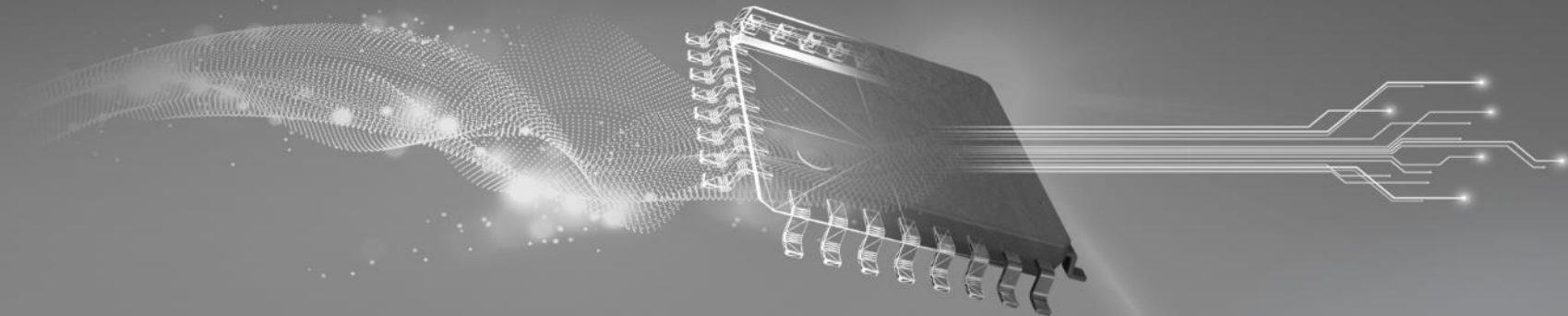


# TI TECH DAYS



## How to avoid design problems by using worst case analysis calculations

Louis Diana FAE SMTS

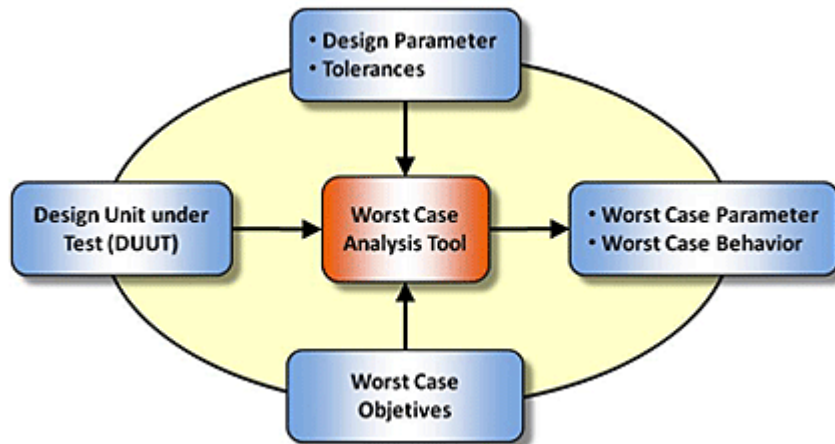
Texas Instruments

# Agenda

- Discussion on what is worst case analysis
- Different types of worst case analysis – i.e.: Extreme value, RSS
- Discussion on electronic component tolerances – resistors, capacitors, and Inductors, with an inductor saturation example.
- Example 1: Output voltage regulation. UVLO, and OVLO are very similar. Reference and IC tolerance will be added here.
- Example 2: MOSFET Power dissipation. FET and Diode tolerances will be added here.
- Example 3 : BJT Transistor Beta

# Worst case analysis definition

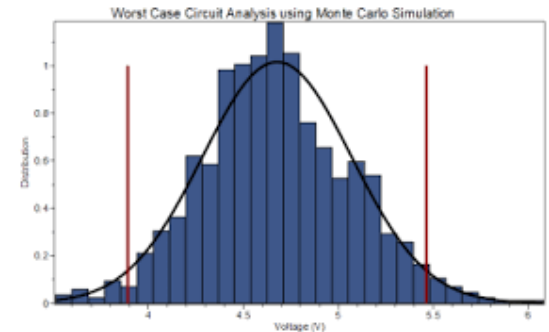
- A worst-case analysis is an assessment of a circuit's functional performance, accounting for tolerances, such as **Beginning of life (BOL)**, environmental (**Temperature**), aging **End of Life (EOL)**, and, in the case of Space applications, radiation tolerances.



# Worst case analysis method types

- **Extreme Value Analysis (EVA)** This is an estimate of the most extreme limits of the circuit's components and function.
- **Root Sum Square (RSS)** method works on a statistical approach. It assumes that most of the components fall to the mid of the tolerance zone rather than at the extreme ends.
- **Monte Carlo analysis**, in which parameters are randomly selected from a distribution, and the circuit simulated, anywhere from 1000 to 100000 times.

$$\Delta Y = \sqrt{\sum_{i=1}^n \delta_i^2}$$



# Worst case analysis component tolerances

## Resistor Tolerances

EOL obtained from component manufacturer, or engineering APL

$$\text{delT} := 75$$

$\text{tol\_rd1\_bol} := 0.1\%$	$\text{tol\_rd1\_eol} := 0.5\%$	$\text{tol\_rd1\_temp} := 25 \cdot 10^{-6} \cdot \text{delT}$	ppm /C
$\text{tol\_rd2\_bol} := 1\%$	$\text{tol\_rd2\_eol} := 0.5\%$	$\text{tol\_rd2\_temp} := 100 \cdot 10^{-6} \cdot \text{delT}$	ppm /C
$\text{tol\_rd3\_bol} := 1\%$	$\text{tol\_rd3\_eol} := 0.5\%$	$\text{tol\_rd3\_temp} := 250 \cdot 10^{-6} \cdot \text{delT}$	ppm /C
$\text{tol\_rd4\_bol} := 10\%$	$\text{tol\_rd4\_eol} := 0.5\%$	$\text{tol\_rd4\_temp} := 2000 \cdot 10^{-6} \cdot \text{delT}$	ppm /C

## Variations

$$\text{k1} := (\text{tol\_rd1\_bol} + \text{tol\_rd1\_eol} + \text{tol\_rd1\_temp})$$

$$\text{k1} = 7.875 \cdot 10^{-3}$$

$$\text{k2} := (\text{tol\_rd2\_bol} + \text{tol\_rd2\_eol} + \text{tol\_rd2\_temp})$$

$$\text{k2} = 0.023$$

$$\text{xr23} := 53.6 \cdot \text{k}$$

$$\text{xr23min} := \text{xr23} \cdot (1 - \text{k1})$$

$$\text{xr23min} = 5.318 \cdot 10^4$$

$$\text{xr23max} := \text{xr23} \cdot (1 + \text{k1})$$

$$\text{xr23max} = 5.402 \cdot 10^4$$

# Worst case analysis component tolerances

## Capacitor Tolerances

EOL obtained from component manufacturer, or engineering APL

$$\text{delT} := 75$$

$$\text{tol\_npo\_bol} := 5\%$$

$$\text{tol\_npo\_eol} := 0.5\%$$

$$\text{tol\_npo\_temp} := 30 \cdot 10^{-6} \cdot \text{delT}$$

$$\text{tol\_bx\_bol} := 10\%$$

$$\text{tol\_bx\_eol} := 21\%$$

$$\text{tol\_bx\_temp} := 15\%$$

$$\text{tol\_x7r\_bol} := 10\%$$

$$\text{tol\_x7r\_eol} := 21\%$$

$$\text{tol\_x7r\_temp} := 15\%$$

BX characteristics are identical to X7R dielectric, with the added restriction that the Temperature-Voltage Coefficient (TVC) is not to exceed -25%  $\Delta C$  at rated voltage, over the operating temperature range (-55°C to 125°C).

## Variations

$$k3 := (\text{tol\_npo\_bol} + \text{tol\_npo\_eol} + \text{tol\_npo\_temp})$$

$$k3 = 0.057$$

$$k4 := (\text{tol\_bx\_bol} + \text{tol\_bx\_eol} + \text{tol\_bx\_temp})$$

$$k4 = 0.46$$

$$k5 := (\text{tol\_x7r\_bol} + \text{tol\_x7r\_eol} + \text{tol\_x7r\_temp})$$

$$k5 = 0.46$$

$$\text{alc12} := 39 \cdot \text{p}$$

$$\text{alc12min} := \text{alc12} \cdot (1 - k3)$$

$$\text{alc12max} := \text{alc12} \cdot (1 + k3)$$

$$\text{alc12min} = 3.833 \cdot 10^{-11}$$

$$\text{alc12max} = 3.967 \cdot 10^{-11}$$

# Worst case analysis component tolerances

## Inductor Tolerances

5. DC current at 25°C that causes an inductance drop of 30% (typ) from its value without current.

Part number <sup>1</sup>	Inductance <sup>2</sup> ±20% (µH)	DCR (mOhms) <sup>3</sup>		SRF typ <sup>4</sup> (MHz)	Isat <sup>5</sup> (A)	I <sub>rms</sub> (A) <sup>6</sup>	
		typ	max			20°C rise	40°C rise
XAL7030-161ME_	0.16	1.15	1.26	158	60.0	24.9	32.5
XAL7030-301ME_	0.30	1.75	1.92	101	41.0	21.0	27.6
XAL7030-601ME_	0.60	3.00	3.30	72	36.0	18.0	23.0
XAL7030-102ME_	1.0	4.55	5.00	52	28.0	16.1	21.8
XAL7030-152ME_	1.5	7.60	8.36	39	23.5	11.9	15.0
XAL7030-222ME_	2.2	13.7	15.07	29	18.0	10.0	12.9
XAL7030-272ME_	2.7	15.7	17.30	32	12.8	9.2	11.4
XAL7030-332ME_	3.3	19.5	21.45	25	12.3	8.0	10.0
XAL7030-472ME_	4.7	26.1	30.00	21	10.1	6.9	9.0
XAL7030-562ME_	5.6	28.1	32.32	17	9.8	5.3	7.3
XAL7030-682ME_	6.8	45.0	51.75	15	8.7	4.4	6.8
XAL7030-822ME_	8.2	53.0	60.94	13	8.4	2.9	5.9
XAL7030-103ME_	10	60.4	69.46	12	7.7	2.6	5.3

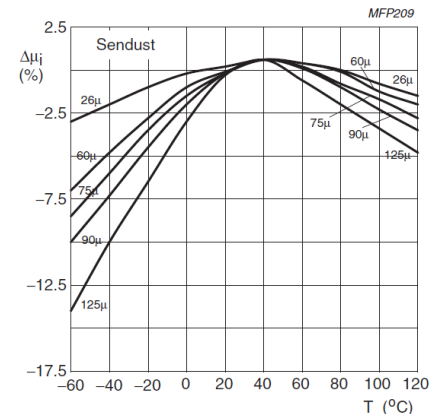
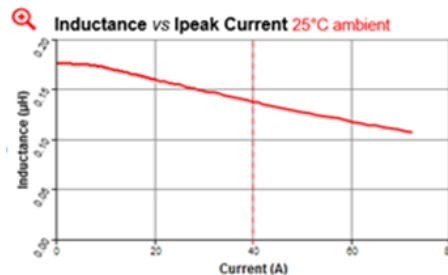
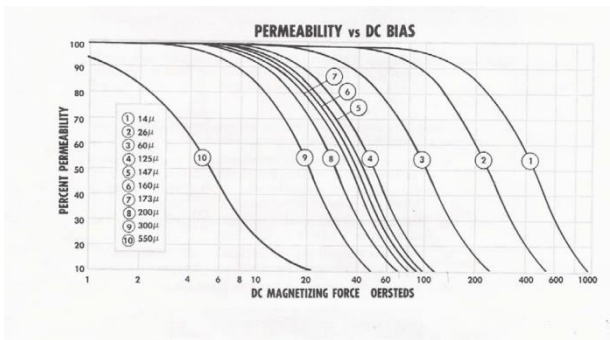


Fig.2 Initial permeability as a function of temperature.



$$L = \frac{4 \cdot 3.14 \cdot \mu \cdot \text{turns}^2 \cdot (Ae)}{l \cdot 10^8}$$

Where:

Inductance = Henry's

$\mu$  = core permeability

N = number of turns

$A_e$  = core cross-section (mm<sup>2</sup>)

$l$  = core magnetic path length (mm)

# Worst case analysis inductance rolloff example

Example of saturation current

$V_{in} = 12V$        $V_o = .9V$   
 $V_{inmax} = 13.2V$     $I_{omax} = 40A$   
 $V_{inmin} = 10.8V$     $I_{omin} = 4A$   
 $f = 650kHz$

Now what happens if I push  $I_{omax}$  to 60A and reduce the inductance by 30%

$V_{in} = 12V$        $V_o = .9V$   
 $V_{inmax} = 13.2V$     $I_{omax} = 60A$   
 $V_{inmin} = 10.8V$     $I_{omin} = 4A$   
 $f = 650kHz$

$L_{out} = 160nH$

$L_{out} = 112nH$

$I_{peak} = 45.6A$

Peak inductor current

$I_{peak} = 68.7A$

Peak inductor current

Rule of thumb derate  $I_{sat}$  by 30 to 40%



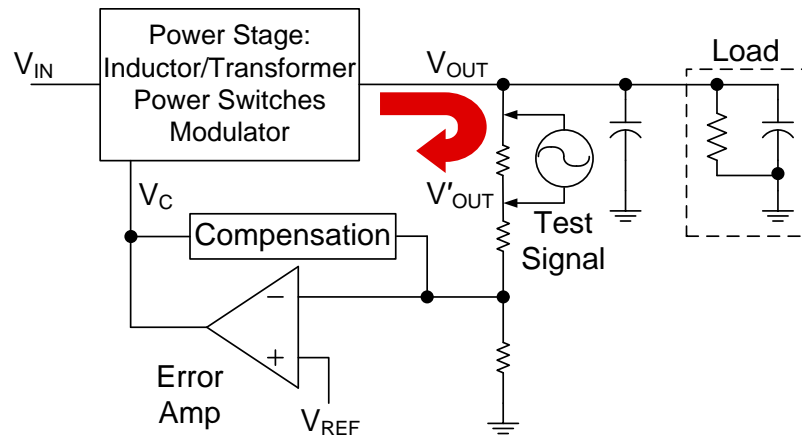
# Worst case analysis output regulation example

## Problem statement

- What is my worst case output voltage regulation

## Procedure

- Find tolerances for  $V_{ref}$ , error-amp, and resistor divider.
- Write equation for feedback regulation
- Calculate sensitivity of variables.
- Solve equation



# Worst case analysis output regulation example

## Reference tolerance

$$\text{tol\_TL431\_bol} := 0.5\% \quad \text{tol\_TL431\_eol} := .25\% \quad \text{tol\_TL431\_temp} := 60 \cdot 10^{-6} \cdot \text{delT}$$

## Reference Variation

$$V_{\text{ref}} := 2.495$$

$$\text{TL431vrefmin} := V_{\text{ref}} \cdot (1 - \text{tol\_TL431\_bol}) \cdot (1 - \text{tol\_TL431\_eol}) \cdot (1 - \text{tol\_TL431\_temp})$$

$$\text{TL431vrefmin} = 2.465$$

$$\text{TL431vrefmax} := V_{\text{ref}} \cdot (1 + \text{tol\_TL431\_bol}) \cdot (1 + \text{tol\_TL431\_eol}) \cdot (1 + \text{tol\_TL431\_temp})$$

$$\text{TL431vrefmax} = 2.525$$

- Reference Voltage Tolerance at 25°C
  - 0.5% (B Grade)
  - 1% (A Grade)
  - 2% (Standard Grade)

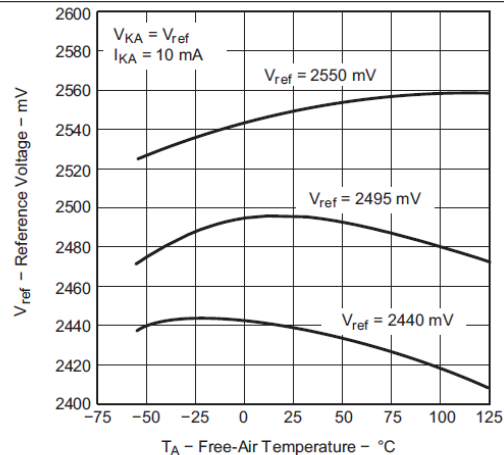


Figure 1. Reference Voltage vs Free-Air Temperature

# Worst case analysis output regulation example

## Op-amp tolerance

Op-amp dc error sources include:

- Input offset voltage  $V_{OS}$
- Input bias current  $I_B$
- Input offset current  $I_{OS}$
- Open loop gain

From LM158 Data sheet:

$V_{os\_bol} = 7\text{mV}$  from  $-55\text{c}$  to  $125\text{c}$

$V_{os\_temp} = 15\mu\text{V/c}$

$V_{os\_eol} = \text{hard to find check with Manufacturer}$

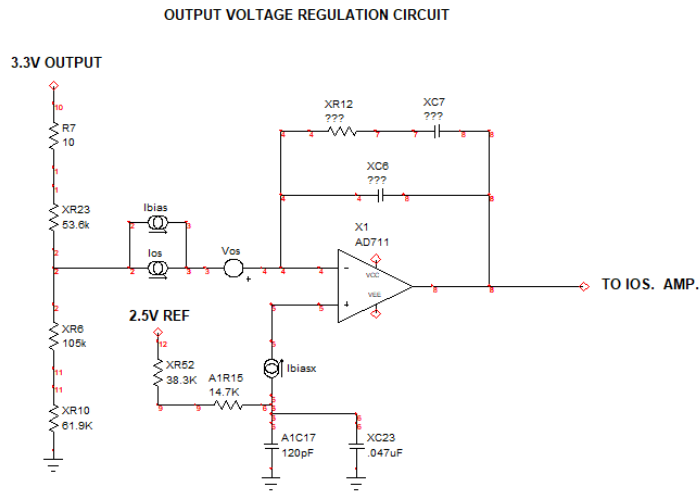
$I_{b\_bol} = 300\text{nA}$  from  $-55\text{c}$  to  $125\text{c}$ ,

$I_{os\_bol} = 100\text{nA}$  from  $-55\text{c}$  to  $125\text{c}$

$I_{os\_temp} = 200\text{pA/c}$ ,  $I_{os\_eol} = \text{hard to find check with Manufacturer}$

Open loop gain min =  $35\text{V/mV} = 35000$

Open loop gain typ =  $140\text{V/mV} = 140000$



# Worst case analysis output regulation example

Below is a sensitivity calculation to show which parts should be minimized or maximized

$$\text{Vonom}(\text{Vref}, \text{Vos}, \text{Vbiasnom}, \text{Vbias\_gainnom}, \text{xr23}, \text{r7}, \text{xr10}, \text{xr6}) := \left( \begin{array}{l} \text{Vref} + \text{Vos} \dots \\ + \text{Vbiasnom} \dots \\ + \text{Vbias\_gainnom} \end{array} \right) \cdot \frac{(\text{xr23} + \text{r7} + \text{xr10} + \text{xr6})}{\text{xr10} + \text{xr6}}$$

$$\frac{d}{d\text{Vref}} \text{Vonom}(\text{Vref}, \text{Vos}, \text{Vbiasnom}, \text{Vbias\_gainnom}, \text{xr23}, \text{r7}, \text{xr10}, \text{xr6}) = 1.321$$

$$\frac{d}{d\text{Vos}} \text{Vonom}(\text{Vref}, \text{Vos}, \text{Vbiasnom}, \text{Vbias\_gainnom}, \text{xr23}, \text{r7}, \text{xr10}, \text{xr6}) = 1.321$$

$$\frac{d}{d\text{Vbiasnom}} \text{Vonom}(\text{Vref}, \text{Vos}, \text{Vbiasnom}, \text{Vbias\_gainnom}, \text{xr23}, \text{r7}, \text{xr10}, \text{xr6}) = 1.321$$

$$\frac{d}{d\text{Vbias\_gainnom}} \text{Vonom}(\text{Vref}, \text{Vos}, \text{Vbiasnom}, \text{Vbias\_gainnom}, \text{xr23}, \text{r7}, \text{xr10}, \text{xr6}) = 1.321$$

$$\frac{d}{d\text{xr23}} \text{Vonom}(\text{Vref}, \text{Vos}, \text{Vbiasnom}, \text{Vbias\_gainnom}, \text{xr23}, \text{r7}, \text{xr10}, \text{xr6}) = 1.504 \cdot 10^{-5}$$

$$\frac{d}{d\text{r7}} \text{Vonom}(\text{Vref}, \text{Vos}, \text{Vbiasnom}, \text{Vbias\_gainnom}, \text{xr23}, \text{r7}, \text{xr10}, \text{xr6}) = 1.504 \cdot 10^{-5}$$

$$\frac{d}{d\text{xr10}} \text{Vonom}(\text{Vref}, \text{Vos}, \text{Vbiasnom}, \text{Vbias\_gainnom}, \text{xr23}, \text{r7}, \text{xr10}, \text{xr6}) = -4.83 \cdot 10^{-6}$$

$$\frac{d}{d\text{xr6}} \text{Vonom}(\text{Vref}, \text{Vos}, \text{Vbiasnom}, \text{Vbias\_gainnom}, \text{xr23}, \text{r7}, \text{xr10}, \text{xr6}) = -4.83 \cdot 10^{-6}$$

# Worst case analysis output regulation example

## Resistor divider tolerance

$$\text{Reqmax} := \frac{1}{\left( \frac{1}{x_{r23\text{max}} + r_{7\text{max}}} + \frac{1}{x_{r10\text{min}} + x_{r6\text{min}}} \right)}$$

$$\text{Reqmax} = 4.074 \cdot 10^4$$

$$a_{1r15\text{max}} = 1.503 \cdot 10^4$$

$$\text{Reqmin} := \frac{1}{\left( \frac{1}{x_{r23\text{min}} + r_{7\text{min}}} + \frac{1}{x_{r10\text{max}} + x_{r6\text{max}}} \right)}$$

$$\text{Reqmin} = 4.041 \cdot 10^4$$

$$a_{1r15\text{min}} = 1.437 \cdot 10^4$$

# Worst case analysis output regulation example

## Voltage error due to the offset current, bias current, A1r15 and Req

$$V_{biasmin} := Req_{min} \cdot (I_{bias} - I_{os}) - I_{bias} \cdot (a_{1r15max} + x_{r52max}) \quad V_{biasmin} = -6.685 \cdot 10^{-4}$$

$$V_{biasmax} := Req_{max} \cdot (I_{bias} + I_{os}) - I_{bias} \cdot (a_{1r15min} + x_{r52min}) \quad V_{biasmax} = 1.748 \cdot 10^{-4}$$

$$V_{biasnom} := \frac{V_{biasmax} + V_{biasmin}}{2} \quad V_{biasnom} = -2.469 \cdot 10^{-4}$$

## Voltage error due to the gain in the error amplifier

$$V_{out} = (V_{pos} - V_{neg}) \times A_v \quad V_{in} = V_{pos} - V_{neg} \quad V_{bias\ gain} = V_{in}$$

$v_{oh} := 5$  **Voh is the Vdd voltage on the error amp. therefore the maximum output voltage on the error amp.**

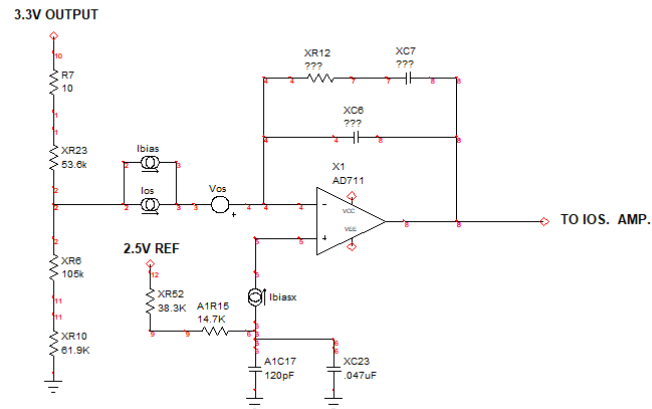
$$V_{bias\_gainmax} := \frac{v_{oh}}{OLG_{min}} \quad V_{bias\_gainmax} = 1.429 \cdot 10^{-4}$$

$$V_{bias\_gainmin} := \frac{v_{oh}}{OLG_{max}} \quad V_{bias\_gainmin} = 3.571 \cdot 10^{-5}$$

**This is the min. and max. voltage required for op-amp operation**

$$V_{bias\_gainnom} := \frac{V_{bias\_gainmax} + V_{bias\_gainmin}}{2} \quad V_{bias\_gainnom} = 8.929 \cdot 10^{-5}$$

OUTPUT VOLTAGE REGULATION CIRCUIT



# Worst case analysis output regulation example

The total output voltage error due to Vref, Vos, Vbias, Req, and A1r15

$$V_{\text{omax}} := (v_{\text{refmax}} + V_{\text{os}} + V_{\text{biasmax}} + V_{\text{bias\_gainmax}}) \cdot \frac{(x_{r23\text{max}} + r_{7\text{max}} + x_{r10\text{min}} + x_{r6\text{min}})}{x_{r10\text{min}} + x_{r6\text{min}}} \quad V_{\text{omax}} = 3.37$$

$$V_{\text{omin}} := (v_{\text{refmin}} - V_{\text{os}} + V_{\text{biasmin}} + V_{\text{bias\_gainmin}}) \cdot \frac{(x_{r23\text{min}} + r_{7\text{min}} + x_{r10\text{max}} + x_{r6\text{max}})}{x_{r10\text{max}} + x_{r6\text{max}}} \quad V_{\text{omin}} = 3.236$$

The percent delta for Vout is as follows

$$V_{\text{onom}} := 3.3$$

$$V_{\text{odelta\%pos}} := \frac{V_{\text{omax}} - V_{\text{onom}}}{V_{\text{onom}}} \cdot 100$$

$$V_{\text{odelta\%pos}} = 2.126$$

$$V_{\text{odelta\%neg}} := \frac{V_{\text{onom}} - V_{\text{omin}}}{V_{\text{onom}}} \cdot 100$$

$$V_{\text{odelta\%neg}} = 1.926$$

# Worst case analysis MOSFET power dissipation example

## Problem statement

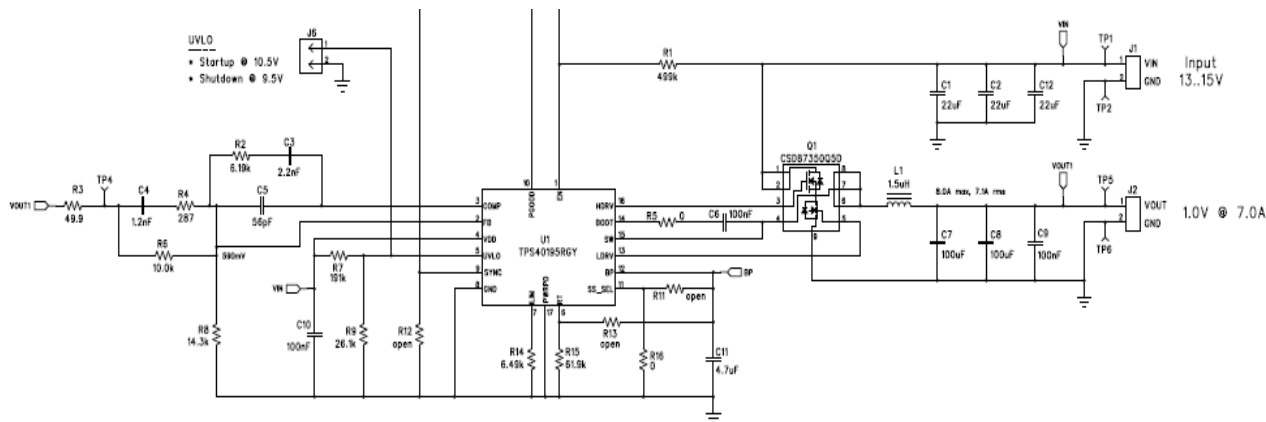
- The FET's in my PS are getting hot

## Possible causes

- Not enough heat sink
- Shoot through

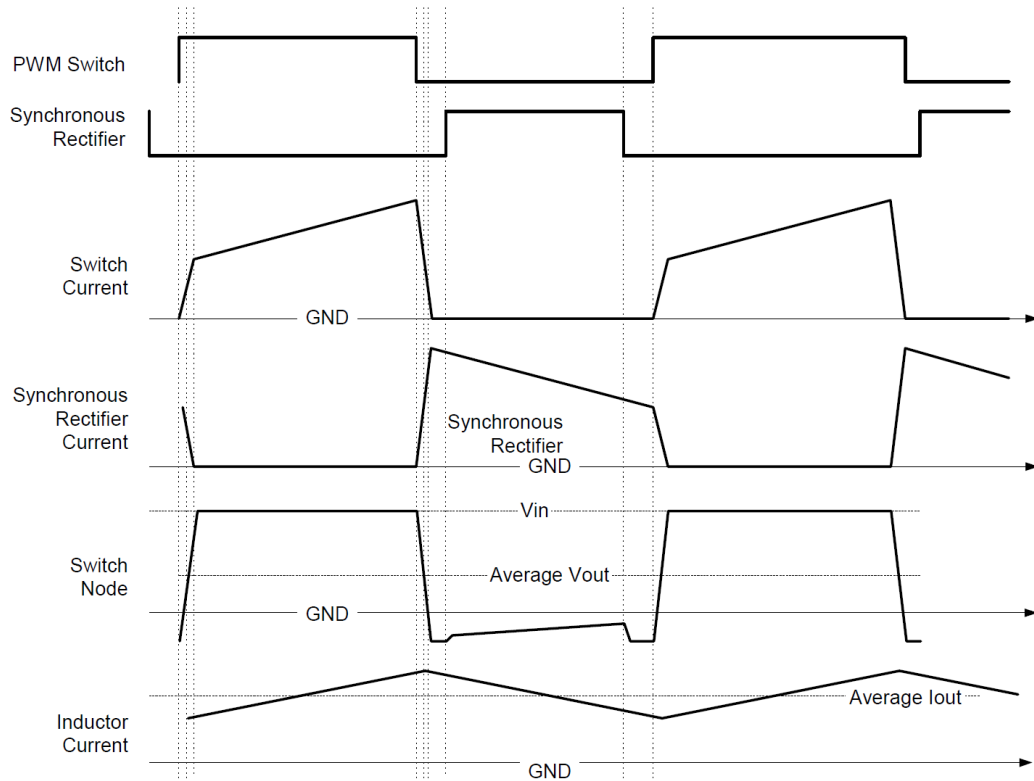
## Solution

- WCA on FET power dissipation





# Worst case analysis MOSFET power dissipation example



## Procedure

- Find tolerances for  $R_{ds}$ ,  $Q_g$  total gate charge,  $Q_{gs}$  charge gate to source,  $Q_{gd}$  charge gate to drain,  $Q_{oss}$  output charge, body drain diode forward voltage, and controller dead time.
- Write equation and Analyze  $R_{ds}$  conducted losses, switching loss, and gate drive loss for top FET.
- Write equation and Analyze  $R_{ds}$  conducted losses, body drain diode loss, and gate drive loss for bottom FET
- Add up all losses

# Worst case analysis component tolerances

## MOSFET tolerance

CSD87350Q5D Synchronous Buck NexFET™ Power Block

### Rds goes up as temp goes up

Rds\_bot = 20%

Rds\_tempmax = 63%

Rds\_tempmin = -40%

$$R_{dson\_top} := 5 \cdot 10^{-3} \cdot \Omega$$

$$R_{dson\_bot} := 1.2 \cdot 10^{-3} \cdot \Omega$$

$$R_{dmin\_top} = 2.4 \times 10^{-3} \Omega$$

$$R_{dmin\_bot} = 5.76 \times 10^{-4} \Omega$$

$$R_{dmax\_top} = 9.78 \times 10^{-3} \Omega$$

$$R_{dmax\_bot} = 2.347 \times 10^{-3} \Omega$$

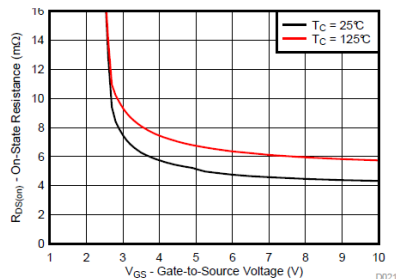


Figure 20. Control MOSFET  $R_{DS(on)}$  vs  $V_{GS}$

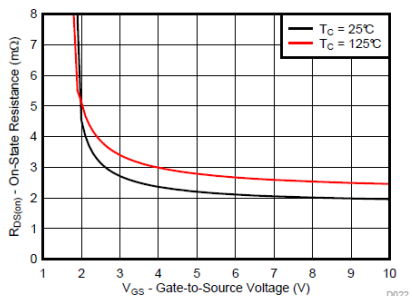


Figure 21. Sync MOSFET  $R_{DS(on)}$  vs  $V_{GS}$

### Total gate charge

qtotal\_top := 8.4nC

qtotal\_bot := 30%

qtotal\_bot := 20nC

$$q_{total\_min\_top} = 5.88 \times 10^{-9} C$$

$$q_{total\_min\_bot} = 1.4 \times 10^{-8} C$$

$$q_{total\_max\_top} = 1.092 \times 10^{-8} C$$

$$q_{total\_max\_bot} = 2.6 \times 10^{-8} C$$

### Gate charge gate to drain and gate to source

Qgd\_top := 1.6nC

Qgd\_bot := 30%

Qgs\_top := 2.6nC

Qgs\_bot := 30%

$$Q_{gd\_min\_top} = 1.12 \times 10^{-9} C$$

$$Q_{gs\_min\_top} = 1.82 \times 10^{-9} C$$

$$Q_{gd\_max\_top} = 2.08 \times 10^{-9} C$$

$$Q_{gs\_max\_top} = 3.38 \times 10^{-9} C$$

# Worst case analysis component tolerances

## MOSFET tolerance

### Qoss output charge

$$\begin{aligned} Q_{oss\_bol} &:= 30\% & Q_{oss\_top} &:= 9.7\text{nC} & Q_{oss\_min\_top} &= 6.79 \times 10^{-9} \text{ C} & Q_{oss\_bot} &:= 28\text{nC} & Q_{oss\_min\_bot} &= 1.96 \times 10^{-8} \text{ C} \\ & & & & Q_{oss\_max\_top} &= 1.261 \times 10^{-8} \text{ C} & & & Q_{oss\_max\_bot} &= 3.64 \times 10^{-8} \text{ C} \end{aligned}$$

### Body drain diode forward voltage

$$V_{body} := .8\text{V}$$

$$V_{body\_bol} := 25\% \quad V_{body\_temphot} := 30\% \text{ At } 125\text{C} \quad V_{body\_tempcold} := 22.5\% \text{ At } -50\text{C}$$

$$V_{body\_max} = 1.3 \text{ V}$$

$$V_{body\_min} = 0.42 \text{ V}$$

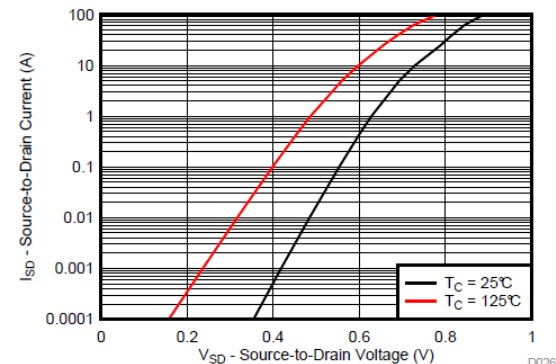


Figure 25. Sync MOSFET Body Diode

# Worst case analysis component tolerances

## TPS40190 Controller dead time tolerance for body diode PWR calculation

Deadtime\_HSOFF\_LSON := 50ns      Deadtime\_LSOFF\_HSON := 25ns      DT\_bol := 20%

Deadtime\_HSOFF\_LSON\_min =  $4 \times 10^{-8}$  s      Deadtime\_LSOFF\_HSON\_min =  $2 \times 10^{-8}$  s

Deadtime\_HSOFF\_LSON\_max =  $6 \times 10^{-8}$  s      Deadtime\_LSOFF\_HSON\_max =  $3 \times 10^{-8}$  s

## Power block delay time tolerance for body diode PWR calculation

Td\_FET\_bol := 30%      Turnon\_dly\_HS := 7ns      Turnon\_dly\_LS := 8ns      Turnoff\_dly\_HS := 13ns      Turnoff\_dly\_LS := 33ns

Trise\_HS := 17ns      Trise\_LS := 10ns      Tfall\_HS := 2.3ns      Tfall\_LS := 4.7ns

Turnon\_dly\_HSmin =  $4.9 \times 10^{-9}$  s      Trise\_HSmin =  $1.19 \times 10^{-8}$  s      Turnoff\_dly\_HSmin =  $9.1 \times 10^{-9}$  s      Tfall\_HSmin =  $1.61 \times 10^{-9}$  s

Turnon\_dly\_HSmax =  $9.1 \times 10^{-9}$  s      Trise\_HSmax =  $2.21 \times 10^{-8}$  s      Turnoff\_dly\_HSmax =  $1.69 \times 10^{-8}$  s      Tfall\_HSmax =  $2.99 \times 10^{-9}$  s

Turnon\_dly\_LSmin =  $5.6 \times 10^{-9}$  s      Trise\_LSmin =  $7 \times 10^{-9}$  s      Turnoff\_dly\_LSmin =  $2.31 \times 10^{-8}$  s      Tfall\_LSmin =  $3.29 \times 10^{-9}$  s

Turnon\_dly\_LSmax =  $1.04 \times 10^{-8}$  s      Trise\_LSmax =  $1.3 \times 10^{-8}$  s      Turnoff\_dly\_LSmax =  $4.29 \times 10^{-8}$  s      Tfall\_LSmax =  $6.11 \times 10^{-9}$  s

# Worst case analysis MOSFET power dissipation example

## 1) First calculate conducted loss

$$I_{rms\_top\_fet} = 10.462 \text{ A}$$

$$P_{fet\_cond\_topmax} := I_{rms\_top\_fet}^2 \cdot R_{dsmax\_top} \quad P_{fet\_cond\_topmax} = 1.07 \cdot \text{W} \quad (\text{Cond losses})$$

$$P_{fet\_cond\_topmin} := I_{rms\_top\_fet}^2 \cdot R_{dsmin\_top} \quad P_{fet\_cond\_topmin} = 0.263 \cdot \text{W} \quad (\text{Cond losses})$$

$$I_{rms\_bot\_fet} = 38.677 \text{ A}$$

$$P_{fet\_cond\_botmax} := I_{rms\_bot\_fet}^2 \cdot R_{dsmax\_bot} \quad P_{fet\_cond\_botmax} = 3.511 \text{ W} \quad (\text{Cond losses})$$

$$P_{fet\_cond\_botmin} := I_{rms\_bot\_fet}^2 \cdot R_{dsmin\_bot} \quad P_{fet\_cond\_botmin} = 0.862 \text{ W} \quad (\text{Cond losses})$$

## 2) Calculate top FET switching loss

$$I_g := 1 \text{ A}$$

$$P_{sw\_fet\_top} := V_{inmax} \cdot f_{max} \cdot \left[ \frac{I_{pfet\_top} \cdot (Q_{gd\_max\_top} + Q_{gs\_max\_top})}{I_g} + \frac{Q_{oss\_max\_top} + Q_{oss\_max\_bot}}{2} \right] \quad P_{sw\_fet\_top} = 1.502 \text{ W} \quad (\text{Switching losses})$$

$$T_{sw} := 18 \cdot \text{ns}$$

$$P_{d\_SW\_FET} := 2 \cdot \left[ \frac{1}{T_{min}} \cdot \int_0^{T_{sw}} \left( V_{inmax} \cdot \frac{t}{T_{sw}} \right) \cdot \left[ I_{pfet\_top} \cdot \left( 1 - \frac{t}{T_{sw}} \right) \right] dt \right] \quad P_{d\_SW\_FET} = 1.517 \cdot \text{W} \quad (\text{Switching losses})$$

Bottom FET has body diode voltage across it at turn on/off therefore loss is in the body diode

# Worst case analysis MOSFET power dissipation example

## 3) calculate gate drive losses

PARAMETER	TEST CONDITIONS	Q1 CONTROL FET			Q2 SYNC FET			UNIT
		MIN	TYP	MAX	MIN	TYP	MAX	
R <sub>G</sub> Series gate resistance			1.3	3	0.8	2	Ω	

PARAMETER	TEST CONDITIONS	MIN	TYP	MAX	UNIT
<b>OUTPUT DRIVERS</b>					
R <sub>HDHI</sub> High-side driver pull-up resistance	V <sub>BOOT</sub> - V <sub>SW</sub> = 4.5 V, I <sub>HDRV</sub> = -100 mA		3	6	Ω
R <sub>HDLO</sub> High-side driver pull-down resistance	V <sub>BOOT</sub> - V <sub>SW</sub> = 4.5 V, I <sub>HDRV</sub> = 100 mA		1.5	3	Ω
R <sub>LDHI</sub> Low-side driver pull-up resistance	I <sub>LDRV</sub> = -100 mA		2.5	5	Ω
R <sub>LDLO</sub> Low-side driver pull-down resistance	I <sub>LDRV</sub> = 100 mA		0.8	1.5	Ω

$$V_{gate} := 8V$$

$$P_{g\_dr\_top} := f \cdot q_{total\_max\_top} \cdot V_{gate} \quad P_{g\_dr\_top} = 0.028 \text{ W} \quad \text{(Gate losses)}$$

$$Act\_gate\_drive\_pwr\_top := \frac{1.3}{3} \cdot P_{g\_dr\_top} \quad Act\_gate\_drive\_pwr\_top = 0.012 \text{ W}$$

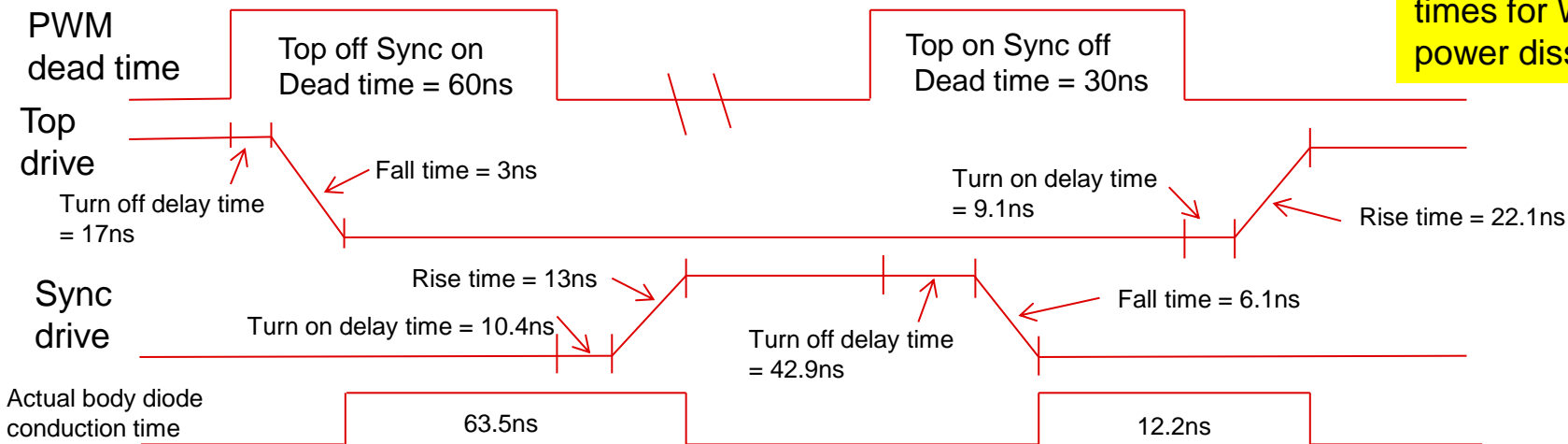
$$P_{g\_dr\_bot} := f \cdot q_{total\_max\_bot} \cdot V_{gate} \quad P_{g\_dr\_bot} = 0.068 \text{ W} \quad \text{(Gate losses)}$$

$$Act\_gate\_drive\_pwr\_LS := \frac{.8}{2.5} \cdot P_{g\_dr\_bot} \quad Act\_gate\_drive\_pwr\_LS = 0.022 \text{ W}$$

# Worst case analysis MOSFET power dissipation example

## 3) Calculate body diode losses

Used maximum times for WC power dissipation



$$T_{delay1} := \text{Deadtime\_HSoff\_LSON\_max} - \text{Turnoff\_dly\_HSmax} - \text{Tfall\_HSmax} + \text{Turnon\_dly\_LSmax} + \text{Trise\_LSmax}$$

$$T_{delay1} = 6.351 \times 10^{-8} \text{ s}$$

$$T_{delay2} := \text{Deadtime\_LSoff\_HSON\_max} - \text{Turnoff\_dly\_LSmax} - \text{Tfall\_LSmax} + \text{Turnon\_dly\_HSmax} + \text{Trise\_HSmax}$$

$$T_{delay2} = 1.219 \times 10^{-8} \text{ s}$$

$$P_{body\_diode\_max} := V_{body\_min} \cdot I_{omax} \cdot \frac{T_{delay1} + T_{delay2}}{T_{min}}$$

$$P_{body\_diode\_max} = 0.475 \text{ W}$$

# Worst case analysis MOSFET power dissipation example

## 4) Add up all the top and bottom FET losses

$$P_{fet\_tot\_top\_min} := P_{fet\_cond\_topmin} + P_{sw\_fet\_top} + Act\_gate\_drive\_pwr\_top$$

$$P_{fet\_tot\_top\_min} = 1.777 \text{ W} \quad \text{(Total top FET losses Cond min)}$$

$$P_{fet\_tot\_top\_max} := P_{fet\_cond\_topmax} + P_{sw\_fet\_top} + Act\_gate\_drive\_pwr\_top$$

$$P_{fet\_tot\_top\_max} = 2.584 \text{ W} \quad \text{(Total top FET losses max)}$$

$$P_{fet\_tot\_bot\_min} := P_{fet\_cond\_botmin} + Act\_gate\_drive\_pwr\_LS + P_{body\_diode\_max}$$

$$P_{fet\_tot\_bot\_min} = 1.359 \text{ W} \quad \text{(Total bottom FET losses cond min)}$$

$$P_{fet\_tot\_bot\_max} := P_{fet\_cond\_botmax} + Act\_gate\_drive\_pwr\_LS + P_{body\_diode\_max}$$

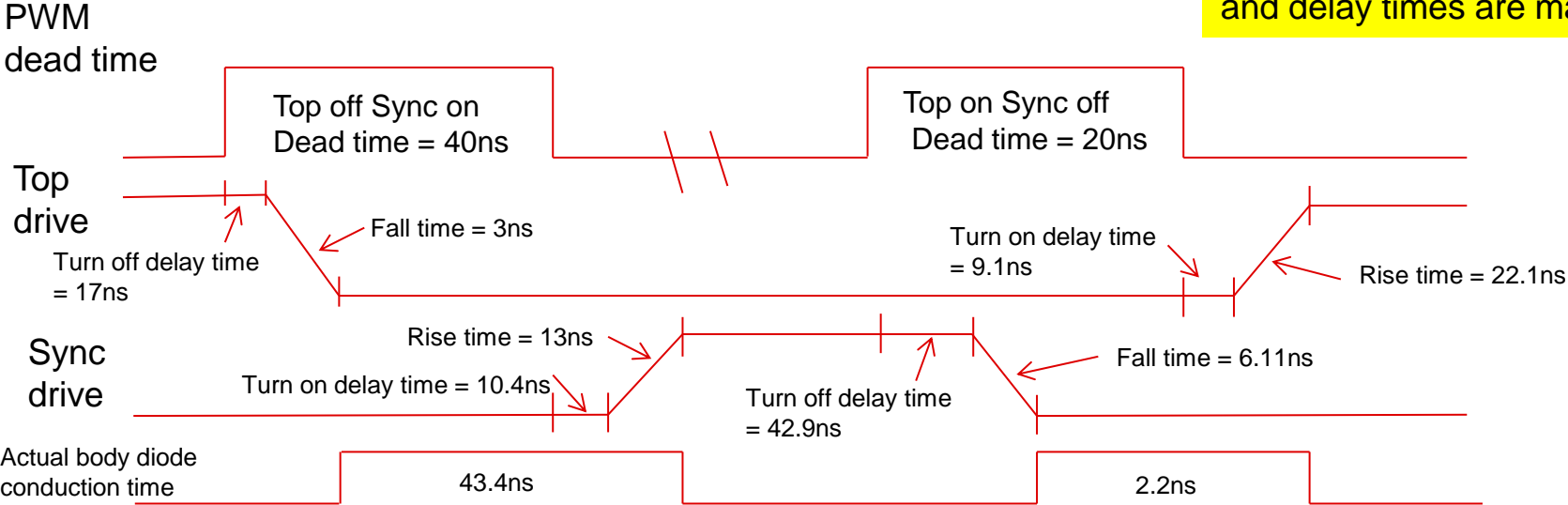
$$P_{fet\_tot\_bot\_max} = 4.008 \text{ W} \quad \text{(Total bottom FET losses max)}$$



# Worst case analysis MOSFET

## Cross conduction and Timing issues

Look at what happens when dead time is minimum and delay times are maximum



# Worst case analysis BJT transistor example

## Problem statement

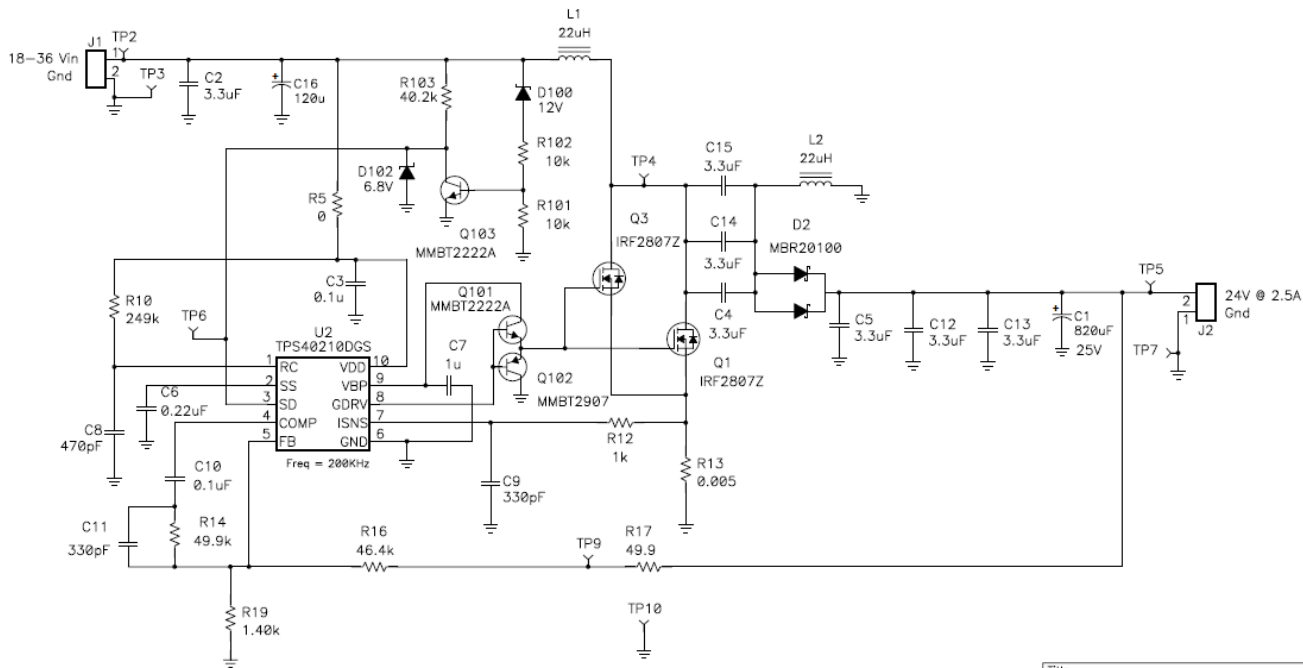
- My PS wont turn on at cold temperature

## Possible causes

- Not enough start up voltage/current
- Enable circuit
- Not enough gate drive

## Solution

- WCA Enable circuit



Title 24V@2.5A SEPIC

# Worst case analysis BJT transistor example

## Procedure

- Calculate base current
- Calculate collector current
- Calculate necessary Beta to maintain transistor in on state

## Resistor Variations

$$\text{tol\_res\_bol} := 1\% \quad \text{tol\_res\_eol} := 0.5\% \quad \text{tol\_res\_temp} := 100 \cdot 10^{-6} \cdot \text{delT}$$

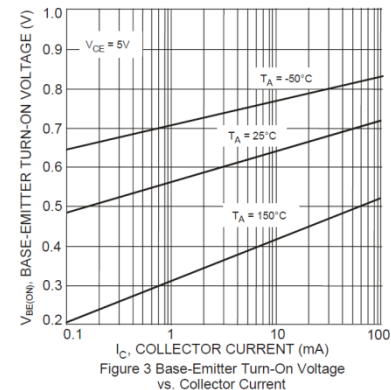
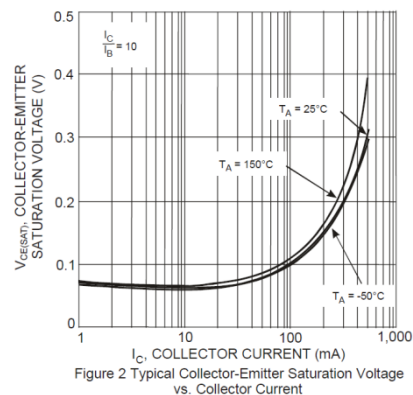
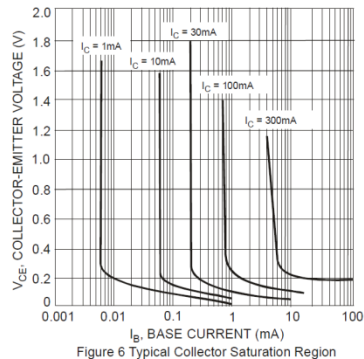
$$R101 := 10\text{-K}\Omega \quad R102 := 10\text{-K}\Omega \quad R103 := 40.2\text{-K}\Omega$$

$$R101_{\min} = 9.8 \times 10^3 \Omega \quad R102_{\min} = 9.8 \times 10^3 \Omega \quad R103_{\min} = 3.94 \times 10^4 \Omega$$

$$R101_{\max} = 1.02 \times 10^4 \Omega \quad R102_{\max} = 1.02 \times 10^4 \Omega \quad R103_{\max} = 4.1 \times 10^4 \Omega$$

$$I_{b\min} := \frac{V_{\text{inmin2}} - V_{D100\max} - V_{\text{besatmax}}}{R102_{\max}}$$

$$I_{C\max} := \frac{V_{\text{inmin2}} - V_{\text{cesatmax}}}{R103_{\min}}$$



Voltage tolerances

$$V_{\text{inmin2}} := 18\text{V} \quad V_{\text{inmax2}} := 36\text{V} \quad V_{\text{besatmin}} := .6\text{V} \quad V_{\text{besatmax}} := 1.2\text{V}$$

$$V_{\text{cesatmax}} := .3\text{V} \quad V_{D100\max} := 12.6\text{V}$$

$$I_{b\min} = 4.118 \times 10^{-4} \text{ A}$$

$$I_{C\max} = 4.493 \times 10^{-4} \text{ A}$$

# Worst case analysis BJT transistor example

## Electrical Characteristics (@T<sub>A</sub> = +25°C, unless otherwise specified.)

Characteristic	Symbol	Min	Max	Unit	Test Condition
<b>ON CHARACTERISTICS (Note 10)</b>					
DC Current Gain	h <sub>FE</sub>	35	—	—	I <sub>C</sub> = 100μA, V <sub>CE</sub> = 10V
		50	—		I <sub>C</sub> = 1.0mA, V <sub>CE</sub> = 10V
		75	—		I <sub>C</sub> = 10mA, V <sub>CE</sub> = 10V
		100	300		I <sub>C</sub> = 150mA, V <sub>CE</sub> = 10V
		40	—		I <sub>C</sub> = 500mA, V <sub>CE</sub> = 10V
		50	—		I <sub>C</sub> = 10mA, V <sub>CE</sub> = 10V, T <sub>A</sub> = -55°C
		35	—		I <sub>C</sub> = 150mA, V <sub>CE</sub> = 1.0V
Collector-Emitter Saturation Voltage	V <sub>CE(SAT)</sub>	—	0.3 1.0	V	I <sub>C</sub> = 150mA, I <sub>B</sub> = 15mA I <sub>C</sub> = 500mA, I <sub>B</sub> = 50mA
Base-Emitter Saturation Voltage	V <sub>BE(SAT)</sub>	0.6	1.2 2.0	V	I <sub>C</sub> = 150mA, I <sub>B</sub> = 15mA I <sub>C</sub> = 500mA, I <sub>B</sub> = 50mA

$$B := \frac{I_{Cmax}}{I_{bmin}}$$

$$B = 1.091$$

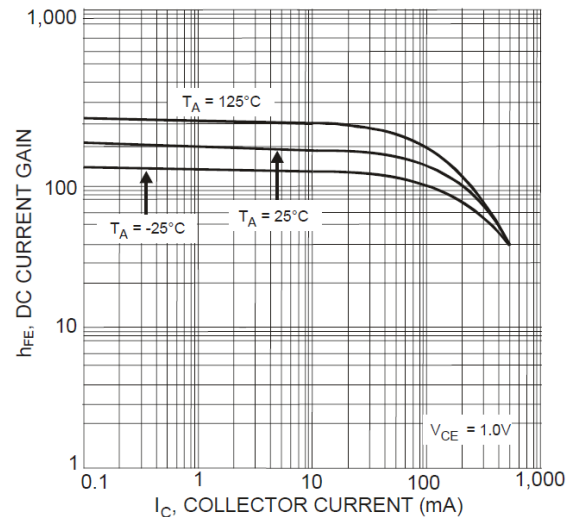


Figure 1 Typical DC Current Gain vs. Collector Current

# Summary

- Analyze the circuit to determine potential issues in the design
- Decide what type of analysis needs to be performed - EV, RSS, Monte Carlo
- Write an equation for the potential issues you found
- Determine the variables in each equation
- Determine the BOL, EOL, and temp tolerances for each variable from the manufactures DS or company APL
- Calculate the tolerances for each
- Calculate the behavioral equations using the variable tolerances to determine the worst case parameters for your design

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