

# Physics of Ultrasound

## TI Precision Labs – Ultrasonic Sensing

Presented by Akeem Whitehead

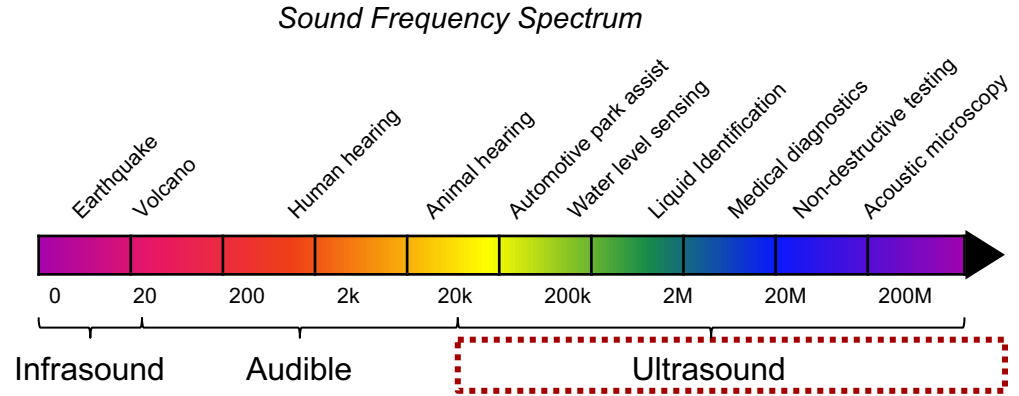
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# Definition of Ultrasound

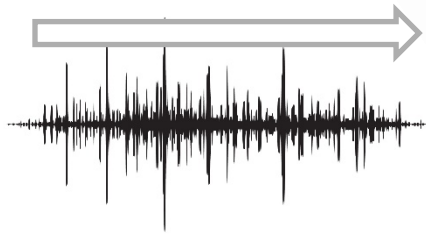
Ultrasound is defined as:

- sound waves with a frequency above the upper limit of human hearing at 20kHz.
- having physical properties that are identical to audible sound.
- a frequency some animals use for navigation and echo location.

This content will focus on ultrasonic systems that use transducers operating between 20kHz up to several GHz.



# Acoustics of Ultrasound



When ultrasound is a **stimulus**:  
*Generates and Emits Ultrasound Wave*

When ultrasound is a **sensation**:  
*Detects and Responds to Ultrasound Wave*

# Sound Propagation

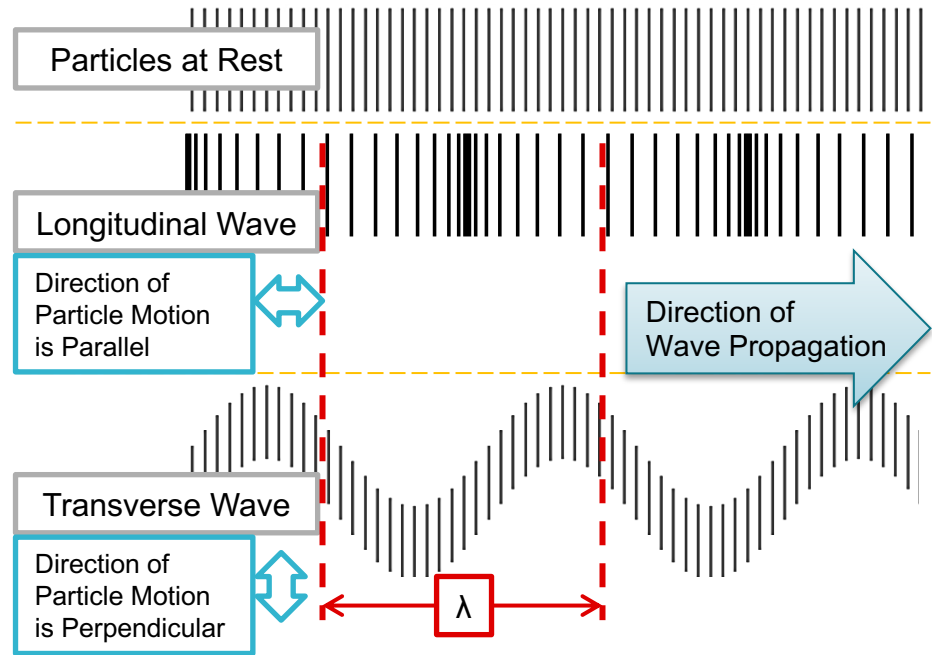
Ultrasound propagates as:

- longitudinal waves in air, water, plasma
- transverse waves in solids

The transducer's vibrating diaphragm is the source of the ultrasonic wave. As the source vibrates, the vibrations propagate away at the speed of sound to form a measurable ultrasonic wave.

The particles of the medium only transport the vibration of the ultrasonic wave, but do not travel with the wave. The medium can cause waves to be reflected, refracted, or attenuated over time.

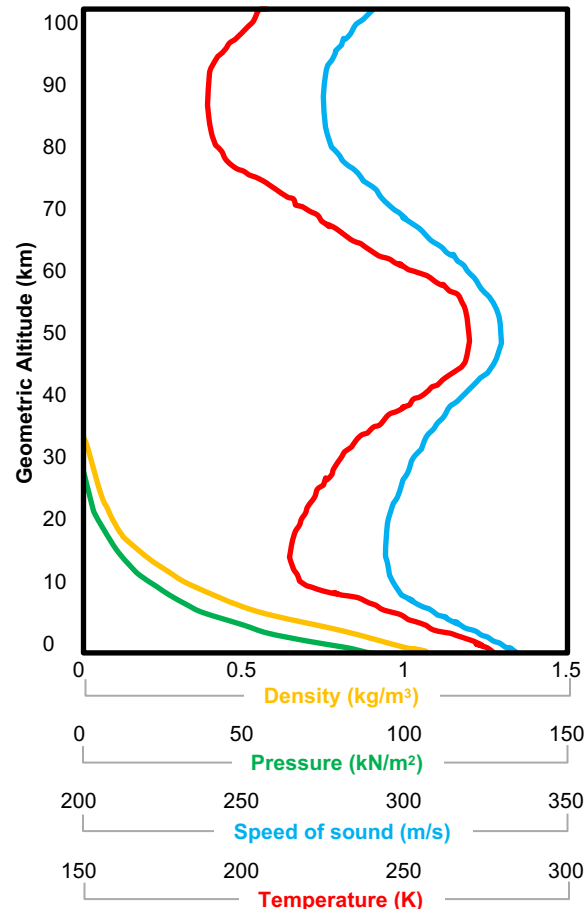
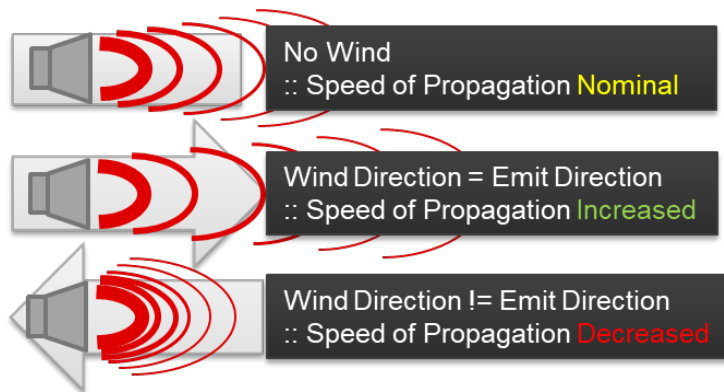
An ultrasonic wave cannot travel through a vacuum.



# Acoustic Properties

Ultrasonic propagation is affected by:

1. Relationship between density, pressure, and temperature to determine the speed of sound.
2. Motion of the transmission medium itself can increase or decrease the speed of sound.
3. Medium viscosity determines the rate at which sound attenuates.



# Sound Wave Properties

Ultrasound is interpreted as pressure and time with the following properties:

- Frequency, Period, or Wavelength
- Amplitude, Sound Pressure, or Intensity
- Speed of Sound
- Direction

Speed & Direction  $\rightarrow$  Velocity Vector

Wave Number & Direction  $\rightarrow$  Wave Vector

# Speed of Sound

- The speed of sound depends on the medium the waves pass through, and is a fundamental property of the material. Use the Newton–Laplace equation to solve for speed of sound:

$$c = \sqrt{\frac{K_s}{\rho}}$$

- where  $K_s$  is the elastic bulk modulus,  $c$  is the velocity of sound, and  $\rho$  is the density.
- The physical properties and the speed of sound change with ambient conditions, such as temperature and humidity.
  - In 20 °C air, at sea level, the speed of sound is approximately 343 m/s, and be calculated using the formula:
$$v = 331 + (0.6 \times T)$$
    - where  $v$  is velocity and  $T$  is temperature in Celsius

## Effects of Temperature On Air

| Temperature<br>$T$ (°C) | Speed of sound<br>$c$ (m/s) | Density of air<br>$\rho$ (kg/m <sup>3</sup> ) | Acoustic<br>Impedance<br>$z_0$ (Pa·s/m) |
|-------------------------|-----------------------------|---|---|
| 35                      | 351.88                      | 1.1455  | 403.2                                   |
| 30                      | 349.02                      | 1.1644  | 406.5                                   |
| 25                      | 346.13                      | 1.1839  | 409.4                                   |
| 20                      | 343.21                      | 1.2041  | 413.3                                   |
| 15                      | 340.27                      | 1.2250  | 416.9                                   |
| 10                      | 337.31                      | 1.2466  | 420.5                                   |
| 5                       | 334.32                      | 1.2690  | 424.3                                   |
| 0                       | 331.30                      | 1.2922  | 428.0                                   |
| -5                      | 328.25                      | 1.3163  | 432.1                                   |
| -10                     | 325.18                      | 1.3413  | 436.1                                   |
| -15                     | 322.07                      | 1.3673  | 440.3                                   |
| -20                     | 318.94                      | 1.3943  | 444.6                                   |
| -25                     | 315.77                      | 1.4224  | 449.1                                   |

# Sound Pressure

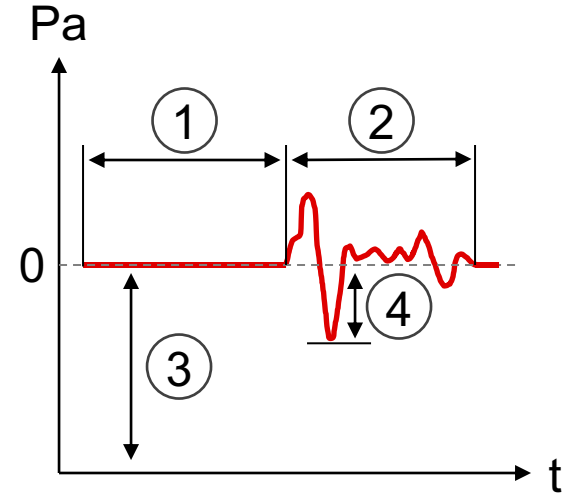
Sound pressure or acoustic pressure is the local pressure deviation from the ambient atmospheric pressure, caused by a sound wave.

The SI unit of sound pressure is the pascal (Pa). Sound pressure level (SPL) or acoustic pressure level is a logarithmic measure of the effective pressure of a sound relative to a reference value. Sound pressure level, denoted  $L_p$  and measured in dB, and is solved by the equation:

$$L_p = 20 \log_{10} \left( \frac{p}{p_0} \right) \text{ dB}$$

where

- $p$  is the root mean square sound pressure
- $p_0$  is the *reference sound pressure*



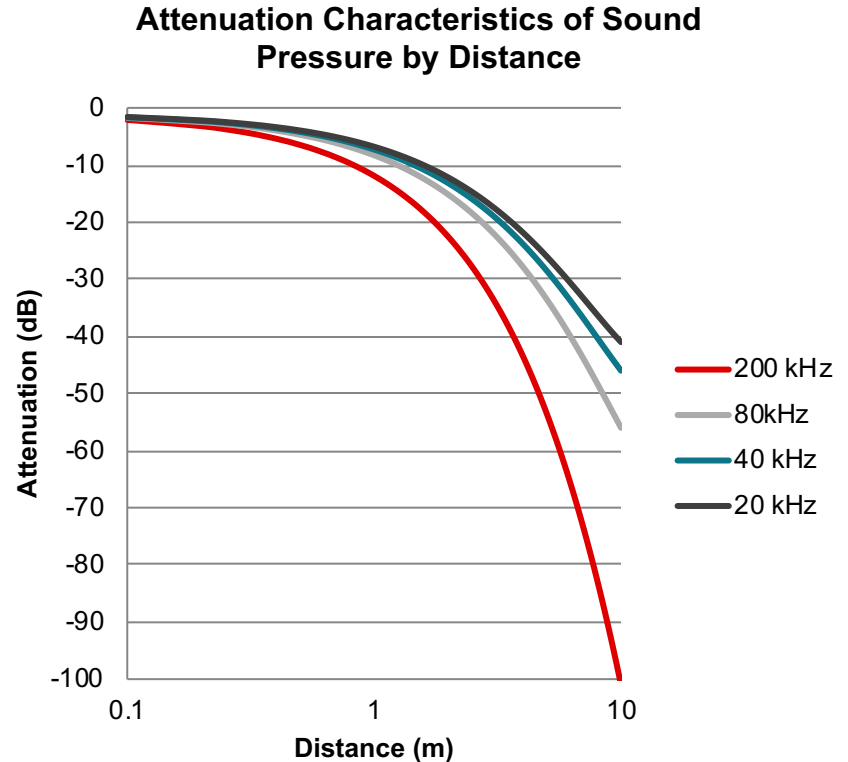
Sound pressure diagram:

1. silence
2. sound
3. atmospheric pressure
4. sound pressure



# Acoustic Attenuation

- When sound travels through a medium, its sound pressure diminishes with distance.
- Scattering and absorption of the sound wave are real-world attenuation factors.
  - Scattering is the reflection of the sound in directions other than its original direction of propagation
  - Absorption is the conversion of the sound energy to other forms of energy.



# Acoustic Impedance

**Acoustic impedance** is a measure of the opposition that a system presents to the acoustic flow resulting of an acoustic pressure applied to the system. The acoustic impedance ( $Z$ ) of a material is defined as the product of its density ( $\rho$ ) and acoustic velocity ( $V$ ):  **$Z = \rho V$**

Acoustic impedance is important in:

- the determination of acoustic transmission and reflection at the boundary of two materials having different acoustic impedances.
- the design of ultrasonic transducers.
- assessing absorption of sound in a medium.

*Acoustic Impedance by Material*

| Material    | Density ( $\text{kgm}^{-3}$ ) | Speed of Sound ( $\text{kgm}^{-1}$ ) | Acoustic Impedance ( $\text{kgm}^{-2}\text{s}^{-1} \times 10^6$ ) |
|-------------|-------------------------------|--------------------------------------|---|
| Air         | 1.3                           | 330                                  | 0.000429  |
| Sponge      | 100                           | 750                                  | 0.075   |
| Water       | 1000                          | 1450                                 | 1.45  |
| Soft Tissue | 1050                          | 1500                                 | 1.58  |
| Aluminum    | 2700                          | 6320                                 | 17.1  |
| Steel       | 7800                          | 5900                                 | 46.02   |
| Iron        | 7700                          | 5900                                 | 45.43   |
| Gold        | 19320                         | 3240                                 | 62.6  |

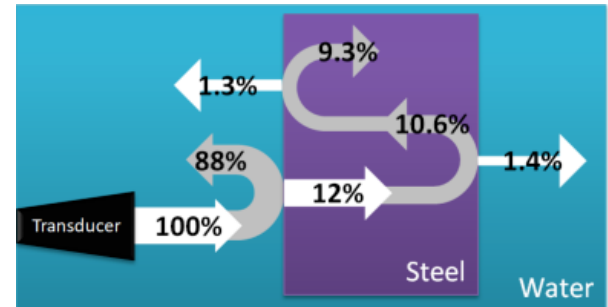
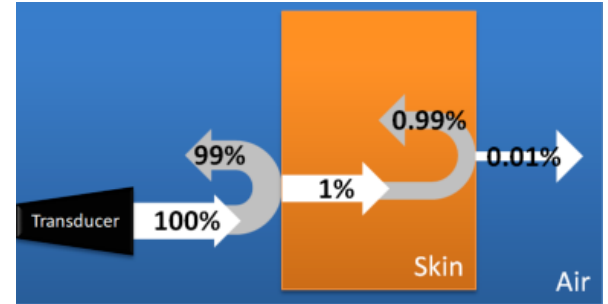
# Impedance Mismatch

This difference in  $Z$  is commonly referred to as the **impedance mismatch**. The greater the impedance mismatch, the greater the percentage of energy that will be reflected at the interface or boundary between one medium and another.

When the acoustic impedances of the materials on both sides of the boundary are known, the fraction of the incident wave intensity that is reflected can be calculated with the equation below. The value produced is known as the **reflection coefficient**.

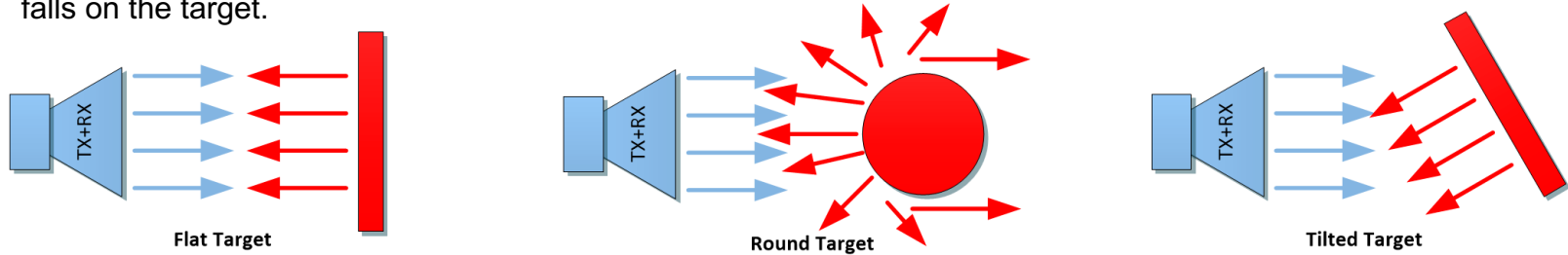
$$\text{Reflection Coefficient} = R = \left( \frac{Z_2 - Z_1}{Z_2 + Z_1} \right)^2$$

Reflection Coefficient Examples



# RADAR or SONAR Cross Section

RADAR or SONAR Cross Section (RCS or SCS) is the measure of a target's ability to reflect radar signals in the direction of the radar receiver. The conceptual definition of RCS includes the fact that not all of the radiated energy falls on the target.



| Target                 | Maximum Sonar Cross Section  | Advantage                     | Disadvantage                                 |
|------------------------|--|-------------------------------|--|
| Sphere                 | $\sigma_{\max} = \pi \times r^2$                                   | Nonspecular                   | Lowest RCS for size; radiates isotopically   |
| Cylinder               | $\sigma_{\max} = (2 \times \pi \times r \times h^2) / \lambda$     | Nonspecular along radial axis | Low RCS for size; specular along axis        |
| Flat rectangular plate | $\sigma_{\max} = (4 \times \pi \times l^2 \times w^2) / \lambda^2$ | Largest RCS for size          | Specular along both axes; difficult to align |

A target's RCS ( $\sigma$ ) can be visualized as the product of three factors:

$\sigma = \text{Projected cross section} \times \text{Reflectivity} \times \text{Directivity}$

- Reflectivity: The percent of intercepted power reradiated (scattered) by the target
- Directivity: The ratio of the power scattered back in the radar's direction to the power that would have been backscattered had the scattering been uniform in all directions (i.e. isotopically)

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