbuf[4*nbiq+1]** Pointer to address of delay line \(dbuf\). Each biquad has 4 delay line elements stored consecutively in memory in the following format:
  
  \[
  x1(n-1) \ldots x1(n-2) \ldots x1(n-2), x1(n-1) \ldots x1(n-2) \ldots x1(n-2)
  \]
  
  where \(i\) is the biquad index (\(x1(n-1)\) is the (n-1)th delay element for biquad 1).

- **nbiq** Number of biquads
- **nx** Number of elements of input and output vectors
- **oflag** Overflow flag.
  
  - If oflag = 1, a 32-bit overflow has occurred.
  - If oflag = 0, a 32-bit overflow has not occurred.

Description

Computes a cascade IIR filter of \(nbiq\) biquad sections. Each biquad section is implemented using Direct-form I. All biquad coefficients (5 per biquad) are stored in vector \(h\). The real data input is stored in vector \(x\). The filter output result is stored in vector \(r\).

This function retains the address of the delay filter memory \(d\) containing the previous delayed values to allow consecutive processing of blocks. This func-
tion is more efficient for block-by-block filter implementation due to the C-calling overhead. However, it can be used for sample-by-sample filtering (nx = 1).

The usage of 5 coefficients instead of 4 facilitates the design of filters with a unit gain of less than 1 (for overflow avoidance), typically achieved by filter coefficient scaling.

**Algorithm**  
(for biquad)  
\[ y(n) = b0 \times x(n) + b1 \times x(n - 1) + b2 \times x(n - 2) - a1 \times y(n - 1) - a2 \times y(n - 2) \]

**Overflow Handling Methodology**  
No scaling implemented for overflow prevention.

**Special Requirements**  
none

**Implementation Notes**  
none

**Example**  
See examples/iircas51 subdirectory

**Benchmarks**  
(preliminary)  
Cycles†  
Core: \( nx \times (5 + 8 \times nbiq) \)  
Overhead: 68

Code size  
154  
(in bytes)

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).
**iirlat**

**Lattice Inverse (IIR) Filter**

**Function**

```c
ushort oflag = iirlat (DATA *x, DATA *h, DATA *r, DATA *dbuffer, int nx, int nh)
```

**Arguments**

- **x [nx]** Pointer to real input vector of nx real elements in normal order:
  - x[0]
  - x[1]
  - ...
  - x[nx-2]
  - x[nx-1]

- **h[nh]** Pointer to lattice coefficient vector of size nh in normal order with the first element zero-padded:
  - 0
  - h[0]
  - h[1]
  - ...
  - h[nh-2]
  - h[nh-1]

- **r[nx]** Pointer to output vector of nx real elements. In-place computation (r = x) is allowed.
  - r[0]
  - r[1]
  - ...
  - r[nx-2]
  - r[nx-1]

- **dbuffer[nh]** Delay buffer
  In the case of multiple-buffering schemes, this array should be initialized to 0 for the first block only. Between consecutive blocks, the delay buffer preserves the previous r output elements needed.

- **nx** Number of real elements in vector x (input samples)
nh Number of coefficients
oflag Overflow error flag

- If oflag = 1, a 32-bit data overflow has occurred in an intermediate or final result.
- If oflag = 0, a 32-bit overflow has not occurred.

Description
Computes a real lattice IIR filter implementation using coefficient stored in vector h. The real data input is stored in vector x. The filter output result is stored in vector r. This function retains the address of the delay filter memory d containing the previous delayed values to allow consecutive processing of blocks. This function can be used for both block-by-block and sample-by-sample filtering (nx = 1)

Algorithm
\[ e_i[n] = x[n], \]
\[ e_{i-1}[n] = e_i[n] - hie_{i-1}[n - 1], \hspace{1cm} i = N, (N-1), ..., 1 \]
\[ e'[n] = -ke_{i-1} + e'_{i-1}[n - 1], \hspace{1cm} i = N, (N-1), ..., 1 \]
\[ y[n] = e_0[n] = e'_{-1}[n] \]

Overflow Handling Methodology  No scaling implemented for overflow prevention.

Special Requirements none

Implementation Notes none

Example
See examples/iirlat subdirectory

Benchmarks (preliminary)

<table>
<thead>
<tr>
<th>Cycles†</th>
<th>Core: 4 * (nh – 1) * nx</th>
</tr>
</thead>
<tbody>
<tr>
<td>Overhead: 24</td>
<td></td>
</tr>
</tbody>
</table>

Code size 54
(in bytes)

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).
**ldiv16**

**32-bit by 16-bit Long Division Function**

**Function**

```c
void ldiv16 (LDA[T] *x, DATA *y, DATA *r, DATA *rexp, ushort nx)
```

**Arguments**

- **x [nx]** Pointer to input data vector 1 of size nx
  - `x[0]`
  - `x[1]`
  - 
  - `x[nx-2]`
  - `x[nx-1]`

- **r[nx]** Pointer to output data buffer
  - `r[0]`
  - `r[1]`
  - 
  - `r[nx-2]`
  - `r[nx-1]`

- **rexp[nx]** Pointer to exponent buffer for output values. These exponent values are in integer format.
  - `rexp[0]`
  - `rexp[1]`
  - 
  - `rexp[nx-2]`
  - `rexp[nx-1]`

- **nx** Number of elements of input and output vectors

**Description**

This routine implements a long division function of a Q31 value divided by a Q15 value. The reciprocal of the Q15 value, `y`, is calculated then multiplied by the Q31 value, `x`. The result is returned as an exponent such that:

\[
r[i] \times rexp[i] = \text{true reciprocal in floating-point}
\]

**Algorithm**

The reciprocal of the Q15 number is calculated using the following equation:

\[
Y_m = 2 \times Y_m - Y_m^2 \times Xnorm
\]

If we start with an initial estimate of `Ym`, the equation converges to a solution very rapidly (typically 3 iterations for 16-bit resolution).
The initial estimate can be obtained from a look-up table, from choosing a midpoint, or simply from linear interpolation. The method chosen for this problem is linear interpolation and is accomplished by taking the complement of the least significant bits of the Xnorm value.

The reciprocal is multiplied by the Q31 number to generate the output.

**Overflow Handling Methodology**  none

**Special Requirements**  none

**Implementation Notes**  none

**Example**  See examples/ldiv16 subdirectory

**Benchmarks**  (preliminary)

<table>
<thead>
<tr>
<th>Cycles†</th>
<th>Core: 4 * nx</th>
</tr>
</thead>
<tbody>
<tr>
<td>Overhead: 14</td>
<td></td>
</tr>
</tbody>
</table>

| Code size  | 91  |
| (in bytes)  |

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).

---

**Base 10 Logarithm**

**Function**  

```c
ushton fflag = log_10 (DATA *x, LDATA *r, ushort nx)
```

(defined in log_10.asm)

**Arguments**

- `x[nx]`  Pointer to input vector of size nx.
- `r[nx]`  Pointer to output data vector (Q31 format) of size nx.
- `nx`  Length of input and output data vectors
- `oflag`  Overflow flag.
  - If `oflag = 1`, a 32-bit overflow has occurred.
  - If `oflag = 0`, a 32-bit overflow has not occurred.

**Description**  Computes the log base 10 of elements of vector x using Taylor series.

**Algorithm**  

```
for (i = 0; i < nx; i++) y(i) = log 10 x(i) where -1 < x(i) < 1
```

**Overflow Handling Methodology**  No scaling implemented for overflow prevention
**Special Requirements** none

**Implementation Notes**

\[ y = 0.4343 \times \ln(x) \text{ with } x = M(x) \times 2^P(x) = M \times 2^P \]

\[ y = 0.4343 \times (\ln(M) + \ln(2) \times P) \]

\[ y = 0.4343 \times (\ln(2 \times M) + (P-1) \times \ln(2)) \]

\[ y = 0.4343 \times (\ln((2 \times M-1)+1) + (P-1) \times \ln(2)) \]

\[ y = 0.4343 \times (f(2 \times M-1) + (P-1) \times \ln(2)) \]

with \( f(u) = \ln(1+u) \).

We use a polynomial approximation for \( f(u) \):

\[ f(u) = (((((C6 \times u + C5) \times u + C4) \times u + C3) \times u + C2) \times u + C1) \times u + C0 \]

for \( 0 \leq u \leq 1 \).

The polynomial coefficients \( C_i \) are as follows:

\( C_0 = 0.000\,001\,472 \)

\( C_1 = 0.999\,847\,766 \)

\( C_2 = -0.497\,373\,368 \)

\( C_3 = 0.315\,747\,760 \)

\( C_4 = -0.190\,354\,944 \)

\( C_5 = 0.082\,691\,584 \)

\( C_6 = -0.017\,414\,144 \)

The coefficients \( B_i \) used in the calculation are derived from the \( C_i \) as follows:

| \( B_0 \) | \( Q30 \) | 1581d | 0062Dh |
| \( B_1 \) | \( Q14 \) | 16381d | 03FFDh |
| \( B_2 \) | \( Q15 \) | -16298d | 0C056h |
| \( B_3 \) | \( Q16 \) | 20693d | 050D5h |
| \( B_4 \) | \( Q17 \) | -24950d | 09E8Ah |
| \( B_5 \) | \( Q18 \) | 21677d | 054ADh |
| \( B_6 \) | \( Q19 \) | -9130d | 0DC56h |

**Example**

See examples/log_10 subdirectory

**Benchmarks**

(preliminary)

<table>
<thead>
<tr>
<th>Cycles†</th>
<th>Core: 35 * nx</th>
</tr>
</thead>
<tbody>
<tr>
<td>Overhead: 36</td>
<td></td>
</tr>
<tr>
<td>Code size</td>
<td>162</td>
</tr>
</tbody>
</table>

(in bytes)

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).
**log_2**

**Base 2 Logarithm**

**Function**

\[ \text{ushort oflag} = \text{log}_2 (\text{DATA} \times x, \text{LDATA} \times r, \text{ushort} \ nx) \]

(defined in log_2.asm)

**Arguments**

- \( x[nx] \): Pointer to input vector of size \( nx \).
- \( r[nx] \): Pointer to output data vector (Q31 format) of size \( nx \).
- \( nx \): Length of input and output data vectors.
- \( oflag \): Overflow flag.
  - If \( oflag = 1 \), a 32-bit overflow has occurred.
  - If \( oflag = 0 \), a 32-bit overflow has not occurred.

**Description**

Computes the log base 2 of elements of vector \( x \) using Taylor series.

**Algorithm**

\[
\text{for } (i = 0; i < nx; i + + ) \quad y(i) = \log_2 x(i) \text{ where } 0 < x(i) < 1
\]

**Overflow Handling Methodology**

No scaling implemented for overflow prevention

**Special Requirements**

none

**Implementation Notes**

\[
y = 1.4427 \times \ln(x) \text{ with } x = M(x) \times 2^P(x) = M \times 2^P \\
y = 1.4427 \times (\ln(M) + \ln(2) \times P) \\
y = 1.4427 \times (\ln(2 \times M) + (P-1) \times \ln(2)) \\
y = 1.4427 \times (\ln((2 \times M-1)+1) + (P-1) \times \ln(2)) \\
y = 1.4427 \times (f(2 \times M-1) + (P-1) \times \ln(2)) \\
\text{with } f(u) = \ln(1+u).
\]

We use a polynomial approximation for \( f(u) \) :
\[
f(u) = (((((C6 \times u+C5) \times u+C4) \times u+C3) \times u+C2) \times u+C1) \times u+C0
\]
for \( 0 <= u <= 1 \).

The polynomial coefficients \( C_i \) are as follows:

- \( C_0 = 0.000 \ 001 \ 472 \)
- \( C_1 = 0.999 \ 847 \ 766 \)
- \( C_2 = -0.497 \ 373 \ 368 \)
- \( C_3 = 0.315 \ 747 \ 760 \)
- \( C_4 = -0.190 \ 354 \ 944 \)
- \( C_5 = 0.082 \ 691 \ 584 \)
- \( C_6 = -0.017 \ 414 \ 144 \)
The coefficients $B_i$ used in the calculation are derived from the $C_i$ as follows:

- $B_0 \quad Q30 \quad 1581d \quad 0062Dh$
- $B_1 \quad Q14 \quad 16381d \quad 03FFDh$
- $B_2 \quad Q15 \quad -16298d \quad 0C056h$
- $B_3 \quad Q16 \quad 20693d \quad 050D5h$
- $B_4 \quad Q17 \quad -24950d \quad 09E8Ah$
- $B_5 \quad Q18 \quad 21677d \quad 054ADh$
- $B_6 \quad Q19 \quad -9130d \quad 0DC56h$

Example

See examples/log_2 subdirectory

Benchmarks

(preliminary)

- Cycles

<table>
<thead>
<tr>
<th>Cycles</th>
<th>Core: $36 \times nx$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Overhead: 37</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Code size</th>
<th>166</th>
</tr>
</thead>
<tbody>
<tr>
<td>(in bytes)</td>
<td></td>
</tr>
</tbody>
</table>

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).

**logn**

**Base e Logarithm (natural logarithm)**

**Function**

`ushort oflag = logn (DATA *x, LDATA *r, ushort nx)`  
(defined in logn.asm)

**Arguments**

- `x[nx]` Pointer to input vector of size `nx`.
- `r[nx]` Pointer to output data vector (Q31 format) of size `nx`.
- `nx` Length of input and output data vectors
- `oflag` Overflow flag.
  - If `oflag = 1`, a 32-bit overflow has occurred.
  - If `oflag = 0`, a 32-bit overflow has not occurred.

**Description**

Computes the log base e of elements of vector `x` using Taylor series.

**Algorithm**

for $(i = 0; i < nx; i += 1)$  

\[ y(i) = \log_{nx}(i) \text{ where } -1 < x(i) < 1 \]

**Overflow Handling Methodology**

No scaling implemented for overflow prevention

**Special Requirements**

none
**maxidx**

**Implementation Notes**

\[ y = 0.4343 \times \ln(x) \text{ with } x = M(x) \times 2^P(x) = M \times 2^P \]
\[ y = 0.4343 \times (\ln(M) + \ln(2) \times P) \]
\[ y = 0.4343 \times (\ln((2 \times M - 1) + 1) + (P - 1) \times \ln(2)) \]
\[ y = 0.4343 \times f(2 \times M - 1) + (P - 1) \times \ln(2)) \]

with \( f(u) = \ln(1 + u) \).

We use a polynomial approximation for \( f(u) \):

\[ f(u) = (((((C_6 \times u + C_5) \times u + C_4) \times u + C_3) \times u + C_2) \times u + C_1) \times u + C_0 \]

for \( 0 \leq u \leq 1 \).

The polynomial coefficients \( C_i \) are as follows:

\[ C_0 = 0.000 \ 001 \ 472 \]
\[ C_1 = 0.999 \ 847 \ 766 \]
\[ C_2 = -0.497 \ 373 \ 368 \]
\[ C_3 = 0.315 \ 747 \ 760 \]
\[ C_4 = -0.190 \ 354 \ 944 \]
\[ C_5 = 0.082 \ 691 \ 584 \]
\[ C_6 = -0.017 \ 414 \ 144 \]

The coefficients \( B_i \) used in the calculation are derived from the \( C_i \) as follows:

\[ B_0 \ Q30 \ 1581d \ 0062Dh \]
\[ B_1 \ Q14 \ 16381d \ 03FFDh \]
\[ B_2 \ Q15 \ -16298d \ 0C056h \]
\[ B_3 \ Q16 \ 20693d \ 050D5h \]
\[ B_4 \ Q17 \ -24950d \ 09E8Ah \]
\[ B_5 \ Q18 \ 21677d \ 054ADh \]
\[ B_6 \ Q19 \ -9130d \ 0DC56h \]

**Example**

See examples/logn subdirectory

**Benchmarks**

(preliminary)

Cycles\(^\dagger\) Core: 26 * nx

Overhead: 36

Code size 132

(in bytes)

\(^\dagger\) Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).

**maxidx**

*Index of the Maximum Element of a Vector*

**Function**

short \( r = \) maxidx (DATA *x, ushort ng, ushort ng_size);

(defined in maxidx.asm)

**Arguments**
maxidx

x[nx]  Pointer to input vector of size nx.

r  Index for vector element with maximum value.

ng  Number of groups.

ng_size  Size of group.

Description
The vector x is divided in ng groups of size ng_size.

Size of x = ng x ng_size. ng_size must be an even number between 2 and 34. The larger ng_size, the better the performance. Returns the index of the maximum element of a vector x. The index is a number between 0 and nx – 1. In case of multiple maximum elements, r contains the index of the first maximum element found.

Example 1: size of x is 64.
Choose ng_size = 32, ng = 2

Example 2: size of x is 100.
Choose ng_size = 20, ng = 5

Example 3: size of x is 90.
Choose ng_size = 30, ng = 3

Algorithm  Not applicable

Overflow Handling Methodology  Not applicable

Special Requirements
- ng_size is an even number between 2 and 34.
- nx is an even number.
- Input vector has to be 32-bit aligned.
- Algorithm uses two locations in .bss section.

Implementation Notes  none

Example  See examples/maxidx subdirectory
### maxidx34

**Index of the Maximum Element of a Vector \( \leq 34 \)**

**Function**

short \( r = \text{maxidx34} (\text{DATA} \ast x, \text{ushort} \ nx) \)

(defined in maxidx34.asm)

**Arguments**

- \( x[nx] \) Pointer to input vector of size \( nx \).
- \( r \) Index for vector element with maximum value.
- \( nx \) Length of input data vector (\( nx \leq 34 \)).

**Description**

Returns the index of the maximum element of a vector \( x \). The index is a number between 0 and \( nx - 1 \). In case of multiple maximum elements, \( r \) contains the index of the first maximum element found.

**Algorithm**

Not applicable

**Overflow Handling Methodology**

Not applicable

**Special Requirements**

- Size of the vector, \( nx \leq 34 \)
  - \( nx \) is an even number.
  - Input vector has to be 32-bit aligned.

**Implementation Notes**

none

**Example**

See examples/maxidx34 subdirectory

---

**Benchmarks**

(preliminary)

<table>
<thead>
<tr>
<th>Cycles†</th>
<th>Core:</th>
<th>nx/2 + ng16</th>
</tr>
</thead>
<tbody>
<tr>
<td>Overhead:</td>
<td>40</td>
<td></td>
</tr>
</tbody>
</table>

| Code size | 143 (in bytes) |

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).
maxval

**Maximum Value of a Vector**

**Function**
short \(r = \text{maxval}(\text{DATA} \,*x, \text{ushort} \, nx)\)
(defined in maxval.asm)

**Arguments**
x[nx] Pointer to input vector of size nx.
r Maximum value of a vector
nx Length of input data vector

**Description**
Returns the maximum element of a vector \(x\).

**Algorithm**
Not applicable

**Overflow Handling Methodology**
Not applicable

**Special Requirements**
- nx is an even number.
- Input vector has to be 32-bit aligned.

**Implementation Notes**
none

**Example**
See examples/maxval subdirectory

**Benchmarks**
(preliminary)
Cycles\(^{†}\)
Core: nx
Overhead: 3
Code size 20
(in bytes)

\(^{†}\) Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).
**Description**  
This function finds the index for vector element with maximum value. In case of multiple maximum elements, \( r_{idx} \) contains the index of the first maximum element found. \( r_{val} \) contains the maximum value.

**Algorithm**  
Not applicable

**Overflow Handling Methodology**  
Not applicable

**Special Requirements**  
none

**Implementation Notes**  
none

**Example**  
See examples/maxvec subdirectory

**Benchmarks**  
(preliminary)

- Cycles Core: \( nx*3 \)
- Overhead: 8
- Code size: 26 (in bytes)

---

**minidx**

*Index of the Minimum Element of a Vector*

**Function**  
short \( r = \text{minidx} \) (DATA *x, ushort \( nx \))  
(defined in minidx.asm)

**Arguments**

- \( x[\text{nx}] \)  
  Pointer to input vector of size \( nx \).
- \( r \)  
  Index for vector element with minimum value
- \( nx \)  
  Length of input data vector

**Description**  
Returns the index of the minimum element of a vector \( x \). In case of multiple minimum elements, \( r \) contains the index of the first minimum element found.

**Algorithm**  
Not applicable

**Overflow Handling Methodology**  
Not applicable

**Special Requirements**

- Input vector must be 321–bit aligned.
- Algorithm uses two locations in .bss section.
**minval**  

**Implementation Notes**  
none

**Example**  
See examples/minidx subdirectory

**Benchmarks**  
(preliminary)

<table>
<thead>
<tr>
<th>Cycles†</th>
<th>Core: nx * 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>Overhead:</td>
<td>7</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Code size</th>
<th>26</th>
</tr>
</thead>
<tbody>
<tr>
<td>(in bytes)</td>
<td></td>
</tr>
</tbody>
</table>

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).

---

**minval**  

**Minimum Value of a Vector**

**Function**

short \( r = \text{minval} \left( \text{DATA} \times x, \text{ushort} \ nx \right) \)

(defined in minval.asm)

**Arguments**

- \( x[nx] \)  
  Pointer to input vector of size \( nx \).
- \( r \)  
  Minimum value of a vector
- \( nx \)  
  Length of input data vector

**Description**

Returns the minimum element of a vector \( x \).

**Algorithm**

Not applicable

**Overflow Handling Methodology**

Not applicable

**Special Requirements**

- \( nx \) is an even number.
- Input vector has to be 32-bit aligned.

**Implementation Notes**  
none

**Example**  
See examples/minval subdirectory

**Benchmarks**  
(preliminary)

<table>
<thead>
<tr>
<th>Cycles†</th>
<th>Core: ( nx/2 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Overhead:</td>
<td>7</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Code size</th>
<th>20</th>
</tr>
</thead>
<tbody>
<tr>
<td>(in bytes)</td>
<td></td>
</tr>
</tbody>
</table>

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).
<table>
<thead>
<tr>
<th><strong>minvec</strong></th>
<th><strong>Index and Value of the Minimum Element of a Vector</strong></th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Function</strong></td>
<td>void minvec (DATA *x, ushort nx, DATA *r_val, DATA *r_idx) (defined in minvec.asm)</td>
</tr>
<tr>
<td><strong>Arguments</strong></td>
<td>x[nx] Pointer to input vector of size nx.</td>
</tr>
<tr>
<td></td>
<td>r_val Minimum value</td>
</tr>
<tr>
<td></td>
<td>r_idx Index for vector element with minimum value</td>
</tr>
<tr>
<td></td>
<td>nx Length of input data vector (nx ≥ 6)</td>
</tr>
<tr>
<td><strong>Description</strong></td>
<td>This function finds the index for vector element with minimum value. In case of multiple minimum elements, r_idx contains the index of the first minimum element found. r_val contains the minimum value.</td>
</tr>
<tr>
<td><strong>Algorithm</strong></td>
<td>Not applicable</td>
</tr>
<tr>
<td><strong>Overflow Handling Methodology</strong></td>
<td>Not applicable</td>
</tr>
<tr>
<td><strong>Special Requirements</strong></td>
<td>none</td>
</tr>
<tr>
<td><strong>Implementation Notes</strong></td>
<td>none</td>
</tr>
<tr>
<td><strong>Example</strong></td>
<td>See examples/minvec subdirectory</td>
</tr>
<tr>
<td><strong>Benchmarks</strong></td>
<td>(preliminary)</td>
</tr>
<tr>
<td></td>
<td>Cycles Core: nx*3</td>
</tr>
<tr>
<td></td>
<td>Overhead: 8</td>
</tr>
<tr>
<td></td>
<td>Code size (bytes) 26</td>
</tr>
</tbody>
</table>
Matrix Multiplication

Function

```c
ushort oflag = mmul (DATA *x1,short row1,short col1,DATA *x2,short row2,short col2,DATA *r)
(defined in mmul.asm)
```

Arguments

- `x1[row1*col1]`: Pointer to input vector of size nx
- `x1[row1*col1]`: Pointer to input matrix of size row1*col1
- `row1`: number of rows in matrix 1
- `col1`: number of columns in matrix 1
- `x2[row2*col2]`: Pointer to input matrix of size row2*col2
- `row2`: number of rows in matrix 2
- `col2`: number of columns in matrix 2
- `r[row1*col2]`: Pointer to output data vector of size row1*col2
- `r[row1*col2]`: Pointer to output matrix of size row1*col2

Description

This function multiplies two matrices

Algorithm

Multiply input matrix A (M by N) by input matrix B (N by P) using 2 nested loops:

```c
for i = 1 to M
    for k = 1 to P
    {
        temp = 0
        for j = 1 to N
            temp = temp + A(i,j) * B(j,k)
        C(i,k) = temp
    }
```

Overflow Handling Methodology

Not applicable

Special Requirements

- Verify that the dimensions of input matrices are legal, i.e. col1 == row2
- `x2[ ]` matrix must be located in the internal memory.
Implementation Notes  In order to take advantage of the dual MAC architecture of the C55x, this implementation checks the size of the matrix \( x_1 \). For small matrices \( x_1 \) (row1 < 4 or col1 < 2), single MAC loops are used. For larger matrices \( x_1 \) (row1 ≥ 4 and col1 ≥ 2), Dual MAC loops are more efficient and quickly make up for the additional initialization overhead.

Example  See examples/mmul subdirectory

Benchmarks  (preliminary)

<table>
<thead>
<tr>
<th>Cycles†</th>
<th>Code size (in bytes)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Core:</td>
<td>215</td>
</tr>
<tr>
<td>if(row1 &lt; 4</td>
<td></td>
</tr>
<tr>
<td>if((row1==even)&amp;&amp;(row1 ≥ 4)&amp;&amp;(col1 ≥ 2)), use dual MAC ((col1 + 4)<em>0.5</em>row1 + 10)col2</td>
<td></td>
</tr>
<tr>
<td>if((row1==odd)&amp;&amp;(row1 ≥ 4)&amp;&amp;(col1 ≥ 2), use dual MAC ((col1 + 4)<em>0.5</em>(row1 – 1) + col1 + 12)col2</td>
<td></td>
</tr>
<tr>
<td>Overhead: 30</td>
<td></td>
</tr>
</tbody>
</table>

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).

\[ mtrans \]

**Matrix Transpose**

**Function**

\[
\mathtt{ushort} \ \mathtt{oflag} = \mathtt{mtrans} \ (\mathtt{DATA} \ *x, \ \mathtt{short} \ \mathtt{row}, \ \mathtt{short} \ \mathtt{col}, \ \mathtt{DATA} \ *r)
\]

(defined in mtrans.asm)

**Arguments**

- \( x[\mathtt{row} * \mathtt{col}] \)  Pointer to input matrix. In-place processing is not allowed.
- \( \mathtt{row} \)  number of rows in matrix
- \( \mathtt{col} \)  number of columns in matrix
- \( r[\mathtt{row} * \mathtt{col}] \)  Pointer to output data vector

**Description**

This function transposes matrix \( x \)

**Algorithm**

\[
\text{for } i = 1 \text{ to } M \\
\quad \text{for } j = 1 \text{ to } N \\
\quad \quad C(j,i) = A(i,j)
\]

**Overflow Handling Methodology**  Not applicable
mul32

Special Requirements none

Implementation Notes none

Example See examples/mtrans subdirectory

Benchmarks (preliminary)

<table>
<thead>
<tr>
<th>Cycles†</th>
<th>Core: (1 + col) * row</th>
</tr>
</thead>
<tbody>
<tr>
<td>Overhead: 23</td>
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</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Code size</th>
<th>65</th>
</tr>
</thead>
<tbody>
<tr>
<td>(in bytes)</td>
<td></td>
</tr>
</tbody>
</table>

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).

mul32 32-bit Vector Multiplication

Function ushort oflag = mul32 (LDATA *x, LDATA *y, LDATA *r, ushort nx) (defined in mul32.asm)

Arguments

<table>
<thead>
<tr>
<th>x[nx]</th>
<th>Pointer to input data vector of size nx. In-place processing allowed (r can be = x = y)</th>
</tr>
</thead>
<tbody>
<tr>
<td>y[nx]</td>
<td>Pointer to input data vector of size nx</td>
</tr>
<tr>
<td>r[nx]</td>
<td>Pointer to output data vector of size nx</td>
</tr>
<tr>
<td>nx</td>
<td>Number of elements of input and output vectors. Nx ≥ 4</td>
</tr>
<tr>
<td>oflag</td>
<td>Overflow flag</td>
</tr>
</tbody>
</table>

☐ If oflag = 1, a 32-bit overflow has occurred
☐ If oflag = 0, a 32-bit overflow has not occurred

Description This function multiplies two 32-bit Q31 vectors, element by element, and produces a 32-bit Q31 vector.

Algorithm for (i = 0; i < nx; i + +) 

\[ z(i) = x(i) * y(i) \]

Overflow Handling Methodology Scaling implemented for overflow prevention (user selectable)

Special Requirements

☐ Input and Output vectors must be 32-bit aligned.
Unfortunately, the text is not clearly visible in the image. It appears to be a page from a technical document discussing a function named `neg`. The text includes implementation notes, example usage, benchmarks, function descriptions, and arguments. The function `neg` is described as negating each element of a vector (fractional values) and includes special cases and algorithm for handling this operation. The page also includes a description of how to use the function, benchmarks for cycles and code size, and a note on overflow handling methodology. The page number is 4-91.
**neg32**

**Benchmarks** (preliminary)

<table>
<thead>
<tr>
<th>Cycles†</th>
<th>Core: 4 * nx</th>
</tr>
</thead>
<tbody>
<tr>
<td>Overhead:</td>
<td>13</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Code size</th>
<th>61</th>
</tr>
</thead>
</table>

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).

**neg32**

**Vector Negate (double-precision)**

**Function**

ushort oflag = neg32 (LDATA *x, LDATA *r, ushort nx)

(defined in neg.asm)

**Arguments**

x[nx] Pointer to input data vector of size nx. In-place processing allowed (r can be = x = y)

r[nx] Pointer to output data vector of size nx. In-place processing allowed

Special cases:

- If x = -1 = 32768 * 2^16, then r = 1 = 321767 * 2^16 with oflag = 1
- If x = 1 = 32767 * 2^16, then r = -1 = 321768 * 2^16 with oflag = 1

nx Number of elements of input and output vectors.

nx \( \geq 4 \)

oflag Overflow flag.

- If oflag = 1, a 32-bit overflow has occurred.
- If oflag = 0, a 32-bit overflow has not occurred.

Caution: overflow in negation of a Q31 number can happen naturally when negating (-1).

**Description**

This function negates each of the elements of a vector (fractional values).

**Algorithm**

for \((i = 0; i < nx; i++)\) \(x(i) = -x(i)\)

**Overflow Handling Methodology**

Saturation implemented for overflow handling

**Special Requirements**
Input and Output vectors must be 32-bit aligned.

Implementation Notes

Example
See examples/neg32 subdirectory

Benchmarks
(preliminary)

Cycles†
Core: 4 * nx

Overhead: 13

Code size
61
(in bytes)

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).

Vector Power

Function
ushort oflag = power (DATA *x, LDATA *r, ushort nx)
(defined in power.asm)

Arguments

x[nx] Pointer to input data vector of size nx. In-place processing allowed (r can be = x = y)

r[1] Pointer to output data vector element in Q31 format

Special cases:
- if x = -1 = 32768*2^16, then r = 1 = 321767*2^16 with oflag = 1
- if x = 1 = 32767*2^16, then r = -1 = 321768*2^16 with oflag = 1

nx Number of elements of input vectors.

nx ≥ 4

oflag Overflow flag.

- If oflag = 1, a 32-bit overflow has occurred.
- If oflag = 0, a 32-bit overflow has not occurred.

Description
This function calculates the power (sum of products) of a vector.

Algorithm
Power = 0 for (i = 0; i < nx; i + + ) power += x(i) * x(i)
q15tofl

Special Requirements

- Output vector must be 32-bit aligned.

Implementation Notes

none

Example

See examples/power subdirectory

Benchmarks (preliminary)

<table>
<thead>
<tr>
<th>Cycles†</th>
<th>Core:</th>
<th>nx – 1</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Overhead:</td>
<td>12</td>
</tr>
</tbody>
</table>

Code size 54 (in bytes)

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).

q15tofl

Q15 to Floating-point Conversion

Function

ushort q15tofl (DATA *x, float *r, ushort nx)
(defined in q152fl.asm)

Arguments

x[nx] Pointer to Q15 input vector of size nx.

r[nx] Pointer to floating-point output data vector of size nx containing the floating-point equivalent of vector x.

nx Length of input and output data vectors

Description

Converts the Q15 stored in vector x to IEEE floating-point numbers stored in vector r.

Algorithm

Not applicable

Overflow Handling Methodology

Saturation implemented for overflow handling

Special Requirements

- Output vector must be 32-bit aligned.

Implementation Notes

none

Example

See examples/ug subdirectory

Benchmarks (preliminary)
**rand16**

**Random Number Generation Algorithm**

**Function**

`ushort oflag = rand16 (DATA *r, ushort nr)`

**Arguments**

- `*r` Pointer to the array where the 16-bit random numbers are stored
- `nr` Number of random numbers that are generated
- `oflag` Overflow error flag (returned value)
  - If `oflag = 1`, a 32-bit data overflow occurred in an intermediate or final result.
  - If `oflag = 0`, a 32-bit overflow has not occurred.

**Description**

This algorithm computes an array of random numbers based on the linear congruential method introduced by D. Lehmer in 1951. This is one of the fastest and simplest techniques of generating random numbers. The code shown here generates 16-bit integers, however, if a 32-bit value is desired the code can be modified to perform 32-bit multiplies using the defined constants RNDMULT and RNDINC. The disadvantage of this technique is that it is very sensitive to the choice of RNDMULT and RNDINC.

**Algorithm**

\[ r[n] = \left( (r[n-1] \times RNDMULT) + RNDINC \right) \mod M \]

where \( 0 \leq n \leq nr \) and \( 0 \leq M \leq 65536 \)

**Overflow Handling Methodology**

No scaling implemented for overflow prevention.

**Special Requirements**

No special requirements.

---

Cycles†

Core: \( 7 \times nx \) (if \( x[n] = 0 \))
\( 32 \times nx \)

Overhead: 18

Code size: 124
(in bytes)

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).
Implementation Notes

Rand16() is written so that it can be called from a C program. Prior to calling rand16(), rand16i() can be called to initialize the random number generator seed value. The C routine passes two parameters to rand16(): A pointer to the random number array *r and the count of random numbers (nr) desired. The random numbers are declared as short or 16 bit values. Two constants RNDMULT and RNDINC are defined in the function. The algorithm is sensitive to the choice of RNDMULT and RNDINC so exercise caution when changing these.

M This value is based on the system that the routine runs. This routine returns a random number from 0 to 65536 (64K) and is NOT internally bounded. If you need a min/max limit, this must be coded externally to this routine.

RNDSEED An arbitrary constant that can be any value between 0 and 64K. If 0 (zero) is chosen, then RNDINC should be some value greater than 1. Otherwise, the first two values will be 0 and 1. To change the set of random numbers generated by this routine, change the RNDSEED value. In this routine, RNDSEED is initialized to 21845, which is 65536/3.

RNDMULT Should be chosen such that the last three digits fall in the pattern even_digit−2−1 such as xx821, xx421 etc. RNDMULT = 31821 is used in this routine.

RNDINC In general, this constant can be any prime number related to M. Research shows that RNDINC (the increment value) should be chosen by the following formula:

$$RNDINC = ((1/2 - (1/6 \times \text{SQRT}(3))) \times M)$$

Using M=65536, RNDINC was picked as 13849.

The random seed initialized in rand16i() is used to generate the first random number. Each random number generated is used to generate the next number in the series. The random number is generated in the accumulator (32 bits) by using the multiply-accumulate (MAC) unit to do the computation. In the course of the algorithm if there is intermediate overflow, the overflow flag bit in status register is set. At the end of the algorithm, the overflow flag is tested for any intermediate overflow conditions.

Example

See examples/rand16 subdirectory
Benchmarks

<table>
<thead>
<tr>
<th>Function</th>
<th>Cycles</th>
<th>Code size</th>
</tr>
</thead>
<tbody>
<tr>
<td>Core:</td>
<td>13 + nr^2</td>
<td>49</td>
</tr>
<tr>
<td>Overhead:</td>
<td>10</td>
<td></td>
</tr>
</tbody>
</table>

**C54x Benchmark for Comparison**

<table>
<thead>
<tr>
<th>Function</th>
<th>Cycles</th>
<th>Code size</th>
</tr>
</thead>
<tbody>
<tr>
<td>Core:</td>
<td>10 + nr^4</td>
<td>56</td>
</tr>
<tr>
<td>Overhead:</td>
<td>16</td>
<td></td>
</tr>
</tbody>
</table>

**rand16init Random Number Generation Initialization**

**Function**
void rand16init(void)

**Arguments**
none

**Description**
Initializes seed for 16-bit random number generator.

**Algorithm**
Not applicable

**Overflow Handling Methodology**
No scaling implemented for overflow prevention.

**Special Requirements**
Allocation of .bss section is required in linker command file.

**Implementation Notes**
This function initializes a global variable rndseed in global memory to be used for the 16 bit random number generation routine (rand16)

**Example**
See examples/rand16i subdirectory

**Benchmarks**

<table>
<thead>
<tr>
<th>Function</th>
<th>Cycles</th>
<th>Code size</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>6</td>
<td>9</td>
</tr>
</tbody>
</table>

**C54x Benchmark for Comparison**

<table>
<thead>
<tr>
<th>Function</th>
<th>Cycles</th>
<th>Code size</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>7</td>
<td>10</td>
</tr>
</tbody>
</table>
**16-bit Reciprocal Function**

**Function**

```c
void recip16 (DATA *x, DATA *r, DATA *rexp, ushort nx)
```

**Arguments**

- `x[nx]` Pointer to input data vector 1 of size `nx`.
  - `x[0]`
  - `x[1]`
  - ...
  - `x[nx-2]`
  - `x[nx-1]`

- `r[nx]` Pointer to output data buffer
  - `r[0]`
  - `r[1]`
  - ...
  - `r[nx-2]`
  - `r[nx-1]`

- `rexp[nx]` Pointer to exponent buffer for output values. These exponent values are in integer format.
  - `rexp[0]`
  - `rexp[1]`
  - ...
  - `rexp[nx-2]`
  - `rexp[nx-1]`

- `nx` Number of elements of input and output vectors

**Description**

This routine returns the fractional and exponential portion of the reciprocal of a Q15 number. Since the reciprocal is always greater than 1, it returns an exponent such that:

```
r[i] * r exp[i] = true reciprocal in floating-point
```

**Algorithm**

```
Ym = 2 * Ym - Ym^2 * Xnorm
```

If we start with an initial estimate of `Ym`, the equation converges to a solution very rapidly (typically 3 iterations for 16-bit resolution).
The initial estimate can be obtained from a look-up table, from choosing a mid-point, or simply from linear interpolation. The method chosen for this problem is linear interpolation and is accomplished by taking the complement of the least significant bits of the Xnorm value.

**Overflow Handling Methodology**  none

**Special Requirements**  none

**Implementation Notes**  none

**Example**  See examples/recip16 subdirectory

**Benchmarks**  (preliminary)

Cycles\(^\dagger\)  Core:  33 \* nx

Overhead:  12

Code size  69

(in bytes)

\(^\dagger\) Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).

---

**rfft**

*Forward Real FFT (in-place)*

**Function**

`void rfft (DATA *x, ushort nx, type);`

*(reference cfft.asm, cbrev.asm, unpack.asm)*

**Arguments**

- **x [nx]**  Pointer to input vector containing nx real elements. On output, vector x contains the first half (nx/2 complex elements) of the FFT output in the following order. Real FFT is a symmetric function around the Nyquist point, and for this reason only half of the FFT(x) elements are required.

  On output x will contain the FFT(x) = y in the following format:

  \[
  y(0)Re y(nx/2)Im \rightarrow DC and Nyquist
  y(1)Re y(1)Im
  y(2)Re y(2)Im
  \ldots
  y(nx/2)Re y(nx/2)Im
  \]

  Complex numbers are stored in Re-Im format

- **nx**  Number of real elements in vector x. can take the following values.

  \[ nx = 16, 32, 64, 128, 256, 512, 2048 \]
type RFFT type selector. Types supported:
- If type = SCALE, scaled version selected
- If type = NOSCALE, non-scaled version selected

Description Computes a Radix-2 real DIT FFT of the nx real elements stored in vector x in normal order. The original content of vector x is destroyed in the process. The first nx/2 complex elements of the RFFT(x) are stored in vector x in normal-order.

Algorithm (DFT)
See CFFT

Special Requirements
- Input vector must be aligned on a 32-bit boundary.
- Twiddle table must be located in the internal memory.
- Ensure that the entire data buffer fits within a 64K boundary (the largest possible array addressable by the 16-bit auxiliary register).
- For best performance, the data buffer has to be in a DARAM block.
- If the twiddle table and the data buffer are in the same DARAM block, then the radix-2 kernel is 7 cycles and the radix-4 kernel is not affected.

Implementation Notes Implemented as a complex FFT of size nx/2 followed by an unpack stage to unpack the real FFT results. Therefore, Implementation Notes for the cfft function apply to this case.

Notice that normally an FFT of a real sequence of size N, produces a complex sequence of size N (or 2*N real numbers) that will not fit in the input sequence. To accommodate all the results without requiring extra memory locations, the output reflects only half of the spectrum (complex output). This still provides the full information because an FFT of a real sequence has even symmetry around the center or nyquist point (N/2).

When scale = 1, this routine prevents overflow by scaling by 2 at each FFT intermediate stages and at the unpacking stage.
Comparing the results to MATLAB:

The C55 DSPLIB rfft() function is implemented as follows using the cfft() and unpack() functions. (N denotes the size of the real fft)

C55 DSPLIB

\[ rfft(\.) \quad \leftrightarrow \quad \text{cfft(\>, N/2} \quad \text{Unpack(\.)} \]

- **NOSCALE** version

C55 DSPLIB

\[ rfft(\.) \quad \leftrightarrow \quad \text{cfft(\>, N} \quad x N/2 \]

MATLAB

The unpack routine in the DSPLIB always scales by two the data independently of the scaled or non-scaled rfft(). In order to compare the results to the MATLAB results, the MATLAB results need to be multiplied by a factor of N/2 (N is the rfft size).

- **SCALE** version

C55 DSPLIB

\[ rfft(\.) \quad \leftrightarrow \quad \text{cfft(\>, N} \]

MATLAB

The C55 DSPLIB scaled rfft results can be compared to the unmodified MATLAB cfft results.
**rfft32**

**Forward 32-bit Real FFT (in-place)**

**Function**

```c
void rfft32 (LDATA *x, ushort nx, type);
```

(Reference cfft32.asm, cbrev32.asm, unpack32.asm)

**Arguments**

- **x [nx]** Pointer to input vector containing nx 32-bit real elements. On output, vector x contains the first (nx/2 complex elements) of the FFT output in the following order. Real FFT is a symmetric function around the Nyquist point, and for this reason only half of the FFT(x) elements are required.
  
  On output x will contain the FFT(x) = y in the following format:
  
  \[
  y(0) \rightarrow DC \text{ and Nyquist} \\
  y(1) \text{Re} y(1) \text{Im} \\
  y(2) \text{Re} y(2) \text{Im} \\
  \vdots \\
  y(nx/2) \text{Re} y(nx/2) \text{Im}
  \]

  Complex numbers are stored in Re-Im format.

- **nx** Number of real elements in vector x. can take the following values.
  
  \[ nx = 16, 32, 64, 128, 256, 512, 1024, 2048 \]

- **type** RFFT type selector. Types supported:
  
  - If type = SCALE, scaled version selected
  - If type = NOSCALE, non-scaled version selected

**Description**

Computes a Radix-2 real DIT FFT of the nx real elements stored in vector x in normal order. The original content of vector x is destroyed in the process. The first nx/2 complex elements of the RFFT(x) are stored in vector x in normal-order.

**Algorithm**

(DFT)

See CFFT

**Special Requirements**

- Input vector must be aligned on a 32-bit boundary.
- Twiddle table must be located in the internal memory.
  
  - Ensure that the entire data buffer fits within a 64K boundary (the largest possible array addressable by the 16-bit auxiliary register).
  - For best performance, the data buffer has to be in a DARAM block.
For best performance, the coefficient buffer can be in an SARAM block or a DARAM different from the DARAM clock that contains the data buffer.

**Implementation Notes** Implemented as a complex FFT of size \( nx/2 \) followed by an unpack stage to unpack the real FFT results. Therefore, Implementation Notes for the `cfft` function apply to this case.

Notice that normally an FFT of a real sequence of size \( N \), produces a complex sequence of size \( N \) (or \( 2*N \) real numbers) that will not fit in the input sequence. To accommodate all the results without requiring extra memory locations, the output reflects only half of the spectrum (complex output). This still provides the full information because an FFT of a real sequence has even symmetry around the center or nyquist point \( (N/2) \).

When `scale = 1`, this routine prevents overflow by scaling by 2 at each FFT intermediate stages and at the unpacking stage.

**Example** See examples/rfft32 subdirectory

---

### rifft

**Inverse Real FFT (in-place)**

**Function**

```c
void rifft (DATA *x, ushort nx, type);
```

**Arguments**

- `x [nx]` Pointer to input vector \( x \) containing \( nx \) real elements. The unpacki routine should be called to unpack the rfft sequence before calling the bit reversal routine. (See examples directory for calling sequence)

  - On output, the vector \( x \) contains \( nx \) complex elements corresponding to \( \text{RIFFT}(x) \) or the signal itself.

- `nx` Number of real elements in vector \( x \). \( nx \) can take the following values.

  - \( nx = 16, 32, 64, 128, 256, 512, 1024, 2048 \)

- `type` RFFT type selector. Types supported:
  - If `type = SCALE`, scaled version selected
  - If `type = NOSCALE`, non-scaled version selected

**Description** Computes a Radix-2 real DIT IFFT of the \( nx \) real elements stored in vector \( x \) in bit-reversed order. The original content of vector \( x \) is destroyed in the process. The first \( nx/2 \) complex elements of the IFFT(\( x \)) are stored in vector \( x \) in normal-order.
Algorithm  (IDFT)  
See CIFFT

Special Requirements

- Input vector must be aligned on a 32-bit boundary.
- Twiddle table must be located in the internal memory.
  - Ensure that the entire data buffer fits within a 64K boundary (the largest possible array addressable by the 16-bit auxiliary register).
  - For best performance, the data buffer has to be in a DARAM block.
  - If the twiddle table and the data buffer are in the same DARAM block, then the radix-2 kernel is 7 cycles and the radix-4 kernel is not affected.

Implementation Notes  Implemented as a complex IFFT of size nx/2 followed by an unpack stage to unpack the real IFFT results. Therefore, Implementation Notes for the cfft function apply to this case.

Notice that normally an IFFT of a real sequence of size N, produces a complex sequence of size N (or 2*N real numbers) that will not fit in the input sequence. To accommodate all the results without requiring extra memory locations, the output reflects only half of the spectrum (complex output). This still provides the full information because an IFFT of a real sequence has even symmetry around the center or nyquist point(N/2).

When scale = 1, this routine prevents overflow by scaling by 2 at each IFFT intermediate stages and at the unpacking stage.

Example  See examples/rifft subdirectory
**Function Descriptions**

### rifft32

**Inverse 32-bit Real FFT (in-place)**

**Function**

```
void rifft32 (LDATA *x, ushort nx, type);
```

*(reference cifft32.asm, cbrev32.asm, and unpacki32.asm)*

**Arguments**

- **x [nx]** Pointer to input vector x containing nx 32-bit real elements. On output, the vector x contains nx complex elements corresponding to RIFFT(x) or the signal itself.
- **nx** Number of real elements in vector x. nx can take the following values:
  - nx = 16, 32, 64, 128, 256, 512, 1024, 2048
- **type** RFFT type selector. Types supported:
  - If type = SCALE, scaled version selected
  - If type = NOSCALE, non-scaled version selected

**Description**

Computes a Radix-2 real DIT IFFT of the nx real elements stored in vector x in bit-reversed order. The original content of vector x is destroyed in the process. The first nx/2 complex elements of the IFFT(x) are stored in vector x in normal-order.

**Algorithm**

(IDFT)

See CIFFT

**Special Requirements**

- Twiddle table must be located in the internal memory.
- Ensure that the entire data buffer fits within a 64K boundary (the largest possible array addressable by the 16-bit auxiliary register).
- For best performance, the data buffer has to be in a DARAM block.
- For best performance, the coefficient buffer can be in an SARAM clock or a DARAM different from the DARAM block that contains the data buffer.

**Implementation Notes**

Implemented as a complex IFFT of size nx/2 followed by an unpack stage to unpack the real IFFT results. Therefore, Implementation Notes for the cift32 function apply to this case.
Notice that normally an IFFT of a real sequence of size N, produces a complex sequence of size N (or 2*N real numbers) that will not fit in the input sequence. To accommodate all the results without requiring extra memory locations, the output reflects only half of the spectrum (complex output). This still provides the full information because an IFFT of a real sequence has even symmetry around the center or nyquist point (N/2).

When scale = 1, this routine prevents overflow by scaling by 2 at each IFFT intermediate stages and at the unpacking stage.

Example
See examples/rifft subdirectory

**sine**

**Function**

```c
ushort oflag = sine (DATA *x, DATA *r, ushort nx)
(defined in sine.asm)
```

**Arguments**

- **x[nx]** Pointer to input vector of size nx. x contains the angle in radians between \([-\pi, \pi]\] normalized between \((-1,1)\) in q15 format.
  - \(x = \frac{x\text{rad}}{\pi}\)
  - For example:
    - \(45^\circ = \frac{\pi}{4}\) is equivalent to \(x = 1/4 = 0.25 = 0x200\) in q15 format.
- **r[nx]** Pointer to output vector containing the sine of vector x in q15 format.
- **nx** Number of elements of input and output vectors.
  - \(nx \geq 4\)
- **oflag** Overflow flag.
  - If oflag = 1, a 32-bit overflow has occurred.
  - If oflag = 0, a 32-bit overflow has not occurred.

**Description**
Computes the sine of elements of vector x. It uses Taylor series to compute the sine of angle x.

**Algorithm**

\[
\text{for } (i = 0; i < nx; i + +) \quad y(i) = \sin(x(i)) \text{ where } x(i) = \frac{x\text{rad}}{\pi}
\]

**Overflow Handling Methodology**
Not applicable

**Special Requirements** none
Function Descriptions

**sqrt_16**

**Implementation Notes** Computes the sine of elements of vector x. It uses the following Taylor series to compute the angle x in quadrant 1 \((0−\pi/2)\).

\[
\sin(x) = c1*x + c2*x^2 + c3*x^3 + c4*x^4 + c5*x^5
\]

- \(c1 = 3.140625x\)
- \(c2 = 0.02026367\)
- \(c3 = -5.3251\)
- \(c4 = 0.5446778\)
- \(c5 = 1.800293\)

The angle x in other quadrant is calculated by using symmetries that map the angle x into quadrant 1.

**Example**

See examples/sine subdirectory

**Benchmarks**

(preliminary)

- Cycles† Core: 19 * nx
- Overhead: 17

- Code size 93 program; 3 data

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).

**sqrt_16**

Square Root of a 16-bit Number

**Function**

\[
\text{ushort oflag = sqrt_16 (DATA \text{x}, DATA \text{r}, short \text{nx})}
\]

(defined in sqrtv.asm)

**Arguments**

- x[nx] Pointer to input vector of size nx.
- r[nx] Pointer to output vector of size nx containing the sqrt(x).
- nx Number of elements of input and output vectors.
- oflag Overflow flag.

- If oflag = 1, a 32-bit overflow has occurred.
- If oflag = 0, a 32-bit overflow has not occurred.

**Description**

Calculates the square root for each element in input vector x, storing results in output vector r.

**Algorithm**

\[
\text{for (} i = 0; \ i < \text{nx}; \ i ++ \text{)} \quad r[i] = \sqrt{x(i)} \quad 0 \leq i \leq \text{nx}
\]
Overflow Handling Methodology  Not applicable

Special Requirements  none

Implementation Notes  The square root of a number(x) can be calculated using Newton’s method. An initial approximation is guessed and then the approximation gets recomputed using the formula,

\[ \text{new approximation} = \text{old approximation} - \frac{(\text{old approximation}^2 - x)}{2}. \]

The new approximation then becomes the old approximation and the process is repeated until the desired accuracy is reached.

Example  See examples/sqrtv subdirectory

Benchmarks  (preliminary)

<table>
<thead>
<tr>
<th>Cycles†</th>
<th>Core: 35 * nx</th>
</tr>
</thead>
<tbody>
<tr>
<td>Overhead:</td>
<td>14</td>
</tr>
<tr>
<td>Code size (in bytes)</td>
<td>84 program; 5 data</td>
</tr>
</tbody>
</table>

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).

Vector Subtract

Function  short oflag = sub (DATA *x, DATA *y, DATA *r, ushort nx, ushort scale)  (defined in sub.asm)

Arguments

- **x[nx]**  Pointer to input data vector 1 of size nx. In-place processing allowed (r can be = x = y)
- **y[nx]**  Pointer to input data vector 2 of size nx
- **r[nx]**  Pointer to output data vector of size nx containing
  - (x−y) if scale =0
  - (x−y)/2 if scale =1
- **nx**  Number of elements of input and output vectors. nx ≥ 4
scale  Scale selection
☐ If scale = 1, divide the result by 2 to prevent overflow.
☐ If scale = 0, do not divide by 2.

oflag  Overflow flag.
☐ If oflag = 1, a 32-bit overflow has occurred.
☐ If oflag = 0, a 32-bit overflow has not occurred.

**Description**
This function subtracts two vectors, element by element.

**Algorithm**
\[
\text{for } (i = 0; i < nx; i + +) \quad z(i) = x(i) - y(i)
\]

**Overflow Handling Methodology**
Scaling implemented for overflow prevention (user selectable)

**Special Requirements**
none

**Implementation Notes**
none

**Example**
See examples/sub subdirectory

**Benchmarks**
(preliminary)

- Cycles†
  - Core: 3 * nx
  - Overhead: 23

- Code size 60
  (in bytes)

† Assumes all data is in on-chip dual-access RAM and that there is no bus conflict due to twiddle table reads and instruction fetches (provided linker command file reflects those conditions).
All functions in the DSPLIB are provided with execution time and code size benchmarks. While developing the included functions, we tried to compromise between speed, code size, and ease of use. However, with few exceptions, the highest priority was given to optimize for speed and ease of use, and last for code size.

Even though DSPLIB can be used as a first estimation of processor performance for a specific function, you should know that the generic nature of DSPLIB may add extra cycles not required for customer specific usage.

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5.1 What DSPLIB Benchmarks are Provided

DSPLIB documentation includes benchmarks for instruction cycles and memory consumption. The following benchmarks are typically included in the assembly source files:

- Calling and register initialization overhead

- Number of cycles in the kernel code: Typically provided in the form of an equation that is a function of the data size parameters. We consider the kernel (or core) code, the instructions contained between the _start and _end labels that you can see in each of the functions.

- Memory consumption: Typically program size in bytes is reported. For functions requiring significant internal data allocation, data memory consumption is also provided. When stack usage for local variables is minimum, that data consumption is not reported.

For functions in which it is difficult to determine the number of cycles in the kernel code as a function of the data size parameters, we have included direct cycle count for specific data sizes.

5.2 Performance Considerations

Benchmark cycles presented assume best case conditions, typically assuming:

- 0 wait-state memory external memory for program and data
- data allocation to on-chip DARAM
- no pipeline hits

A linker command file showing the memory allocation used during testing and benchmarking in the Code Composer C55x Simulator is included under the example subdirectory.

Remember, execution speed in a system is dependent on where the different sections of program and data are located in memory. Be sure to account for such differences, when trying to explain why a routine is taking more time that the reported DSPLIB benchmarks.
Software Updates and Customer Support

This chapter details the software updates and customer support issues for the TMS320C55x DSPLIB.

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6.1 DSPLIB Software Updates

C55x DSPLIB Software updates will be periodically released, incorporating product enhancement and fixes.

DSPLIB Software Updates will be posted as they become available in the same location you download this information. Source Code for previous releases will be kept public to prevent any customer problem in case we decide to discontinue or change the functionality of one of the DSPLIB functions. Make sure to read the readme.1st file available in the root directory of every release.

6.2 DSPLIB Customer Support

If you have any questions or want to report problems or suggestions regarding the C55x DSPLIB, contact Texas Instruments at dsph@ti.com.

We encourage the use of the software report form (report.txt) contained in the DSPLIB root directory to report any problem associated with the C55x DSPLIB.
Overview of Fractional Q Formats

Unless specifically noted, DSPLIB functions use Q15 format or to be more exact Q0.15. In a $Q_m.n$ format, there are $m$ bits used to represent the two’s complement integer portion of the number, and $n$ bits used to represent the two’s complement fractional portion. $m+n+1$ bits are needed to store a general $Q_m.n$ number. The extra bit is needed to store the sign of the number in the most-significant bit position. The representable integer range is specified by $(-2^m, 2^m)$ and the finest fractional resolution is $2^{-n}$.

For example, the most commonly used format is Q.15. Q.15 means that a 16-bit word is used to express a signed number between positive and negative 1. The most-significant binary digit is interpreted as the sign bit in any Q format number. Thus in Q.15 format, the decimal point is placed immediately to the right of the sign bit. The fractional portion to the right of the sign bit is stored in regular two’s complement format.

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A.1 Q3.12 Format

Q.3.12 format places the sign bit after the fourth binary digit from the right, and the next 12 bits contain the two’s complement fractional component. The approximate allowable range of numbers in Q.3.12 representation is $(-8,8)$ and the finest fractional resolution is $2^{-12} = 2.441 \times 10^{-4}$.

Table A–1. Q3.12 Bit Fields

<table>
<thead>
<tr>
<th>Bit</th>
<th>15</th>
<th>14</th>
<th>13</th>
<th>12</th>
<th>11</th>
<th>10</th>
<th>9</th>
<th>...</th>
<th>0</th>
</tr>
</thead>
<tbody>
<tr>
<td>Value</td>
<td>S</td>
<td>I3</td>
<td>I2</td>
<td>I1</td>
<td>Q11</td>
<td>Q10</td>
<td>Q9</td>
<td>...</td>
<td>Q0</td>
</tr>
</tbody>
</table>

A.2 Q.15 Format

Q.15 format places the sign bit at the leftmost binary digit, and the next 15 leftmost bits contain the two’s complement fractional component. The approximate allowable range of numbers in Q.15 representation is $(-1,1)$ and the finest fractional resolution is $2^{-15} = 3.05 \times 10^{-5}$.

Table A–2. Q.15 Bit Fields

<table>
<thead>
<tr>
<th>Bit</th>
<th>15</th>
<th>14</th>
<th>13</th>
<th>12</th>
<th>11</th>
<th>10</th>
<th>9</th>
<th>...</th>
<th>0</th>
</tr>
</thead>
<tbody>
<tr>
<td>Value</td>
<td>S</td>
<td>Q14</td>
<td>Q13</td>
<td>Q12</td>
<td>Q11</td>
<td>Q10</td>
<td>Q9</td>
<td>...</td>
<td>Q0</td>
</tr>
</tbody>
</table>

A.3 Q.31 Format

Q.31 format spans two 16-bit memory words. The 16-bit word stored in the lower memory location contains the 16 least-significant bits, and the higher memory location contains the most-significant 15 bits and the sign bit. The approximate allowable range of numbers in Q.31 representation is $(-1,1)$ and the finest fractional resolution is $2^{-31} = 4.66 \times 10^{-10}$.

Table A–3. Q.31 Low Memory Location Bit Fields

<table>
<thead>
<tr>
<th>Bit</th>
<th>15</th>
<th>14</th>
<th>13</th>
<th>12</th>
<th>...</th>
<th>3</th>
<th>2</th>
<th>1</th>
<th>0</th>
</tr>
</thead>
<tbody>
<tr>
<td>Value</td>
<td>Q15</td>
<td>Q14</td>
<td>Q13</td>
<td>Q12</td>
<td>...</td>
<td>Q3</td>
<td>Q2</td>
<td>Q1</td>
<td>Q0</td>
</tr>
</tbody>
</table>

Table A–4. Q.31 High Memory Location Bit Fields

<table>
<thead>
<tr>
<th>Bit</th>
<th>15</th>
<th>14</th>
<th>13</th>
<th>12</th>
<th>...</th>
<th>3</th>
<th>2</th>
<th>1</th>
<th>0</th>
</tr>
</thead>
<tbody>
<tr>
<td>Value</td>
<td>S</td>
<td>Q30</td>
<td>Q29</td>
<td>Q28</td>
<td>...</td>
<td>Q19</td>
<td>Q18</td>
<td>Q17</td>
<td>Q16</td>
</tr>
</tbody>
</table>
Appendix A

Calculating the Reciprocal of a Q15 Number

The most optimal method for calculating the inverse of a fractional number \((Y=1/X)\) is to normalize the number first. This limits the range of the number as follows:

\[
0.5 \leq X_{\text{norm}} < 1 \\
-1 \leq X_{\text{norm}} \leq -0.5
\]  

(1)

The resulting equation becomes

\[
Y = \frac{1}{(X_{\text{norm}} \cdot 2^{-n})}
\]

or

\[
Y = \frac{2^n}{X_{\text{norm}}}
\]  

(2)

where \(n = 1, 2, 3, \ldots, 14, 15\)

Letting \(Y_e = 2^n\):

\[
Y_e = 2^n
\]  

(3)

Substituting (3) into equation (2):

\[
Y = Y_e \cdot \frac{1}{X_{\text{norm}}}
\]  

(4)

Letting \(Y_m = \frac{1}{X_{\text{norm}}}\):

\[
Y_m = \frac{1}{X_{\text{norm}}}
\]  

(5)

Substituting (5) into equation (4):

\[
Y = Y_e \cdot Y_m
\]  

(6)

For the given range of \(X_{\text{norm}}\), the range of \(Y_m\) is:

\[
1 \leq Y_m < 2 \\
-2 \leq Y_m \leq -1
\]  

(7)

To calculate the value of \(Y_m\), various options are possible:

a) Taylor Series Expansion
b) 2nd,3rd,4th,... Order Polynomial (Line Of Best Fit)
c) Successive Approximation
The method chosen in this example is (c). Successive approximation yields the most optimum code versus speed versus accuracy option. The method outlined below yields an accuracy of 15 bits.

Assume \( Y_m(new) = \text{exact value of } \frac{1}{X_{\text{norm}}} \): \n
\[
Y_m(new) = \frac{1}{X_{\text{norm}}} \quad \text{(c1)}
\]

or

\[
Y_m(new) \times X = 1 \quad \text{(c2)}
\]

Assume \( Y_m(old) = \text{estimate of value } \frac{1}{X} \):

\[
Y_m(old) \times X_{\text{norm}} = 1 + D_{xy}
\]

or

\[
D_{xy} = Y_m(old) \times X_{\text{norm}} - 1 \quad \text{(c3)}
\]

where \( D_{xy} = \text{error in calculation} \)

Assume that \( Y_m(new) \) and \( Y_m(old) \) are related as follows:

\[
Y_m(new) = Y_m(old) - D_y
\]

where \( D_y = \text{difference in values} \)

Substituting (c2) and (c4) into (c3):

\[
Y_m(old) \times X_{\text{norm}} = Y_m(new) \times X_{\text{norm}} + D_{xy}
\]

\[
(Y_m(new) + D_y) \times X_{\text{norm}} = Y_m(new) \times X_{\text{norm}} + D_{xy}
\]

\[
Y_m(new) \times X_{\text{norm}} + D_y \times X_{\text{norm}} = Y_m(new) \times X_{\text{norm}} + D_{xy}
\]

\[
D_y \times X_{\text{norm}} = D_{xy}
\]

\[
D_y = D_{xy} \times \frac{1}{X_{\text{norm}}} \quad \text{(c5)}
\]

Assume that \( 1/X_{\text{norm}} \) is approximately equal to \( Y_m(old) \):

\[
D_y = D_{xy} \times Y_m(old) \quad \text{(approx)} \quad \text{(c6)}
\]

Substituting (c6) into (c4):

\[
Y_m(new) = Y_m(old) - D_{xy} \times Y_m(old)
\]

\[
\text{(c7)}
\]

Substituting for \( D_{xy} \) from (c3) into (c7):

\[
Y_m(new) = Y_m(old) - (Y_m(old) \times X_{\text{norm}} - 1) \times Y_m(old)
\]

\[
Y_m(new) = Y_m(old) - Y_m(old)^2 \times X_{\text{norm}} + Y_m(old)
\]

\[
Y_m(new) = 2 \times Y_m(old) - Y_m(old)^2 \times X_{\text{norm}}
\]

\[
\text{(c8)}
\]
If after each calculation we equate $Ym_{old}$ to $Ym_{new}$:

$$Ym_{old} = Ym_{new} = Ym$$

Then equation (c8) evaluates to:

$$Ym = 2 \times Ym - Ym^2 \times Xnorm$$  \hspace{1cm} (c9)

If we start with an initial estimate of $Ym$, then equation (c9) converges to a solution very rapidly (typically 3 iterations for 16-bit resolution).

The initial estimate can be obtained from a look-up table, from choosing a midpoint, or simply from linear interpolation. The method chosen for this problem is linear interpolation and accomplished by taking the complement of the least significant bits of the $Xnorm$ value.
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