Analog Engineer's Circuit Single-supply, 2nd-order, multiple feedback high-pass filter circuit

TEXAS INSTRUMENTS

Amplifiers

Input		Output		Supply	
V _{iMin}	V _{iMax}	V _{oMin}	V _{oMax}	V _{cc}	V _{ee}
-2.45V	+2.45V	0.05V	4.95V	5V	0V

Gain	Cutoff Frequency (f _c)	Max Frequency (f _{max})	V _{ref}
-1V/V	1kHz	10kHz	2.5V

Design Description

The multiple-feedback (MFB) high-pass (HP) filter is a 2nd-order active filter. V_{ref} provides a DC offset to accommodate for single-supply applications. This HP filter inverts the signal (Gain = -1V/V) for frequencies in the pass band. An MFB filter is preferable when the gain is high or when the Q-factor is large (for example, 3 or greater).



Design Notes

- 1. Select an op amp with sufficient input common-mode range and output voltage swing.
- 2. Add V_{ref} to bias the input signal to meet the input common-mode range and output voltage swing.
- 3. Select the capacitor values first since standard capacitor values are more coarsely subdivided than the resistor values. Use high-precision, low-drift capacitor values to avoid errors in f_c.
- 4. To minimize the amount of slew-induced distortion, select an op amp with sufficient slew rate (SR).
- 5. For HP filters, the maximum frequency is set by the gain bandwidth (GBW) of the op amp. Therefore, be sure to select an op amp with sufficient GBW.

1



Design Steps

The first step in design is to find component values for the normalized cutoff frequency of 1 radian/second. In the second step, the cutoff frequency is scaled to the desired cutoff frequency with scaled component values.

The transfer function for a 2nd-order MFB high pass filter is given by:

$$H(s) = \frac{-s^{2}\frac{C_{1}}{C_{3}}}{s^{2} + s\frac{C_{1} + C_{2} + C_{3}}{R_{2} \times C_{2} \times C_{3}} + \frac{1}{R_{1} \times R_{2} \times C_{2} \times C_{3}}}$$

$$H(s) = \frac{-s^{2}\frac{C_{1}}{C_{3}}}{s^{2} + a_{1} \times s + a_{0}}$$
Here, $a_{1} = \frac{C_{1} + C_{2} + C_{3}}{R_{2} \times C_{2} \times C_{3}}$, $a_{0} = \frac{1}{R_{1} \times R_{2} \times C_{2} \times C_{3}}$
(3)

1. Set normalized values of C_1 , C_2 , and C_3 (C_{1n} , C_{2n} , and C_{3n}) and calculate normalized values of R_1 and R_2 (R_{1n} and R_{2n}) by setting w_c to 1radian/sec (or $f_c = 1 / (2 \times \pi)Hz$). For a 2nd-order Butterworth filter, (see the *Butterworth Filter Table* in the *Active Low-Pass Filter Design Application Report*).

$$\omega_c = 1 \frac{\text{radian}}{\text{second}} \rightarrow a_0 = 1, a_1 = \sqrt{2}, \text{ let } C_{1n} = C_{2n} = C_{3n} = 1 \text{ F}$$

Then
$$R_{1n} \times R_{2n} = 1$$
 or $R_{2n} = \frac{1}{R_{1n}}$, $a_1 = \frac{3}{R_{2n}} = \sqrt{2}$

:
$$R_{2n} = 2.1213$$
, $R_{1n} = \frac{1}{R_{2n}} = 0.4714$

2. Scale the component values and cutoff frequency. The resistor values are very small and capacitors values are unrealistic, hence these have to be scaled. The cutoff frequency is scaled from 1 radian/sec to w_0 . If we assume *m* to be the scaling factor, increase the resistors by *m* times, then the capacitor values have to decrease by 1/m times to keep the same cutoff frequency of 1 radian/sec. If we scale the cutoff frequency to be w_0 then the capacitor values have to be decreased by $1/w_0$. The component values for the design goals are calculated in step 3 and 4.

$$R_1 = R_{1n} \times m = (0.4714 \times m), R_2 = R_{2n} \times m = (2.1213 \times m)$$

$$C_1 = \frac{C_{1n}}{m \times \omega_0} = \frac{1}{m \times \omega_0} F$$
$$C_2 = \frac{C_{2n}}{m \times \omega_0} = \frac{1}{m \times \omega_0} F$$
$$C_3 = \frac{C_{3n}}{m \times \omega_0} = \frac{1}{m \times \omega_0} F$$

2 Single-supply, 2nd-order, multiple feedback high-pass filter circuit

3. Set C_1 , C_2 , and C_3 to 1nF and calculate m.

Given $\omega_0{=}2\times\pi\times f_c$, where $f_c{=}$ 1kHz,

$$C_1 = C_2 = C_3 = \frac{1}{m \times \omega_0} F = \frac{1}{m \times 2 \times \pi \times 1 \text{kHz}}$$

So, *m*= 159155

4. Calculate R_1 and R_2 based on m.

 $R_1 = R_{1n} \times m = 0.4714 \times 159155 \approx 75$ kΩ (Standard Value)

 $R_2 = R_{2n} \times m = 2.1213 \times 159155 \approx 336$ kΩ (Standard Value)

5. Calculate minimum required GBW and SR for f_{max} . Be sure to use the noise gain for GBW calculations. Do not use the signal gain of -1V/V.

 $\text{GBW} = 100 \times \text{Noise Gain} \times \text{f}_{max} = 100 \times 2 \times 10 \text{kHz} = 2 \text{MHz}$

 $SR = 2 \times \pi \times f_{max} \times V_{iMax} = 2 \times \pi \times 10 \text{kHz} \times 2.45 \text{V} = 0.154 \frac{\text{V}}{\text{\mu s}}$

The TLV9062 device has GBW of 10MHz and SR of 6.5V/µs, so the requirements are met.



Design Simulations



Filter Output in Response to a 5- V_{pp} , 10-kHz Input-Signal (Gain = -1V/V).

4



Filter Output in Response to a 5-V_{pp}, 100-Hz Input-Signal (Gain = -0.01V/V)



Design References

- 1. See Analog Engineer's Circuit Cookbooks for TI's comprehensive circuit library.
- 2. SPICE Simulation File: SBOC599.
- 3. TI Precision Labs.
- 4. Active Low-Pass Filter Design Application Report

Design Featured Op Amp

TLV9062				
V _{ss}	1.8V to 5.5V			
V _{inCM}	Rail-to-Rail			
Vout	Rail-to-Rail			
Vos	0.3mV			
lq	538µA			
lb	0.5pA			
UGBW	10MHz			
SR	6.5V/µs			
#Channels	1, 2, 4			
www.ti.com/product/TLV9062				

Design Alternate Op Amp

	TLV316	OPA325
V _{ss}	1.8V to 5.5V	2.2V to 5.5V
V _{inCM}	Rail-to-Rail	Rail-to-Rail
Vout	Rail-to-Rail	Rail-to-Rail
V _{os}	0.75mV	0.150mV
lq	400µA	650µA
lb	10pA	0.2pA
UGBW	10MHz	10MHz
SR	6V/µs	5V/µs
#Channels	1, 2, 4	1, 2, 4
	www.ti.com/product/TLV316	www.ti.com/product/OPA325

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